

# Non-SUSY String vacua & Exceptional Field Theory

Emanuel Malek

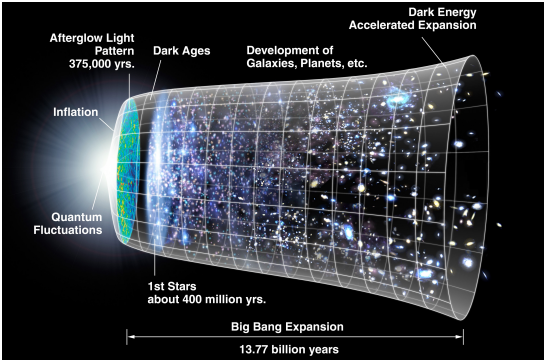
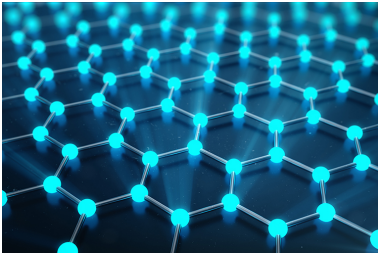
Humboldt-Universität zu Berlin



Rencontres Theoriciens Paris Seminar  
6th January 2022

with Samtleben & Giambrone, Guarino, Nicolai, Sterckx, Trigiante

# Quest for non-SUSY vacua



# Problems

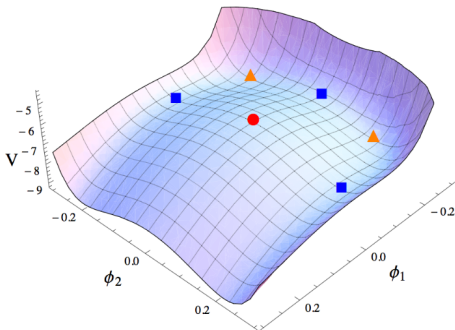
Construct & study physically relevant solutions

- ▶ Solve second-order PDEs
- ▶ Fluctuations
- ▶ Instabilities

# Lower-dimensional models

Useful: lower-dimensional model

- ▶ Finite number of fields  $\rightarrow$  easier solutions
- ▶ Study fluctuations  $\rightarrow$  stability
- ▶ Captures only part of physics



## Non-SUSY AdS vacua

$$\text{AdS} \times M_{\text{compact}}$$

- ▶ No scale separation  $\rightarrow$  no effective theory
- ▶ “Consistent truncation” instead
- ▶ All solutions of lower-d theory  $\rightarrow$  solutions of full higher-d theory
- ▶ Difficult to construct

# Lower-dimensional models vs string theory

Easier to construct solutions & study subset of fluctuations

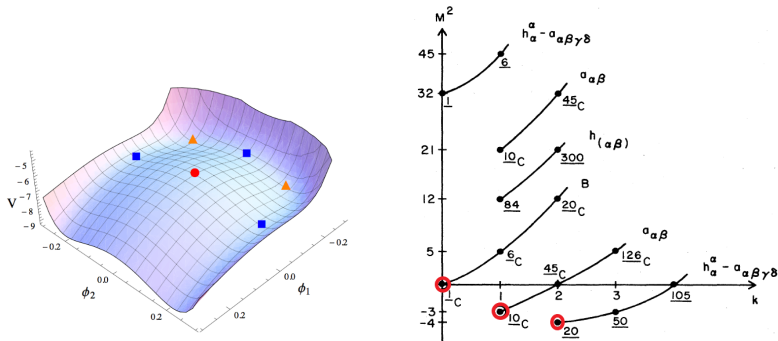


FIG. 2. Mass spectrum of scalars.

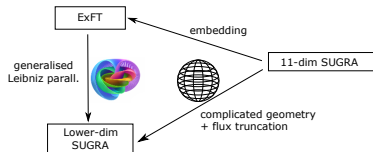
- ▶ Most non-SUSY AdS solutions already unstable! c.f. [Comsa, Firsching, Fischbacher '19], [Bobev, Fischbacher, Gautason, Pilch '20]
- ▶ Is “zero-mode” stability enough?

Two goals:

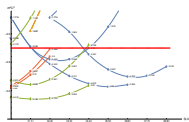
Uplift lower-dim gauged supergravity to string theory?

Full spectrum of masses  $\Leftrightarrow$  perturbative stability in 10-/11-d?

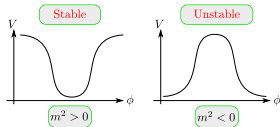
# Exceptional Field Theory & consistent truncations



## Kaluza-Klein spectroscopy

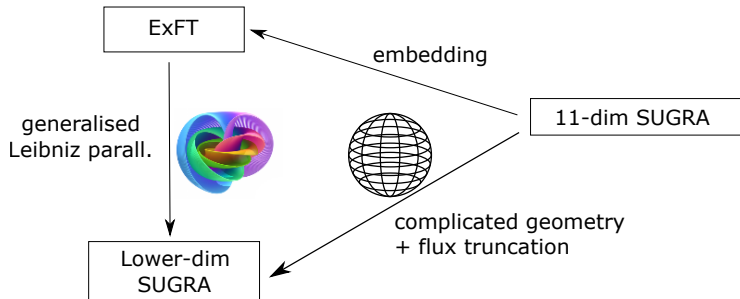


## Stability of non-SUSY AdS<sub>4</sub>





# Exceptional field theory & consistent truncations



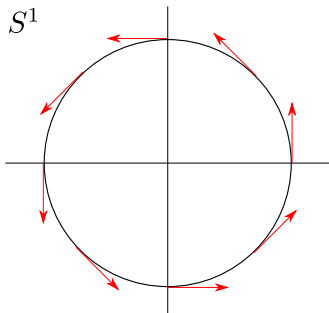
## Consistent truncation

Non-linear embedding of lower-dimensional  
supergravity into 10-/11-d supergravity

- ▶ All solutions of lower-d SUGRA  $\rightarrow$  solutions of 10-/11-d SUGRA
- ▶ Non-linearity: highly non-trivial!
- ▶ Symmetry arguments crucial for consistency & construction

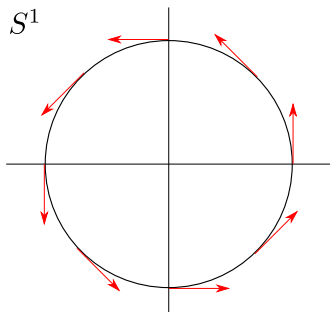
## Consistent truncation on group manifold

Symmetry arguments crucial for consistency, e.g.  
group manifold



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group manifold



$$U_m{}^\mu \in \text{GL}(D)$$

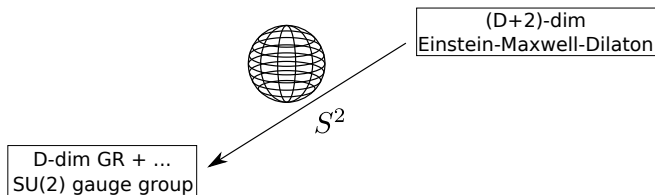
$$L_{U_m} U_n = f_{mn}{}^p U_p$$

$$g_{\mu\nu}(x, y) = g_{mn}(x) (U^{-1})_\mu{}^m(y) (U^{-1})_\nu{}^n(y)$$

# Larger symmetry groups from generalising geometry

Symmetry argument for other consistent truncations?

$$S = \int d^{D+2}x \sqrt{|g|} \left( R_g - (\nabla\phi)^2 - e^{\alpha\phi} F^2 \right)$$



$$ds_{D+2}^2 = \gamma^{\frac{1}{D}} \left( \Delta^{\frac{1}{D}} ds_D^2 + g^{-2} \Delta^{-\frac{D-1}{D}} T_{ij}^{-1} \mathfrak{D}\mu^i \mathfrak{D}\mu^j \right),$$

$$e^{\sqrt{\frac{2(D)}{D+1}} \hat{\phi}} = \Delta^{-1} \gamma^{\frac{D-1}{D+1}},$$

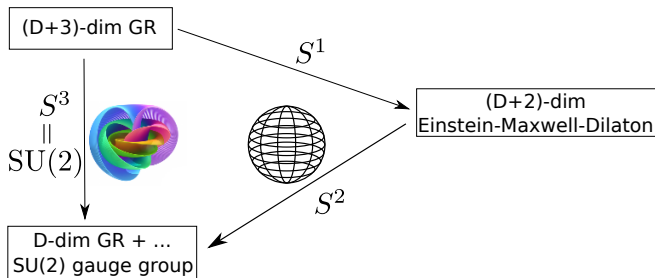
$$\hat{F}_2 = \frac{1}{2} \epsilon_{ijk} \left( g^{-1} \Delta^{-2} \mu^i \mathfrak{D}\mu^j \wedge \mathfrak{D}\mu^k - 2g^{-1} \Delta^{-2} \mathfrak{D}\mu^i \wedge \mathfrak{D} T_{jl} T_{km} \mu^l \mu^m - \Delta^{-1} F_{(2)}^{ij} T_{kl} \mu^l \right).$$

[Cvetic, Lü, Pope '00]

# Larger symmetry groups from generalising geometry

Symmetry argument for other consistent truncations?

$$S = \int d^{D+3}x \sqrt{|G|} (R_G)$$

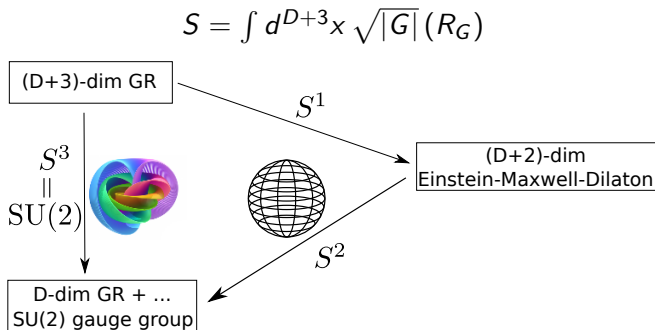


$$U_m{}^\mu \in \text{GL}(3)$$

$$L_{U_m} U_n = f_{mn}{}^p U_p$$

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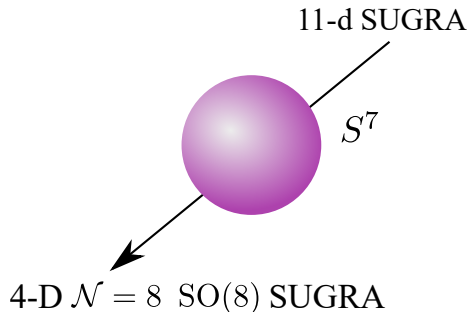
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## Consistent truncations beyond group manifolds

Consistent truncations of 10-d/11-d SUGRA beyond group manifolds?



[de Wit, Nicolai '82]



# Exceptional Field Theory

[Berman, Perry '10], [Coimbra, Strickland-Constable, Waldram '11],  
[Hohm, Samtleben, '13], ...

Exceptional Field Theory: Unify metric + fluxes of  
supergravity

IIB supergravity on  $M_4 \times C_6$ :

$$\{g, \Phi, B_{(2)}, A_{(0)}, A_{(2)}, A_{(4)}, \dots\} = \mathcal{M}_{MN} \in \frac{E_{7(7)}}{SU(8)}.$$

Diffeo + gauge transf  $\rightarrow$  generalised vector field  $V^M \in \mathbf{56}$  of  $E_{7(7)}$   
Lie derivative  $\rightarrow$  generalised Lie derivative

$$\mathcal{L}_V = V^M \partial_M - (\partial \times_{adj} V) = \text{diffeo} + \text{gauge transf},$$

$$\text{with } \partial_M = (\partial_i, \partial^i, \partial^{jk}, \dots) = (\partial_i, 0, \dots, 0).$$

# Exceptional Field Theory = reformulation of supergravity

Exceptional Field Theory: Reformulation of IIB supergravity

$$\{g, \Phi, B_{(2)}, A_{(0)}, A_{(2)}, A_{(4)}, \dots\} = \mathcal{M}_{MN}$$

$$L = e^{-2\Phi} \left( R - \frac{1}{12} H_{\mu\nu\lambda} H^{\mu\nu\lambda} + 4\partial_\mu \Phi \partial^\mu \Phi \right) + \dots$$

with  $H_{\mu\nu\rho} = 3\partial_{[\mu} B_{\nu\rho]}$ .

# Exceptional Field Theory = reformulation of supergravity

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$$\begin{aligned} L &= e^{-2\Phi} \left( R - \frac{1}{12} H_{\mu\nu\lambda} H^{\mu\nu\lambda} + 4\partial_\mu \Phi \partial^\mu \Phi \right) + \dots \\ &= \mathcal{M}^{MN} \partial_M \mathcal{M}^{PQ} \partial_N \mathcal{M}_{PQ} + \dots \end{aligned}$$

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Exceptional Field Theory: Reformulation of IIB supergravity

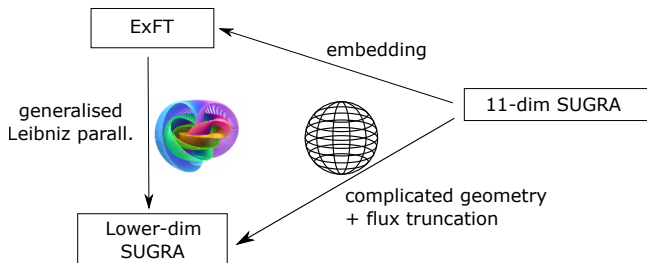
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Generalised Lie derivative  $\Rightarrow$  generalised Ricci scalar

# Exceptional Field Theory and consistent truncations

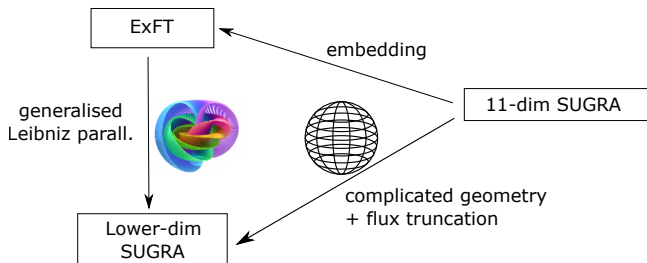
Consistent truncations captured by  
“generalised group manifolds” in ExFT



$$U_A^M \in E_{7(7)}$$
$$\mathcal{L}_{U_A} U_B = X_{AB}^C U_C$$
$$\mathcal{M}_{MN}(x, Y) = M_{AB}(x) (U^{-1})_M^A(Y) (U^{-1})_N^B(Y)$$

# Exceptional Field Theory and consistent truncations

Consistent truncations captured by  
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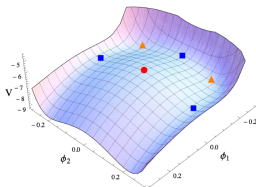
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# Uplifting to string theory

Consistent truncations on  $S^p$ ,  $H^{p,q}$ ,  $S^p \times S^q$ , ...

[Aldazabal, Berman, Geissbühler, Cassani, Graña, Hohm, Inverso, Lee, EM, Marqués, Petrini, Samtleben, Strickland-Constable, Thompson, Trigiante, Waldram, ...]

$$\mathcal{M}_{MN}(x, Y) = M_{AB}(x)(U^{-1})_M^A(Y)(U^{-1})_N^B(Y)$$

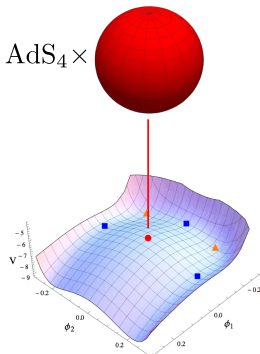


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$$\mathcal{M}_{MN}(x, Y) = \delta_{AB}(U^{-1})_M^A(Y)(U^{-1})_N^B(Y)$$



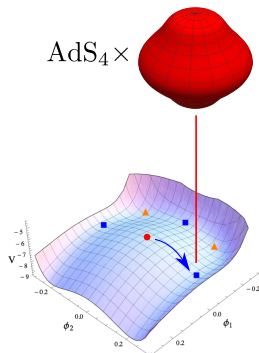


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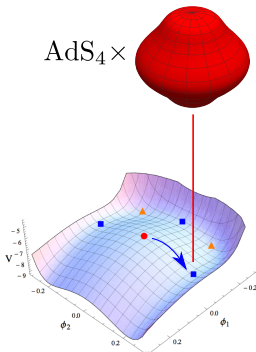


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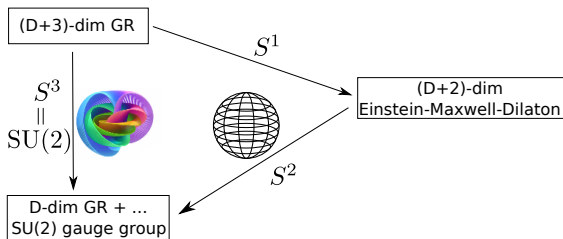
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$$\mathcal{M}_{MN}(x, Y) = M_{AB}(x)(U^{-1})_M^A(Y)(U^{-1})_N^B(Y)$$



Multiplication by  $E_{7(7)}$  matrix!

## Higher-dimensional space?



Is there a similar higher-dimensional space underlying ExFT? General  $\partial_M$ ?

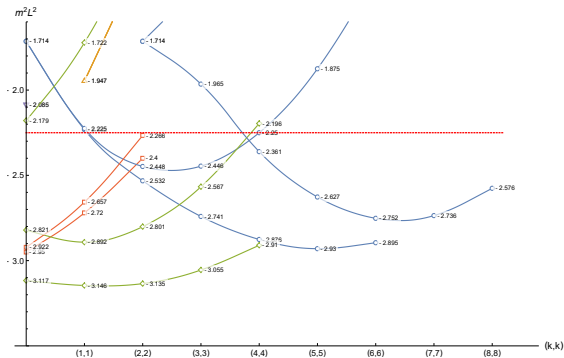
No!

Section condition:

$$\mathbb{P}_{MN}{}^{PQ} \partial_P \otimes \partial_Q = 0$$

Covariant restriction to 7 (11-d SUGRA) or 6 (IIB SUGRA) coordinates.

# Kaluza-Klein spectroscopy



# Kaluza-Klein spectroscopy

Consistent truncation:

- ▶ Lower-dimensional theory
- ▶ Compute subset of masses for any vacuum!

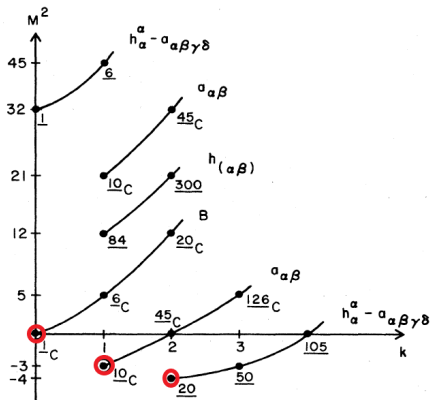
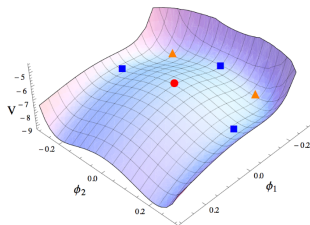


FIG. 2. Mass spectrum of scalars.



# Kaluza-Klein spectroscopy

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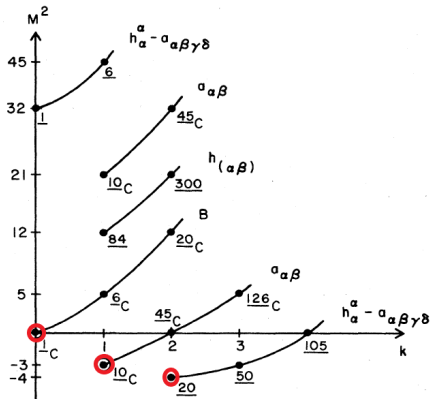
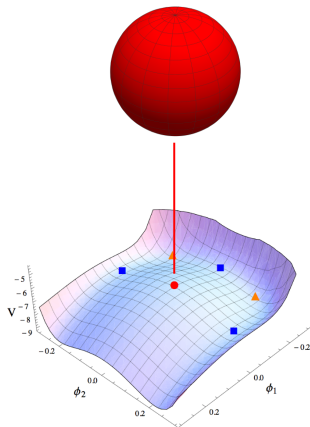


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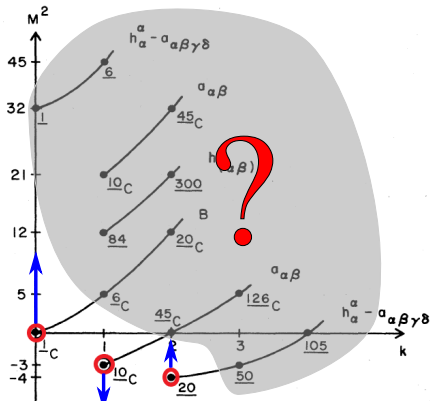
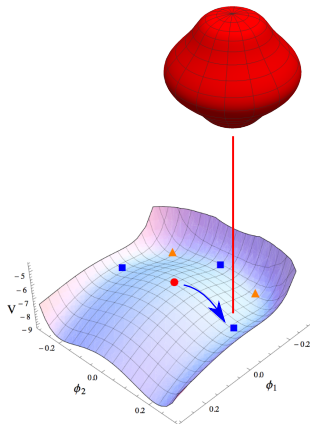


FIG. 2. Mass spectrum of scalars.



# Kaluza-Klein spectroscopy

Consistent

[EM, Samtleben PRL '20]

Extend this to full KK spectrum using ExFT!

- ▶ Low
- ▶ Com

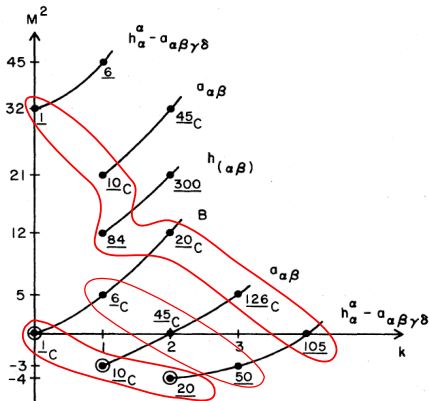
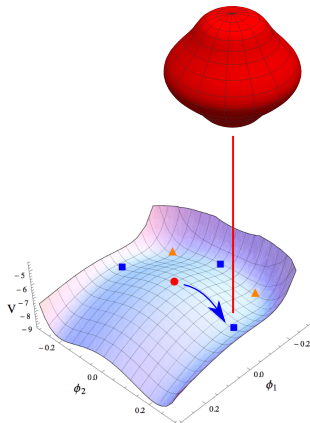


FIG. 2. Mass spectrum of scalars.





# Traditional Kaluza-Klein spectroscopy

Traditionally:

- ▶ Spin-2 fields [Bachas, Estes '11] ✓
- ▶  $M_{int} = \frac{G}{H}$  ✓

Here: [EM, Samtleben PRL '20]

- ▶ Compactifications with few or no remaining (super-)symmetries!

## Kaluza-Klein spectrum on $\text{AdS}_D \times M_{compact}$

Free scalar on  $S^1$ :

$$0 = \partial_x^2 \phi(x, y) + \partial_y^2 \phi(x, y),$$
$$\phi(x, y) = \phi^{(\ell)}(x) e^{i\ell y/R}, \quad m^2 = \frac{\ell^2}{R^2}.$$

# Kaluza-Klein spectrum on $\text{AdS}_D \times M_{compact}$

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E.g. IIB supergravity around  $\text{AdS}_5 \times S^5$ :

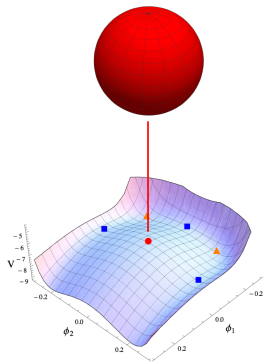
- ▶ Expand  $h_{\mu\nu}$ ,  $\Phi$ ,  $\chi$ ,  $B_{\mu\nu}$ ,  $A_{\mu\nu}$ ,  $A_{\mu\nu\rho\sigma}$ , ... in  $S^5$  tensor harmonics
- ▶ Complicated mass diagonalisation, e.g.

$$\Delta_L h_{\mu\nu} = \frac{1}{3} F_{(\mu}{}^{\rho\sigma\kappa\lambda} f_{\nu)\rho\sigma\kappa\lambda} - \frac{1}{18} g_{\mu\nu} F_{\rho\sigma\kappa\lambda\tau} f^{\rho\sigma\kappa\lambda\tau} - F_{(\mu}{}^{\rho\sigma\kappa\tau} F_{\nu)}{}^{\delta\sigma\kappa\tau} h_{\rho\delta}$$
$$- \frac{1}{36} h_{\mu\nu} F_{\rho\sigma\kappa\lambda\tau} F^{\rho\sigma\kappa\lambda\tau} + \frac{1}{9} g_{\mu\nu} F_{\rho\sigma\kappa\lambda\epsilon} F_{\tau}{}^{\sigma\kappa\lambda\epsilon} h^{\rho\tau},$$

## KK spectroscopy strategy

First at max symmetric point:

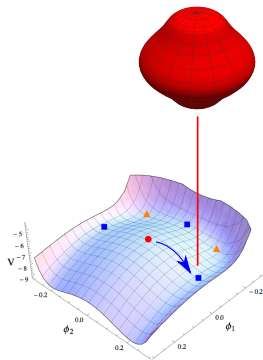
$$\mathcal{M}_{MN}(x, Y) = \delta_{AB}(U^{-1})_M^A(Y)(U^{-1})_N^B(Y)$$



## KK spectroscopy strategy

Then at less symmetric point:

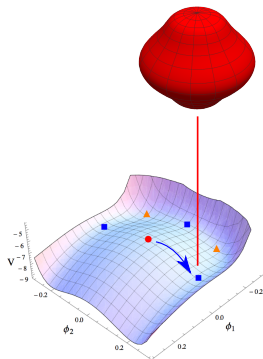
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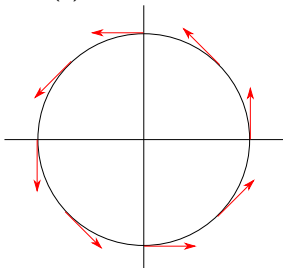
$$\mathcal{M}_{MN}(x, Y) = M_{AB}(x)(U^{-1})_M^A(Y)(U^{-1})_N^B(Y)$$



Multiplication by  $E_{7(7)}$  matrix,  $M_{AB}(x)$ !

## KK spectroscopy at max. symmetric point

$U_A^M \in E_{7(7)}$  give basis for all fields

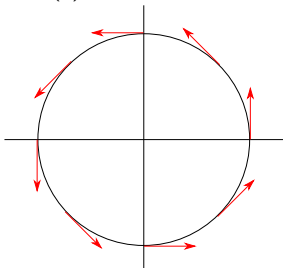


Only need scalar harmonics:  $\mathcal{Y}_\Sigma$

$$\text{c.f. } h_{ij}(x, y) = \sum_\ell h^{(\ell)}(x) \mathcal{Y}_{(ij)}^{(\ell)}(y), \quad b_{ij}(x, y) = \sum_\ell b^{(\ell)}(x) \mathcal{Y}_{[ij]}^{(\ell)}(y)$$

## KK spectroscopy at max. symmetric point

$U_A^M \in E_{7(7)}$  give basis for all fields



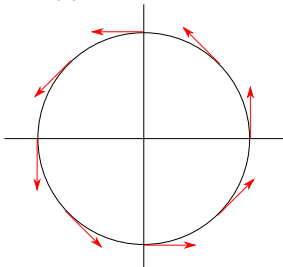
Only need scalar harmonics:  $\mathcal{Y}_\Sigma$

$$\mathcal{M}_{MN}(x, Y) \in E_{7(7)}/\text{SU}(8)$$



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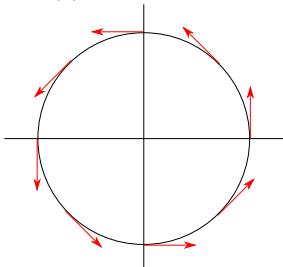
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$$j_{AB}^\Sigma \in \mathfrak{e}_{7(7)} \ominus \mathfrak{su}(8)$$

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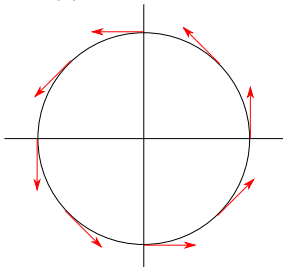
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KK Ansatz = consistent truncation  $\otimes$  scalar harmonics

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$$\mathcal{M}_{MN}(x, Y) = (\delta_{AB} + j_{AB}{}^\Sigma(x) \mathcal{Y}_\Sigma) (U^{-1})_M^A(Y) (U^{-1})_N^B(Y)$$

$$j_{AB}{}^\Sigma \in \mathfrak{e}_{7(7)} \ominus \mathfrak{su}(8)$$

Immediate mass diagonalisation!

## Mass matrix

- ▶ Lower-dim info:

$$\mathcal{L}_{U_A} U_B = X_{AB}{}^C U_C,$$

- ▶ Higher-dim info:

$$\mathcal{L}_{U_A} \mathcal{Y}_\Sigma = L_{KA} \mathcal{Y}_\Sigma = \mathcal{T}_{A\Sigma}{}^\Omega \mathcal{Y}_\Omega.$$

Mass matrix:

$$\mathbb{M}_{I\Sigma, J\Omega}^{(\text{scalar})} = \mathbb{M}_{IJ}^{(0)} \delta_{\Sigma\Omega} + \delta_{IJ} \mathbb{M}_{\Sigma\Omega}^{(\text{spin-2})} + \mathcal{N}_{IJ}{}^C \mathcal{T}_{C, \Omega\Sigma}$$

## Mass matrix

- ▶ Lower-dim info:

$$\mathcal{L}_{U_A} U_B = X_{AB}{}^C U_C,$$

- ▶ Higher-dim info:

$$\mathcal{L}_{U_A} \mathcal{Y}_\Sigma = L_{K_A} \mathcal{Y}_\Sigma = \mathcal{T}_{A\Sigma}{}^\Omega \mathcal{Y}_\Omega.$$

Mass matrix:

$$\mathbb{M}_{I\Sigma, J\Omega}^{(\text{scalar})} = \mathbb{M}_{IJ}^{(0)} \delta_{\Sigma\Omega} + \delta_{IJ} \mathbb{M}_{\Sigma\Omega}^{(\text{spin}-2)} + \mathcal{N}_{IJ}{}^C \mathcal{T}_{C, \Omega\Sigma}$$

- ▶ Lower-dim SUGRA mass matrix  $\mathbb{M}_{IJ}^{(0)}$

## Mass matrix

- ▶ Lower-dim info:

$$\mathcal{L}_{U_A} U_B = X_{AB}{}^C U_C,$$

- ▶ Higher-dim info:

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- ▶ Lower-dim SUGRA mass matrix  $\mathbb{M}_{IJ}^{(0)}$

$$\begin{aligned} \mathbb{M}_{IJ}^{(0)} &= \frac{1}{7} \left( X_{AE}{}^F X_{BE}{}^F + X_{EA}{}^F X_{EB}{}^F + X_{EF}{}^A X_{EF}{}^B + 7 X_{AE}{}^F X_{BF}{}^E \right) \mathcal{P}_{AD}{}^I \mathcal{P}_{BD}{}^J \\ &+ \frac{2}{7} \left( X_{AC}{}^E X_{BD}{}^E - X_{AE}{}^C X_{BE}{}^D - X_{EA}{}^C X_{EB}{}^D \right) \mathcal{P}_{AB}{}^I \mathcal{P}_{CD}{}^J \\ &+ \frac{1}{6} \mathcal{P}_{AB}{}^I \mathcal{P}_{CD}{}^J X_{FA}{}^B X_{FC}{}^D. \end{aligned}$$

## Mass matrix

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- ▶ Higher-dim info:

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- ▶ Spin-2 mass matrix  $\mathbb{M}_{\Sigma\Omega}^{(\text{spin-2})} = \mathcal{T}_{A, \Sigma\Lambda} \mathcal{T}_{A, \Lambda\Omega}$

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Mass matrix:

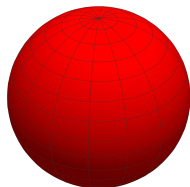
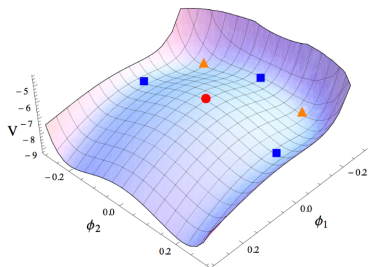
$$\mathbb{M}_{I\Sigma, J\Omega}^{(\text{scalar})} = \mathbb{M}_{IJ}^{(0)} \delta_{\Sigma\Omega} + \delta_{IJ} \mathbb{M}_{\Sigma\Omega}^{(\text{spin-2})} + \mathcal{N}_{IJ}{}^C \mathcal{T}_{C, \Omega\Sigma}$$

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- ▶ Spin-2 mass matrix  $\mathbb{M}_{\Sigma\Omega}^{(\text{spin-2})} = \mathcal{T}_{A, \Sigma\Lambda} \mathcal{T}_{A, \Lambda\Omega}$
- ▶ Key object:

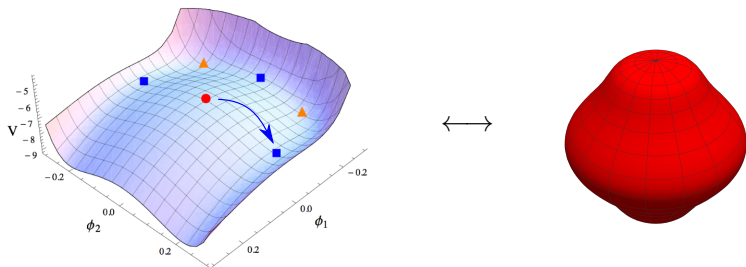
$$\mathcal{N}_{IJ}{}^C = -4(X_{CA}{}^B + 12 X_{AB}{}^C) \mathcal{P}^{AD} {}_{[I} \mathcal{P}^{BD} {}_{J]}.$$



## KK spectroscopy at less symmetric point



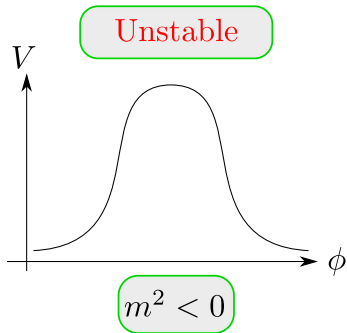
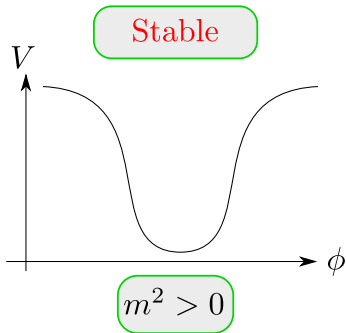
## KK spectroscopy at less symmetric point



Multiplication by  $E_{7(7)}$  matrix,  $M_{AB}(x)$ !

Use same harmonics as for max. symmetric point

## Stability of non-SUSY AdS<sub>4</sub> vacua



# Zero-mode vs higher-dimensional stability

Most non-SUSY vacua already unstable in lower-dim theory

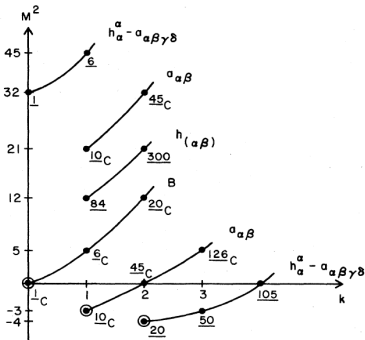
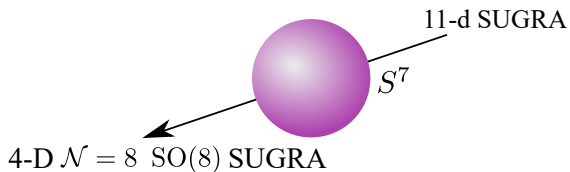


FIG. 2. Mass spectrum of scalars.

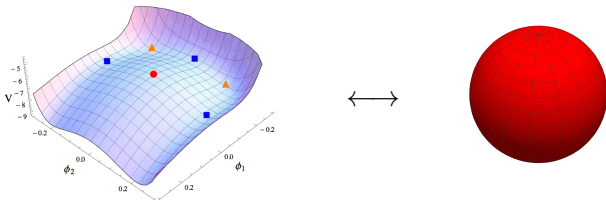
Is “zero-mode” stability enough?

# Non-SUSY $SO(3) \times SO(3)$ $AdS_4$ vacua



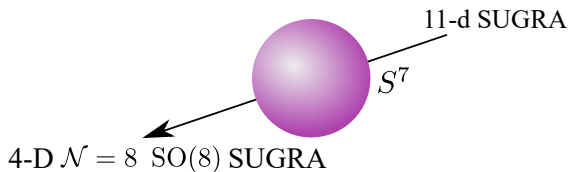
[de Wit, Nicolai '82], [Hohm, Samtleben '14], [Lee, Strickland-Constable, Waldram '14]  
[Godazgar, Godazgar, Kruger, Nicolai, Pilch '14]

- ▶ Non-SUSY  $SO(3) \times SO(3)$   $AdS_4$  vacuum [Warner '83]



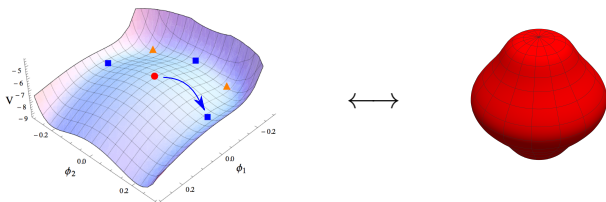
- ▶ Only non-SUSY vacuum that is stable in 4-d! [Fischbacher, Pilch, Warner '10], [Comsa, Firsching, Fischbacher '19]

# Non-SUSY $SO(3) \times SO(3)$ $AdS_4$ vacua



[de Wit, Nicolai '82], [Hohm, Samtleben '14], [Lee, Strickland-Constable, Waldram '14]  
[Godazgar, Godazgar, Kruger, Nicolai, Pilch '14]

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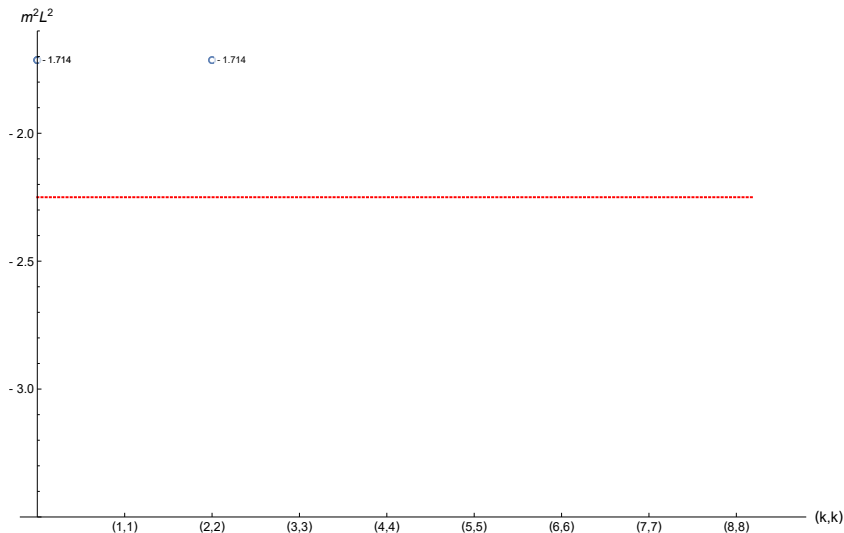


- ▶ Only non-SUSY vacuum that is stable in 4-d! [Fischbacher, Pilch, Warner '10], [Comsa, Firsching, Fischbacher '19]

# Tachyonic KK modes

Modes  $\ell = 0$ :  $\mathcal{N} = 8$  supergravity multiplet

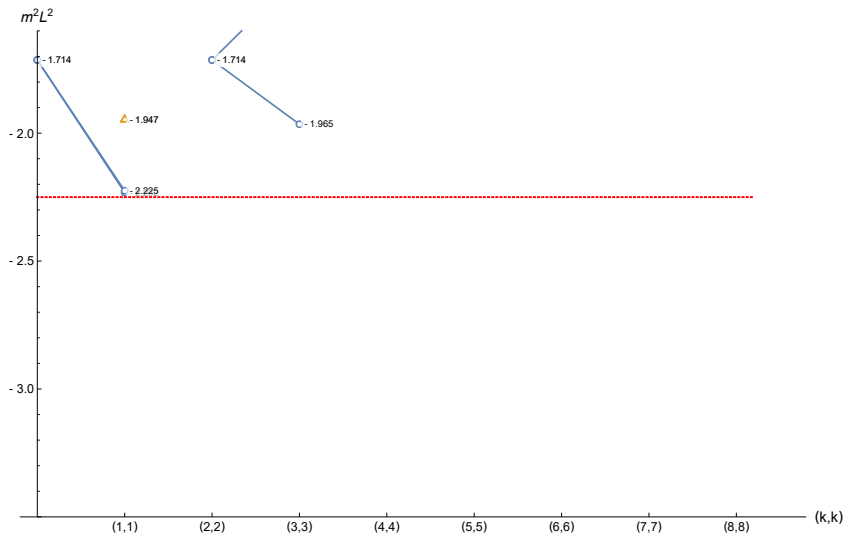
[Fischbacher, Pilch, Warner '10]



# Tachyonic KK modes

Modes  $\ell \leq 1$ : still stable!

[EM, Nicolai, Samtleben JHEP '20]

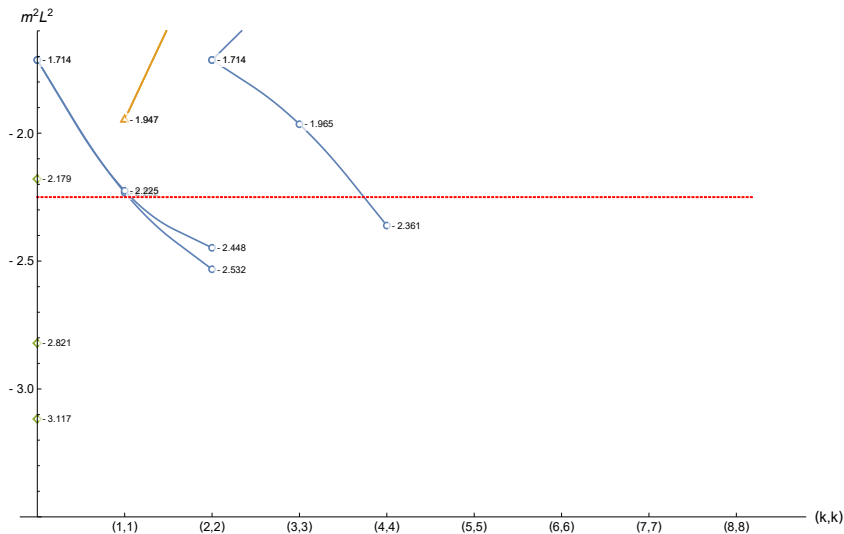




# Tachyonic KK modes

Modes  $\ell \leq 2$ : **tachyons!**

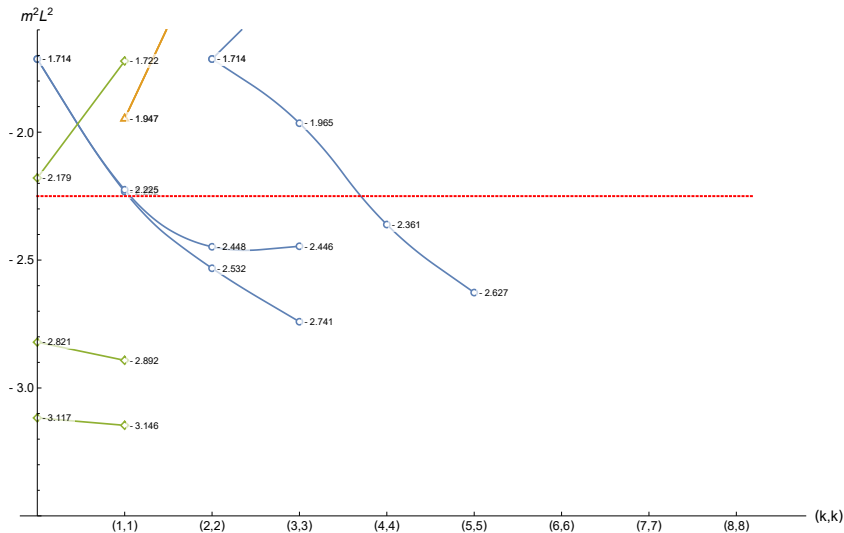
[EM, Nicolai, Samtleben JHEP '20]



# Tachyonic KK modes

Modes  $\ell \leq 3$

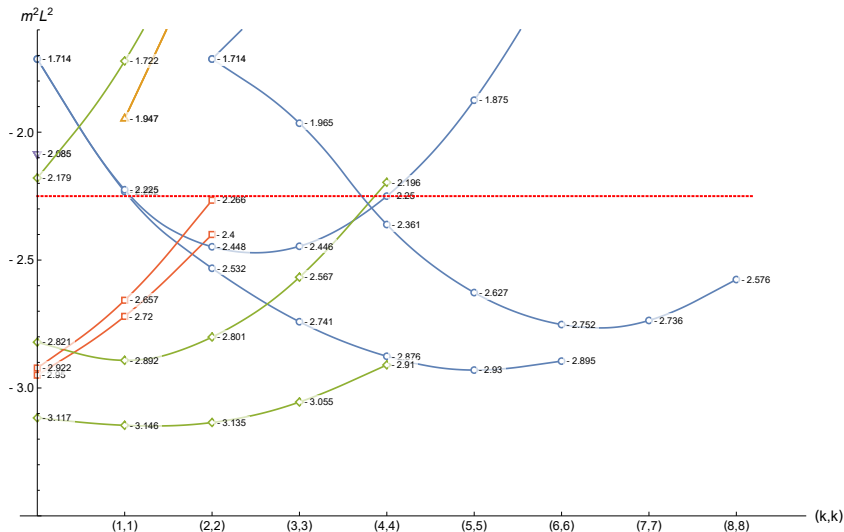
[EM, Nicolai, Samtleben JHEP '20]



# Tachyonic KK modes

Modes  $\ell \leq 6$

[EM, Nicolai, Samtleben JHEP '20]



## A false hope

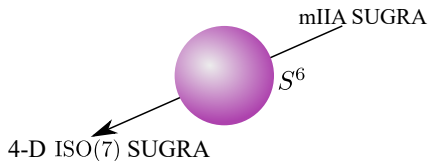
- ▶  $SO(3) \times SO(3)$  AdS<sub>4</sub> [Warner '83] is unstable
- ▶ Instability from higher KK modes [EM, Nicolai, Samtleben JHEP '20]

“Zero-mode” stability does not guarantee perturbative stability in higher dimensions

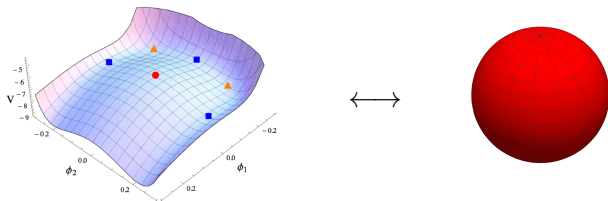
- ▶ Also “brane-jet instability” [Bena, Pilch, Warner '20]

# Zero-mode stability in ISO(7) SUGRA

- ▶ [Guarino, Jafferis, Varela '15]



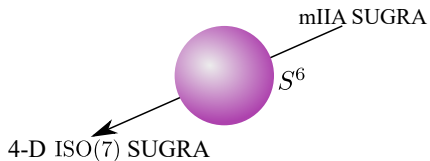
- ▶ 7 stable non-SUSY AdS<sub>4</sub> vacua



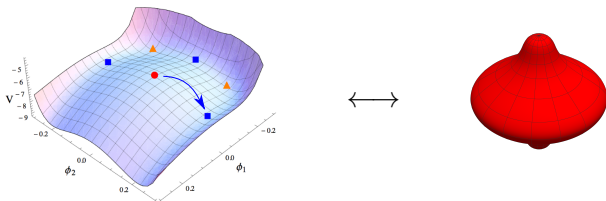
- ▶  $G_2$  invariant + 6 less symmetric non-SUSY AdS<sub>4</sub>, stable in 4-D

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- ▶  $G_2$  invariant + 6 less symmetric non-SUSY AdS<sub>4</sub>, stable in 4-D

## Stability of $G_2$ vacuum in mIIA

- ▶ Analytic spectrum:

$$L^2\mathbb{M}_{(\text{scalar})}^2 = (\ell + 2)(\ell + 3) - \frac{3}{2}\mathcal{C}_{G_2} \geq 0.$$

$\ell$ :  $S^6$  KK level

$\mathcal{C}_{G_2}$ :  $G_2$  Casimir

$G_2$  vacuum is perturbatively stable in mIIA SUGRA

[Guarino, EM, Samtleben PRL '21]

- ▶ No signs of Ooguri-Vafa instability [Guarino, Tarrío, Varela '20]
- ▶ Protected against “bubble of nothing”
- ▶ May suffer from different non-perturbative instabilities [Bomans, Cassani, Dibitetto, Petri '21]

## Stability of six other AdS<sub>4</sub> vacua in mIIA

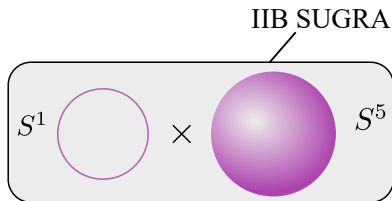
Evidence for perturbative stability in mIIA SUGRA  
[Guarino, EM, Samtleben PRL '21]

- ▶ Numerical evaluation up to level  $\ell = 4$ :
  - ▶ no tachyons
  - ▶ lowest-lying masses increase monotonically with level
- ▶ No signs of Ooguri-Vafa instability [Guarino, Tarrío, Varela '20]
- ▶ Protected against “bubble of nothing”



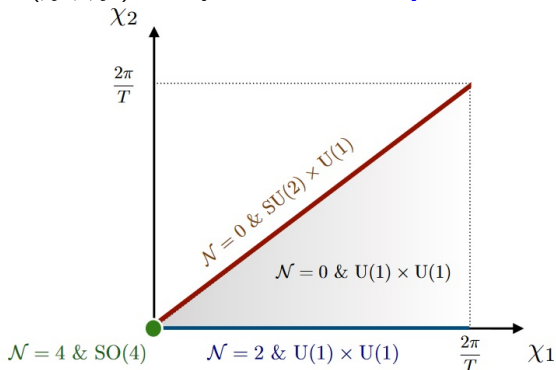
# Non-SUSY flat deformations

- ▶ [Inverso, Samtleben, Trigiante '16]



4-D  $[SO(6) \times SO(1, 1)] \ltimes \mathbb{R}^{12}$  SUGRA

- ▶ 2-parameter  $(\chi_1, \chi_2)$  family of  $AdS_4$  vacua [Guarino, Sterckx '21]



## IIB S-fold geometry

$\text{AdS}_4 \times S^5 \times S^1$  S-fold vacua of IIB String Theory

$\text{SL}(2, \mathbb{Z})_{\text{IIB}}$  monodromy along  $S^1$

[Hull, Catal-Özer '03]

$$\mathcal{J}_k = \begin{pmatrix} k & -1 \\ 1 & 0 \end{pmatrix} \in \text{SL}(2, \mathbb{Z})$$

Reduce on  $S^5$ ,  $\chi_{1,2} \longleftrightarrow$  Wilson lines of KK vector

$\chi_{1,2}$  locally coordinate redefinition, but not globally

c.f.  $\mathbb{C}$ -structure moduli of  $T^2$

## Non-SUSY conformal manifold?

Non-SUSY exactly marginal deformations not expected to exist

Evidence for a miracle

[Giambrone, Guarino, EM, Samtleben, Sterckx, Trigiante 2112.11966]

- ▶ Perturbative stability
- ▶ Non-perturbative stability
- ▶ Perturbative quantum corrections

$\chi_1, \chi_2$  deformations are locally coordinate transformations!

# KK Spectroscopy

[Giambrone, Guarino, EM, Samtleben, Sterckx, Trigiante 2112.11966]

KK spectroscopy  $\rightarrow$  full KK spectrum  
Perturbatively stable!

At  $\chi_{1,2} = 0$ ,  $\mathcal{N} = 4$  point

$$\mathbb{M}_{(\text{spin}-2)}^2 L^2 = \frac{1}{2} \ell(\ell + 4) + l_1(l_1 + 1) + l_2(l_2 + 1) + \frac{1}{2} \left( \frac{2n\pi}{T} \right)^2$$

SO(4) spin:  $l_1, l_2$ ,

$S^5$  level:  $l$

$S^1$  level:  $n$

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SO(4) spin:  $l_1, l_2$ ,

$S^5$  level:  $l$

$S^1$  level:  $n$

$$\frac{2n\pi}{T} \longrightarrow \frac{2n\pi}{T} + j_1 \chi_1 + j_2 \chi_2$$

$j_{1,2}$  charges under  $U(1) \times U(1)$  Cartan

Space invaders:  $\chi_{1,2} \rightarrow \chi_{1,2} + \frac{4\pi}{T}$ ,  $n \rightarrow n - 2j_{1,2}$

## Non-perturbative stability?

[Giambrone, Guarino, EM, Samtleben, Sterckx, Trigiante 2112.11966]

- ▶ Probe-brane analysis:  $T > Q$   
Branes more stable than in SUSY case!
- ▶ No Ooguri-Vafa instability [Ooguri, Vafa '16]
- ▶  $S^1$  and  $S^5$  protected against “bubble of nothing” [Witten '82]
- ▶ D3-brane bubble of nothing [Bomans, Cassani, Dibitetto, Petri '21] ??

## Beyond “large- $N$ ” limit

[Giambrone, Guarino, EM, Samtleben, Sterckx, Trigiante 2112.11966]

Moduli  $\chi_{1,2}$  not lifted by perturbative quantum ( $\alpha'$ ,  $g_s$ ) corrections

Protection by diffeomorphism symmetry

- ▶  $\chi_1, \chi_2 \rightarrow$  coordinate transformations (locally)
- ▶  $\chi_1, \chi_2$  do not appear in diffeo-invariant quantities

Also applies to  $\mathcal{N} = 1$  exactly marginal deformations

[Bobev, Gautason, van Muiden '21]

## Non-perturbative corrections?

Flat directions lifted by non-perturbative corrections?

- ▶ 5-brane instantons on  $S^5 \times S^1$
- ▶ Classical instanton action  $e^{-vol_{S^5 \times S^1}}$  invariant under  $\chi_1, \chi_2$
- ▶ Instanton amplitude sensitive to  $\chi_{1,2}$ ?



# Applications to SUSY AdS

AdS KK spectrum  $\iff$  anomalous dimensions of CFT operators

- ▶  $U(3) \mathcal{N} = 2$  AdS<sub>4</sub> vacuum [Corrado, Pilch, Warner '02]  
⇒ Full spectrum [EM, Samtleben '20]
- ▶  $U(2) \mathcal{N} = 2$  AdS<sub>5</sub> vacuum [Pilch, Warner '00]  
⇒ Full spectrum & check with LS SCFT [Bobev, EM, Robinson, Samtleben, van Muiden '20]
- ▶ AdS<sub>5</sub> S-folds [Inverso, Samtleben, Trigiante '16], [Guarino, Sterckx, Trigiante '20]  
⇒ Full spectrum & compactness of conformal manifold [Giambrone, EM, Samtleben, Trigiante '21]

## Conclusions

ExFT: powerful tool to construct non-SUSY AdS vacua & determine perturbative stability

- ▶ Perturbative non-SUSY AdS vacua with possible protection against non-perturbative instability
- ▶ (SUSY) AdS vacua: KK spectrum  $\Leftrightarrow$  Anomalous dimensions

### Open questions

- ▶ Vacua of less SUSY gSUGRA?
- ▶  $\Lambda \geq 0$ ?
- ▶ Non-perturbative stability? Positive Mass Theorem? [Dibitetto '21]
- ▶ Non-perturbative correction?

Thank you!