

Primordial High Energy Neutrinos

Theoretical & observational constraints and sharp
spectral features

Nicolas Grimbaum Yamamoto

arXiv:[2507.02063](https://arxiv.org/abs/2507.02063) in collaboration with T.Hambye

Summary •

1

Motivations

2

Sharp spectral features

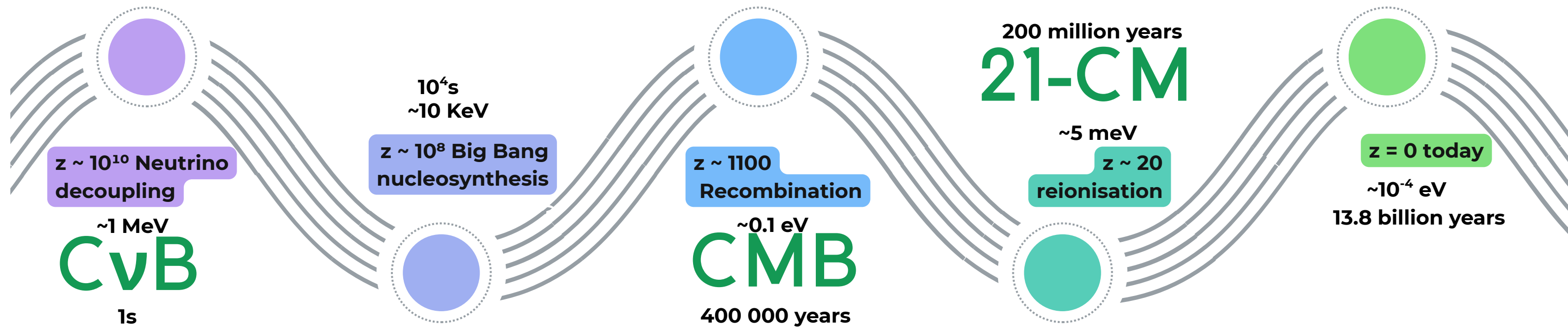
3

Medium interactions

4

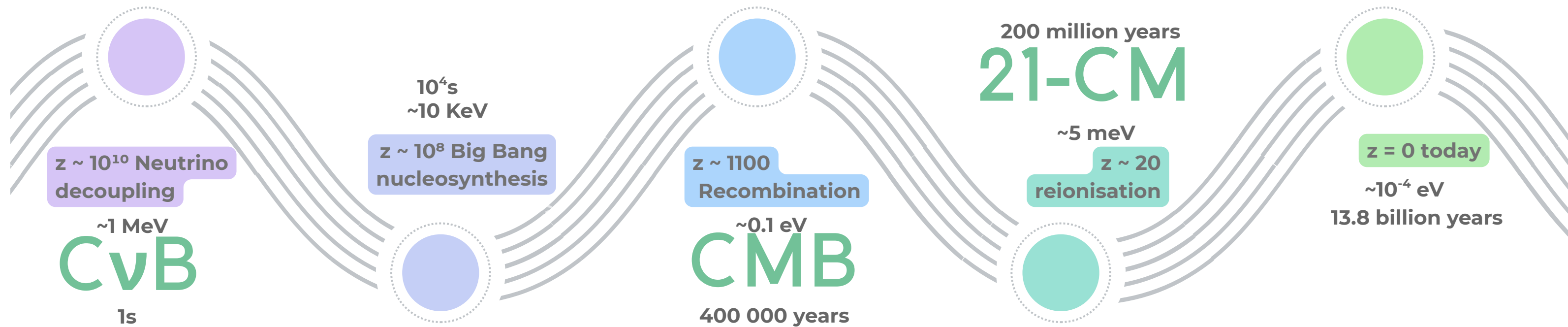
Constraints

Motivations.



→ Primordial High
Energy Neutrinos
(PHENUs)

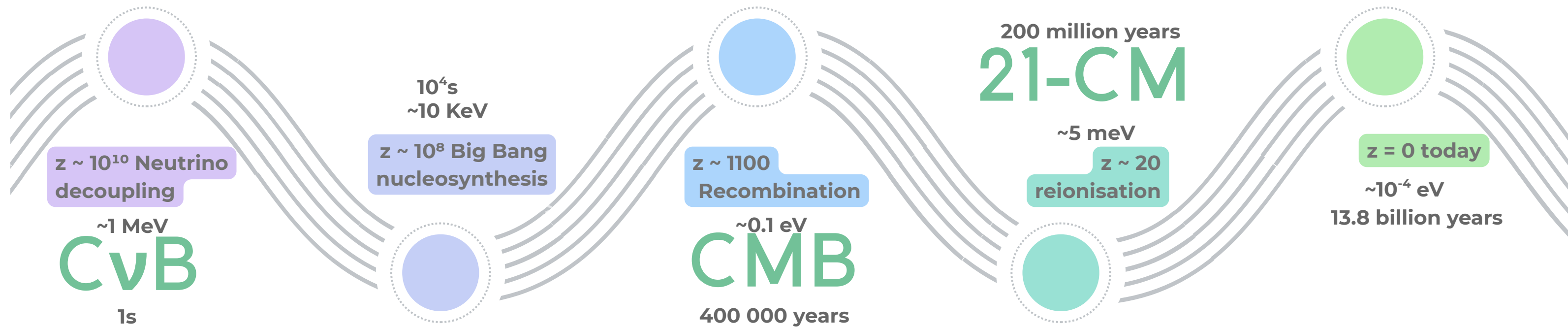
Motivations.



→ **Primordial High Energy Neutrinos (PHENUs)**



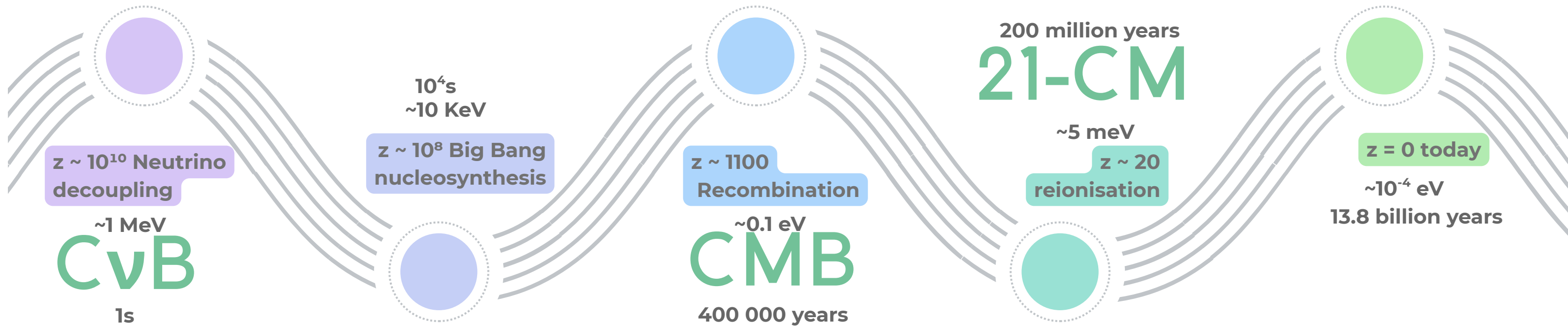
Motivations.



→ Primordial High Energy Mewtrinos (PHEMEW) !



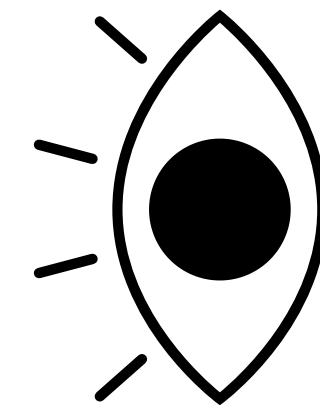
Motivations.



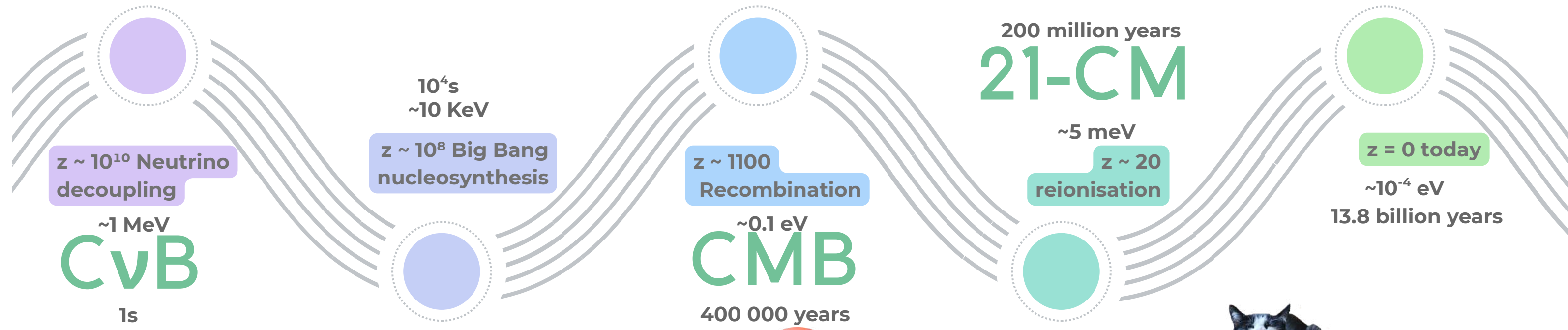
→ Primordial High Energy Mewtrinos (PHEMEW) !



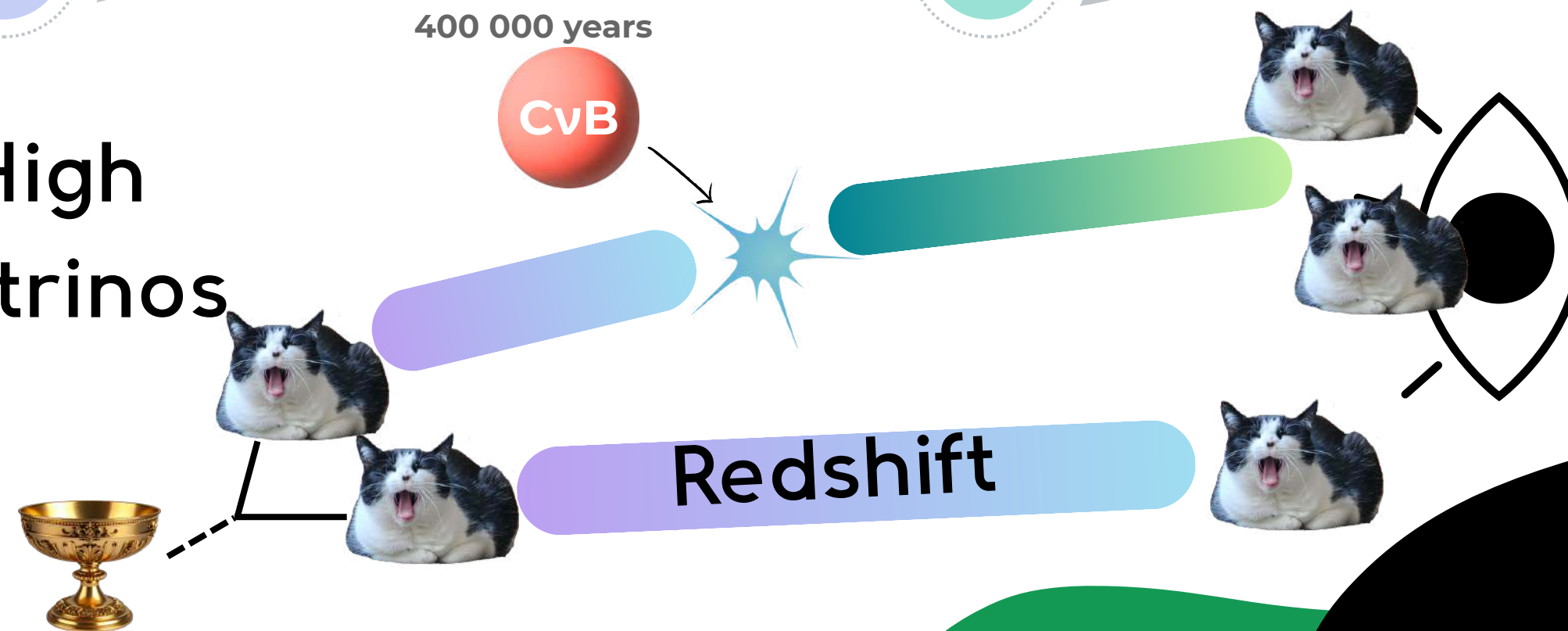
Redshift



Motivations.



→ Primordial High Energy Mewtrinos (PHEMEW) !



Motivations.

Few works on this topic:

- Frampton, Glashow, '80
- Gelmini, Gondolo, Sarkar '92
- Kanzaki, Kawasaki, Kohri, Moroi '07
- Ema, Jinno, Moroi '13, '14
- McKeen '18
- ...

UNSTABLE HEAVY PARTICLES*

P. H. Frampton and S. L. Glashow

Lyman Laboratory of Physics
Harvard University
Cambridge, MA 02138

ABSTRACT

It is pointed out that for very massive particles in our universe there exist stringent bounds on their possible properties. New experiments which will search primarily for proton decay can usefully extend the domain of these bounds.

Motivations.

Few works on this topic:

- Frampton, Glashow, '80
- Gelmini, Gondolo, Sarkar '92
- Kanzaki, Kawasaki, Kohri, Moroi '07
- Ema, Jinno, Moroi '13, '14
- McKeen '18
- ...

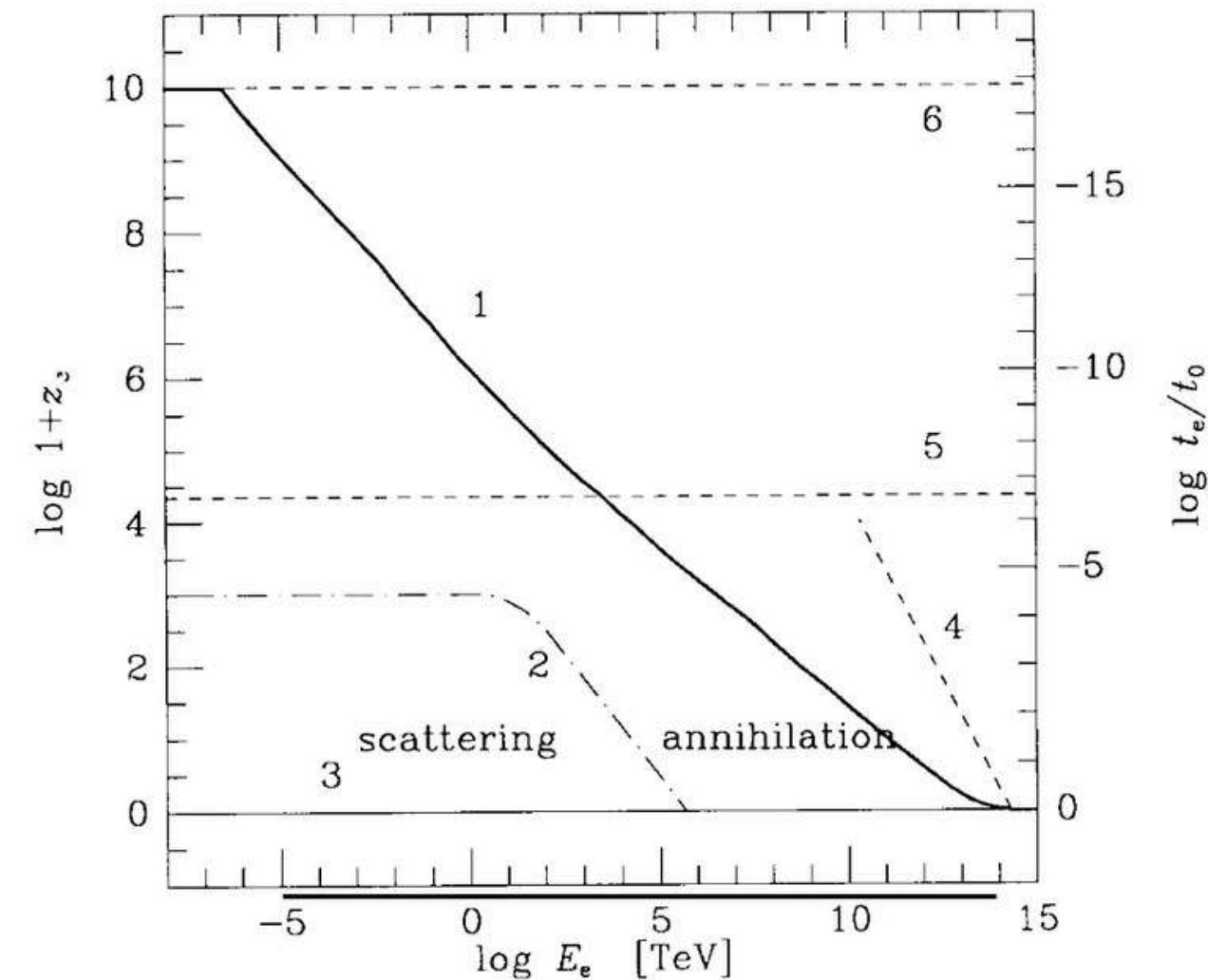


Fig. 1. The absorption redshift z_a (line 1) for cosmic neutrinos as a function of the neutrino energy at emission E_e taking $\Omega_0 h^2 = 1$. The other lines indicate: (2) the boundary between the two regions where absorption due to annihilation and scattering dominate; (3) the present epoch; (4) the Z-boson pole; (5) the epoch of matter-radiation equality; (6) the epoch of light-neutrino decoupling.

Motivations.

Few works on this topic:

- Frampton, Glashow, '80
- Gelmini, Gondolo, Sarkar '92
- Kanzaki, Kawasaki, Kohri, Moroi '07
- Ema, Jinno, Moroi '13, '14
- McKeen '18
- ...

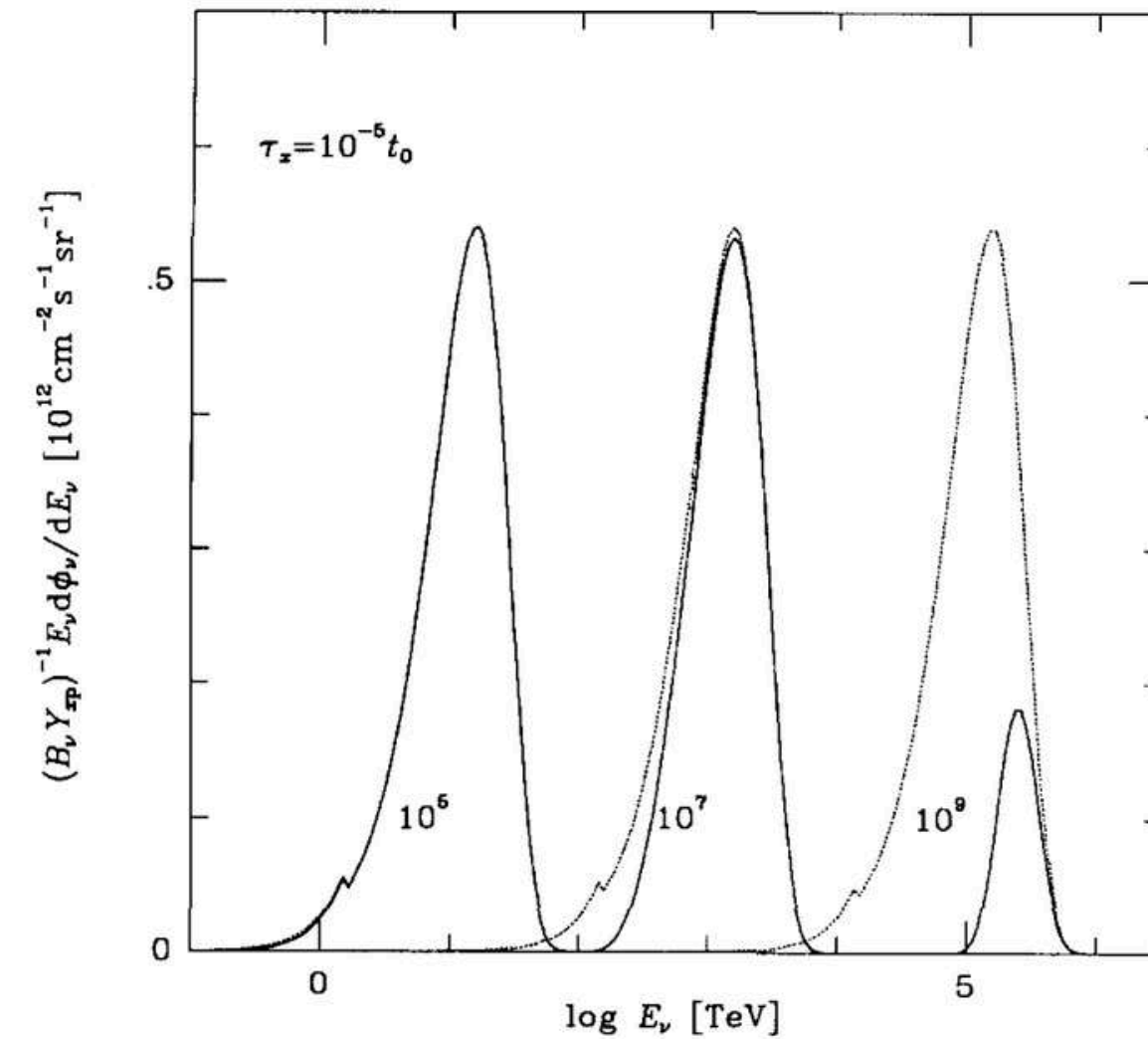
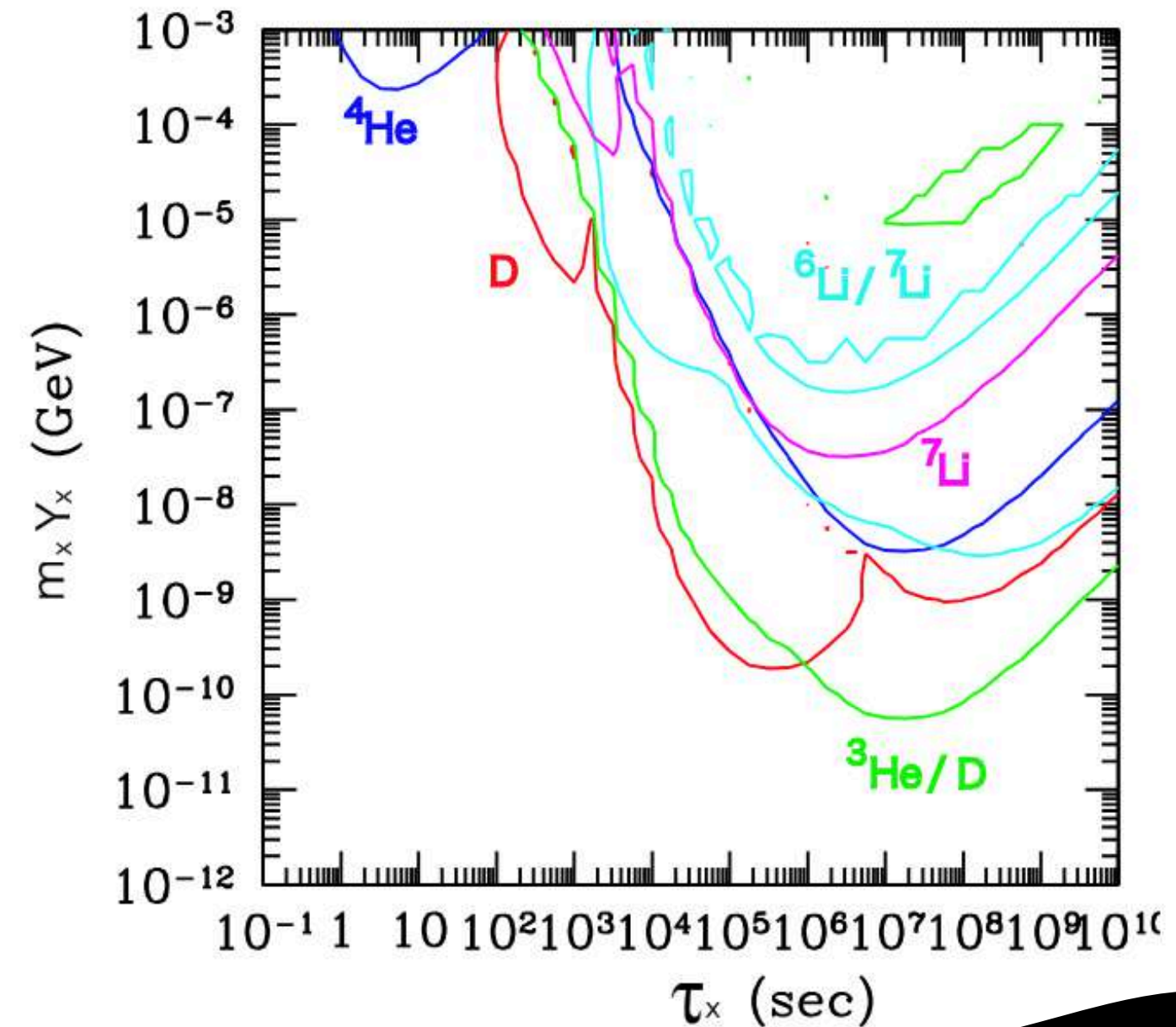


Fig. 2. The present energy spectrum of decay generated neutrinos for $\tau_x = 10^{-5} t_0$ and $3E_e = 10^5$ TeV, 10^7 TeV and 10^9 TeV. The full lines show the effect of cosmological neutrino absorption.

Motivations.

Few works on this topic:

- Frampton, Glashow, '80
- Gelmini, Gondolo, Sarkar '92
- Kanzaki, Kawasaki, Kohri, Moroi '07
- Ema, Jinno, Moroi '13, '14
- McKeen '18
- ...



Motivations.

Few works on this topic:

- Frampton, Glashow, '80
- Gelmini, Gondolo, Sarkar '92
- Kanzaki, Kawasaki, Kohri, Moroi '07
- Ema, Jinno, Moroi '13, '14
- McKeen '18
- ...

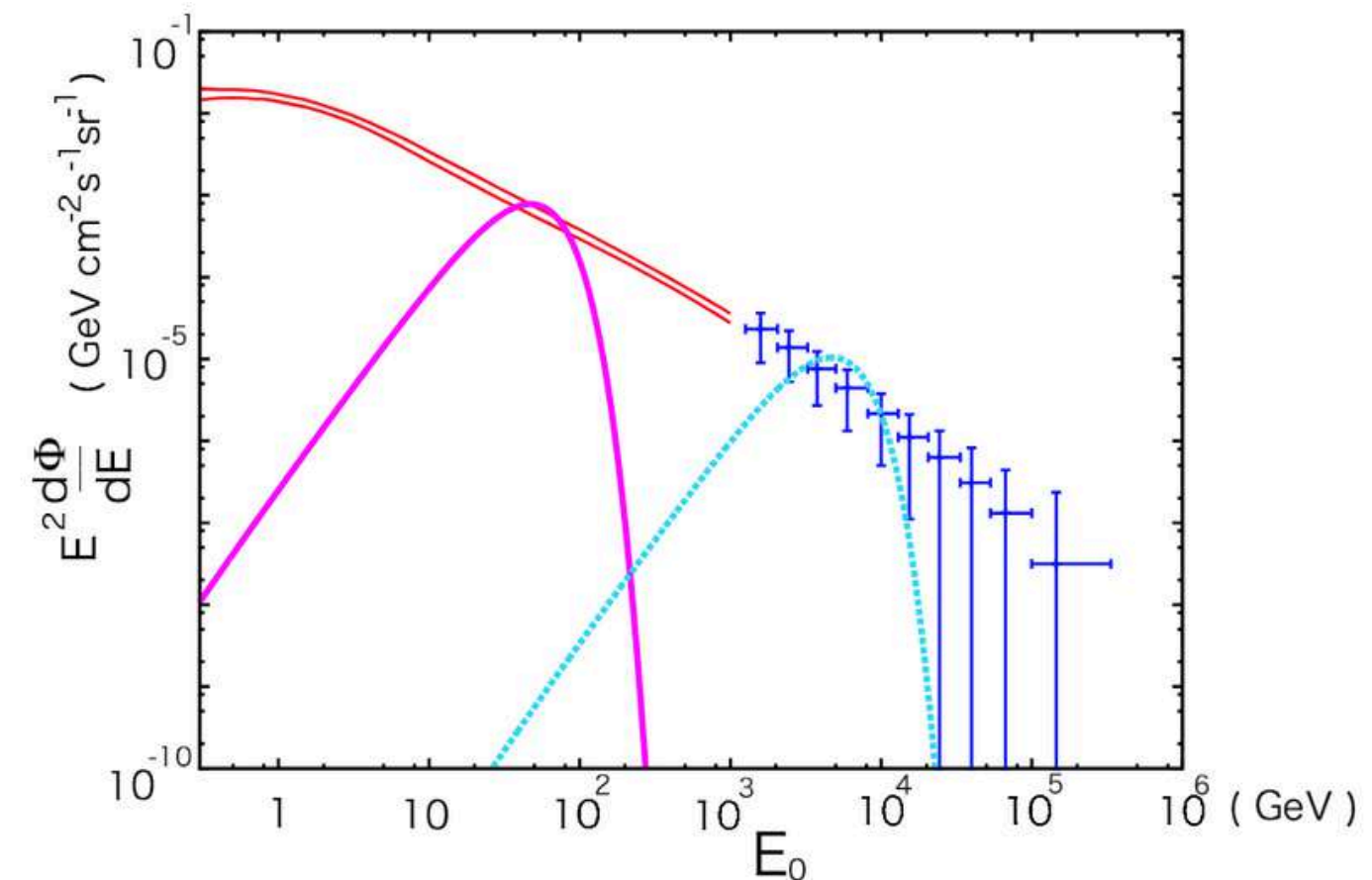


Figure 16. Atmospheric neutrino flux. Thin solid lines represent 1σ range of the atmospheric neutrino fluxes [42]. The point data are from AMANDA. Thick solid and dotted lines represent diffuse neutrino signal with $m_X = 10^3 \text{ GeV}$ and $Y_X = 2.53 \times 10^{-17}$ (thick solid line) and 10^5 GeV and $Y_X = 3.37 \times 10^{-21}$ (thick dotted line). The lifetime is $\tau_X = 10^{16} \text{ sec}$.

Motivations.

Few works on this topic:

- Frampton, Glashow, '80
- Gelmini, Gondolo, Sarkar '92
- Kanzaki, Kawasaki, Kohri, Moroi '07
- Ema, Jinno, Moroi '13, '14
- McKeen '18
- ...

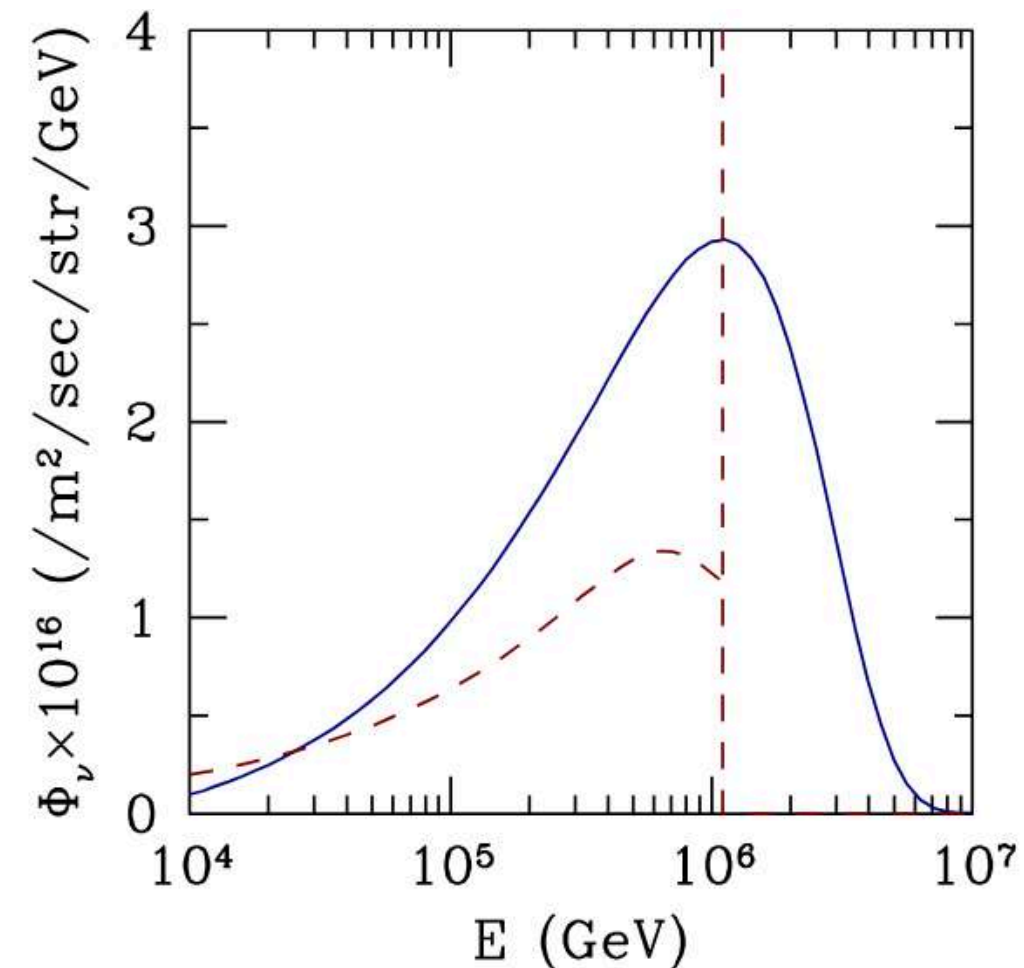


Figure 3: The total present cosmic-ray neutrino flux from the long-lived particle X , normalized by $10^{-16} \text{ m}^{-2} \text{ sec}^{-1} \text{ str}^{-1} \text{ GeV}^{-1}$. Here, we take $(\tau_X, \bar{E}_\nu, Y_X) = (5.2 \times 10^{14} \text{ sec}, 2.2 \times 10^2 \text{ PeV}, 1.2 \times 10^{-26})$ (blue-solid, corresponding to $1 + z_* = 100$), and $(10^{29} \text{ sec}, 1.1 \text{ PeV}, 4.0 \times 10^{-16})$ (red-dashed). The vertical line at $E = 1.1 \text{ PeV}$ is the contribution from the Galaxy.

Motivations.

Few works on this topic:

- Frampton, Glashow, '80
- Gelmini, Gondolo, Sarkar '92
- Kanzaki, Kawasaki, Kohri, Moroi '07
- Ema, Jinno, Moroi '13, '14
- McKeen '18
- ...

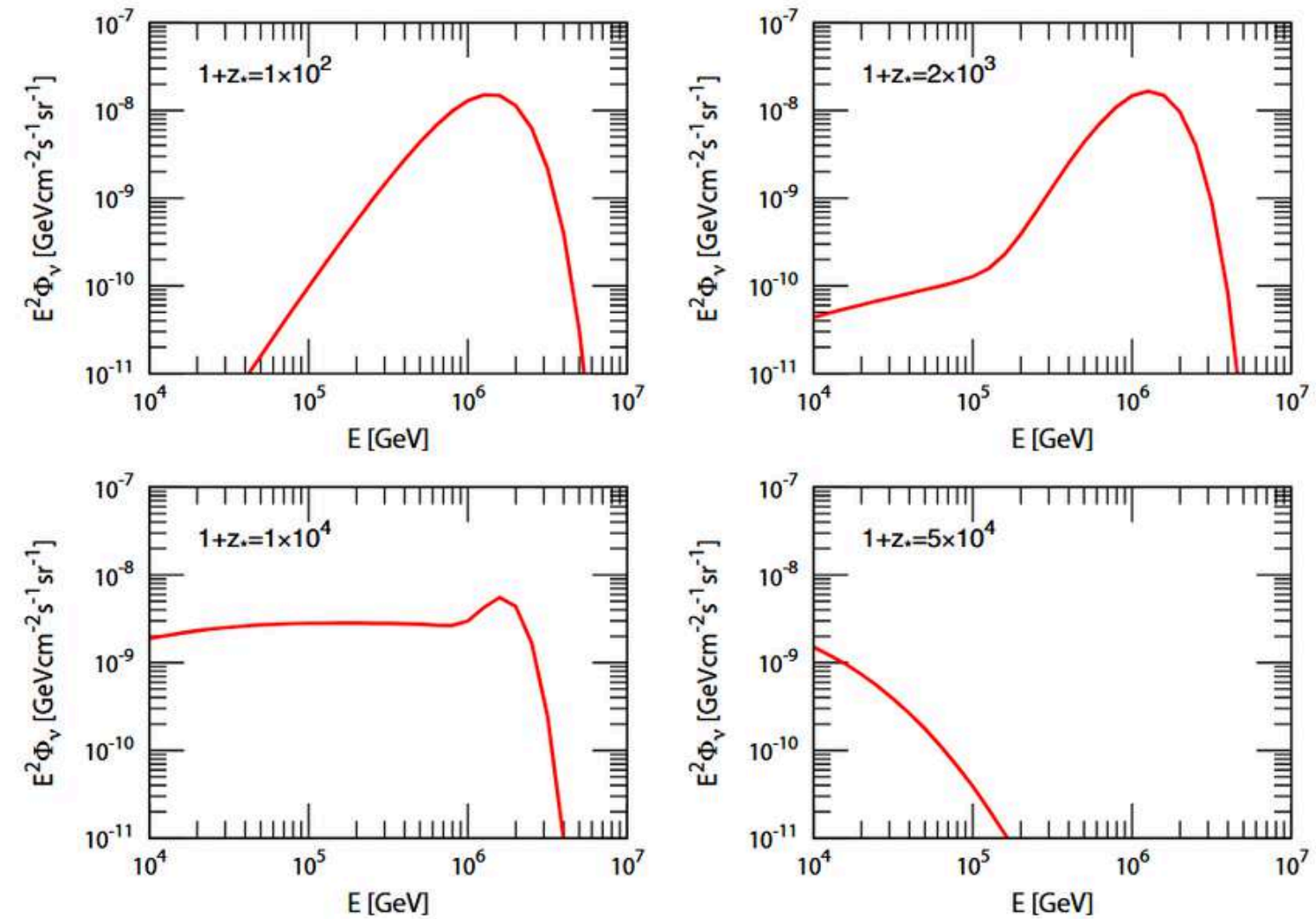
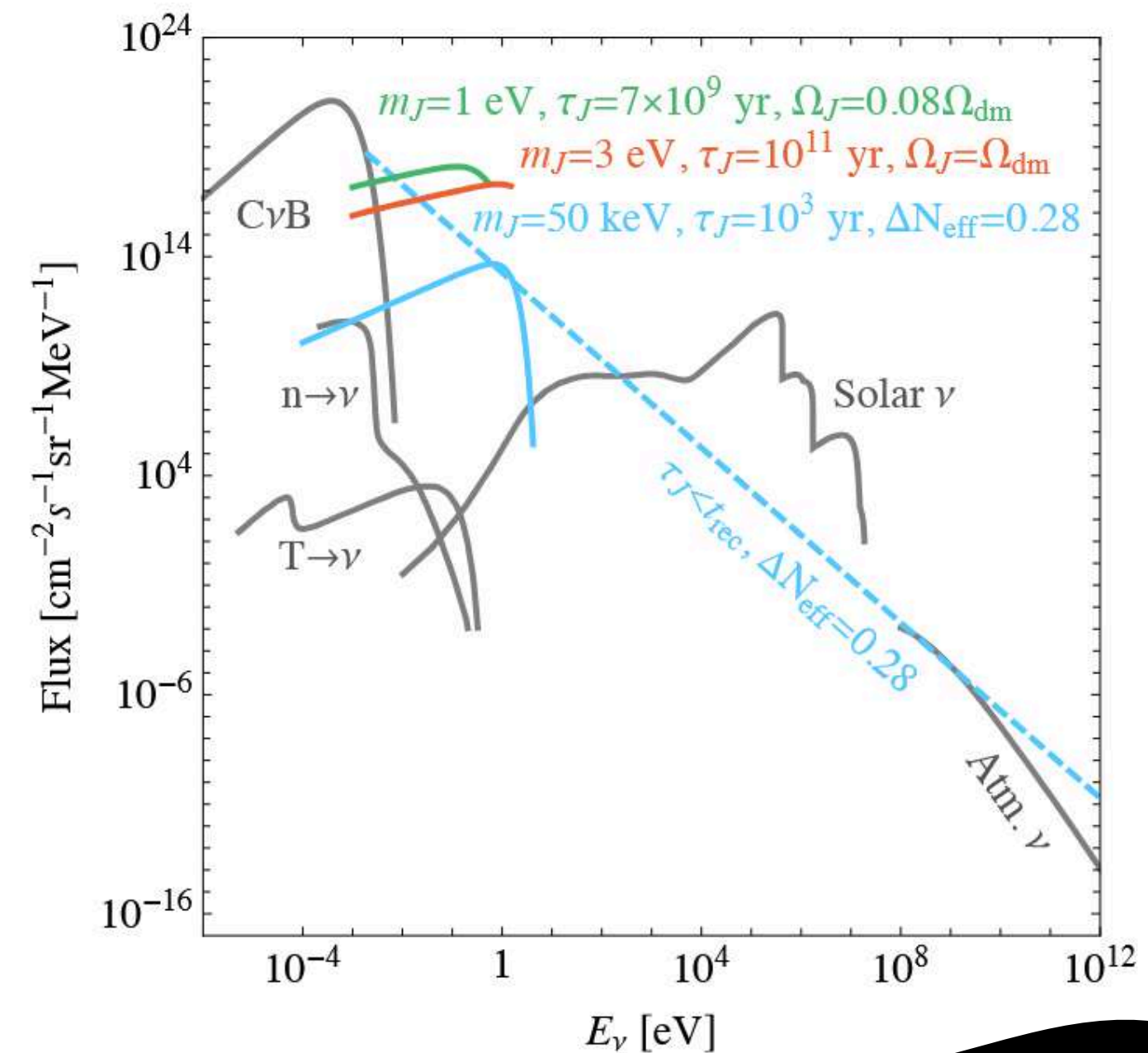


Figure 2: The present per-flavor neutrino fluxes for some different input parameters. Top left: $(\bar{E}_\nu, 1+z_*, Y_X) = (10^8 \text{ GeV}, 10^2, 10^{-26})$. Top right: $(\bar{E}_\nu, 1+z_*, Y_X) = (2 \times 10^9 \text{ GeV}, 2 \times 10^3, 10^{-26})$. Bottom left: $(\bar{E}_\nu, 1+z_*, Y_X) = (10^{10} \text{ GeV}, 10^4, 10^{-26})$. Bottom right: $(\bar{E}_\nu, 1+z_*, Y_X) = (5 \times 10^{10} \text{ GeV}, 5 \times 10^4, 10^{-26})$.

Motivations.

Few works on this topic:

- Frampton, Glashow, '80
- Gelmini, Gondolo, Sarkar '92
- Kanzaki, Kawasaki, Kohri, Moroi '07
- Ema, Jinno, Moroi '13, '14
- **McKeen '18**
- ...

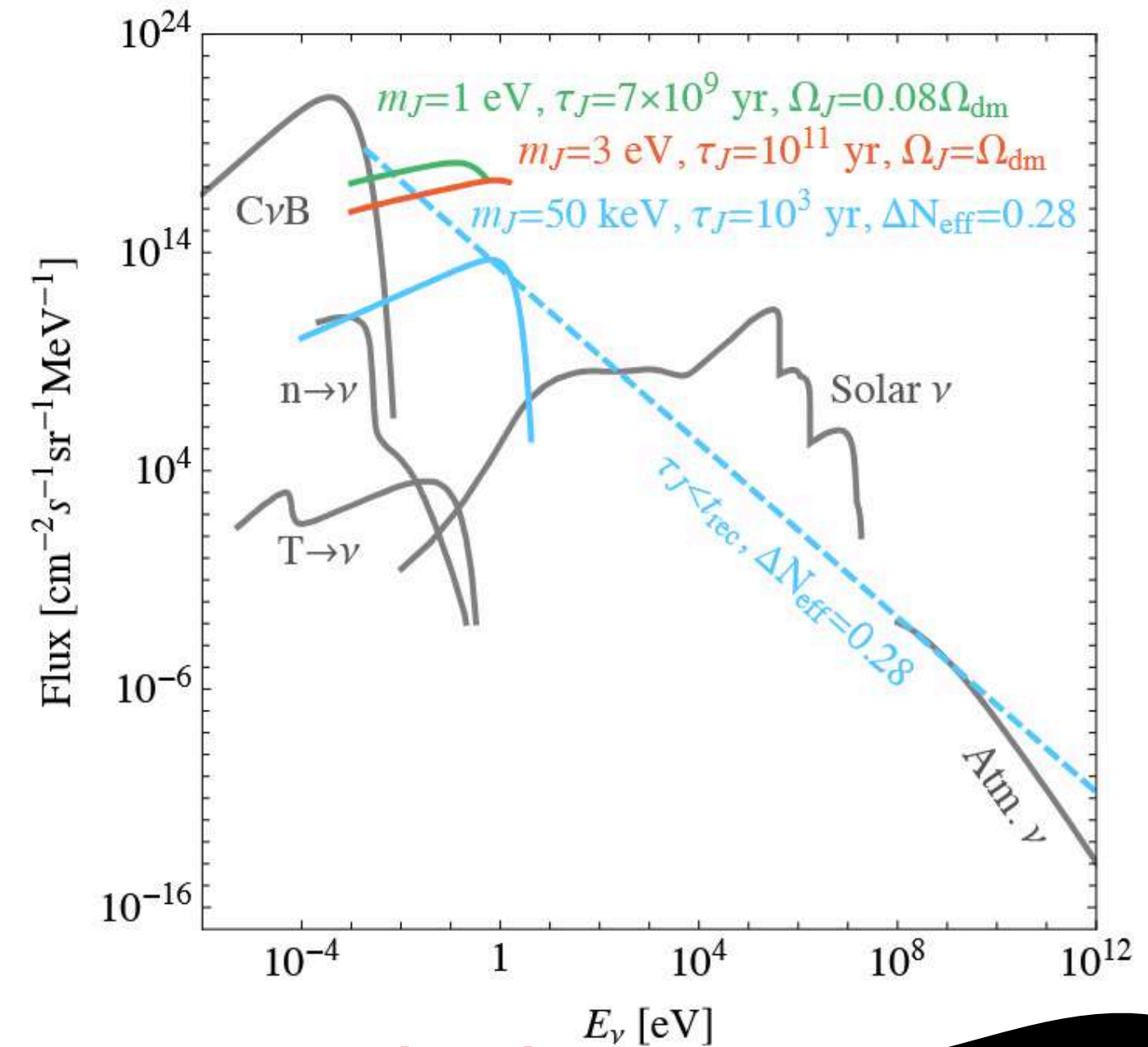


Motivations.

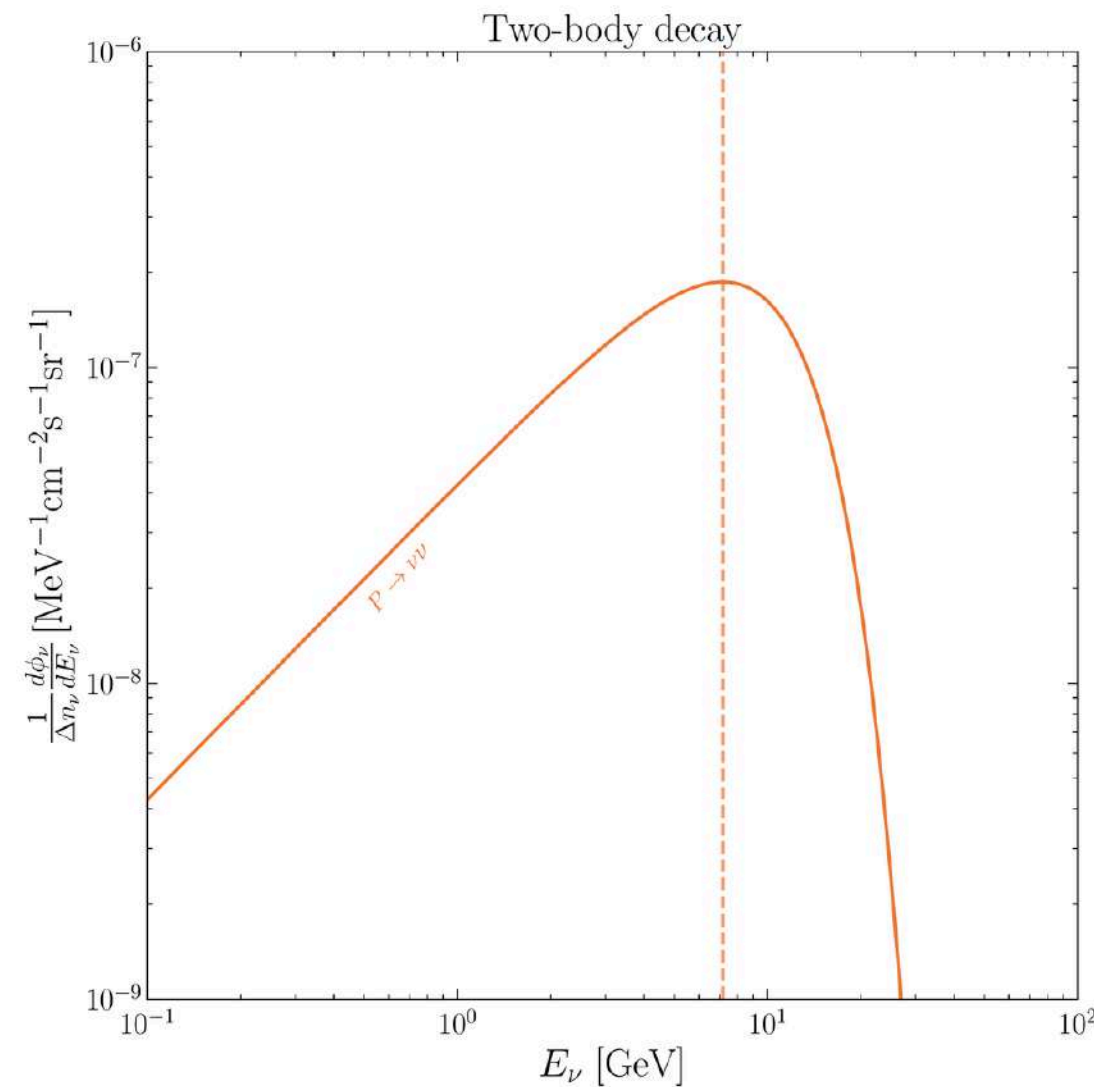
Few works on this topic:

- Frampton, Glashow, '80
- Gelmini, Gondolo, Sarkar '92
- Kanzaki, Kawasaki, Kohri, Moroi '07
- Ema, Jinno, Moroi '13, '14
- **McKeen '18**
- ...

→ **A general study is needed**

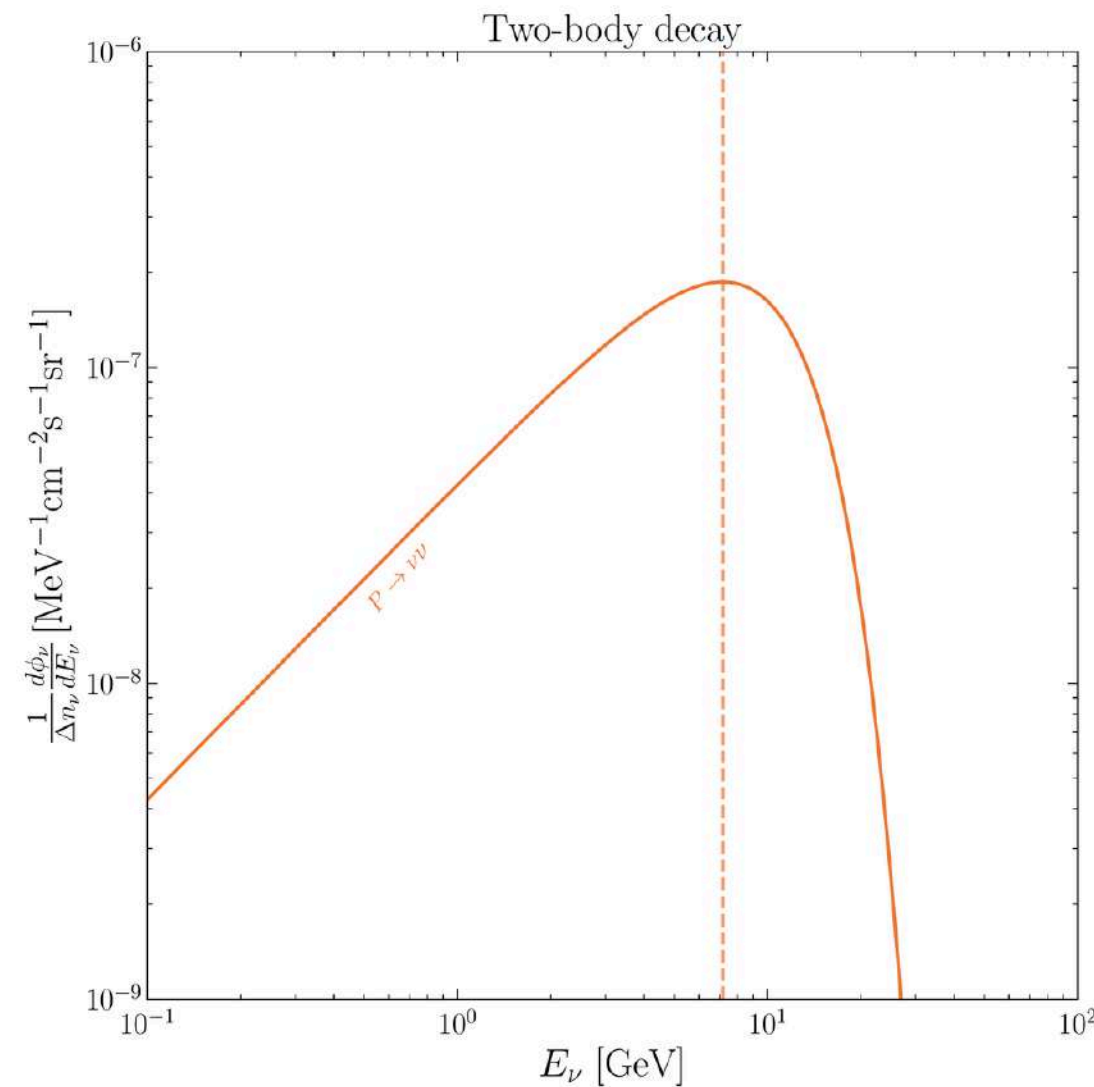


Sharp Spectral Features.



$$\frac{d\phi_\nu}{dE_\nu} = \frac{n\Omega_P^0 \rho_{crit}^0}{4\pi m_P \tau_P} \int_0^\infty dz \frac{e^{-t(z)/\tau_P}}{H(z)} \left. \frac{dN}{dE} \right|_{E=E_\nu(1+z)}$$

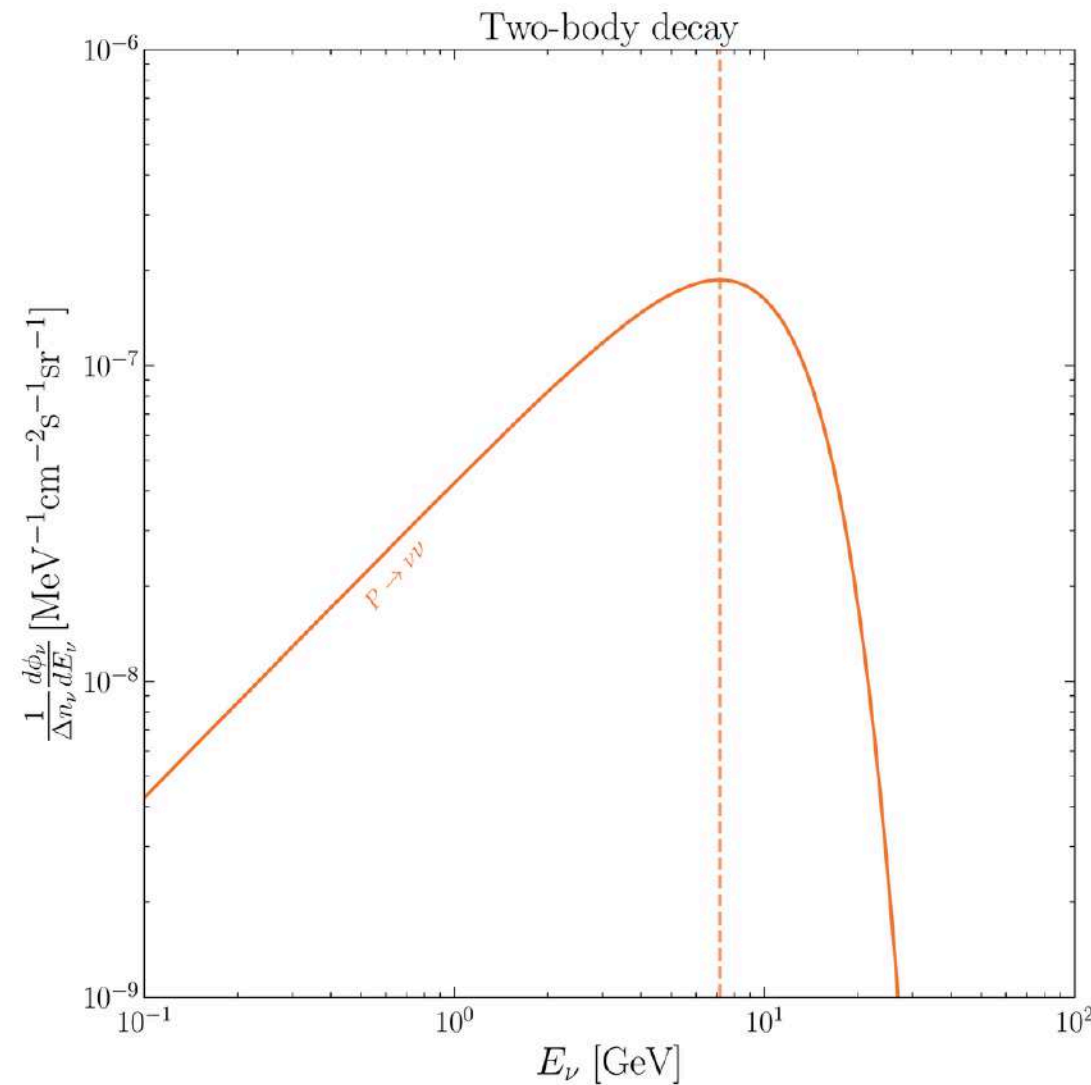
Sharp Spectral Features.



$$\frac{d\phi_\nu}{dE_\nu} = \frac{n\Omega_P^0 \rho_{crit}^0}{4\pi m_P \tau_P} \int_0^\infty dz \frac{e^{-t(z)/\tau_P}}{H(z)} \left. \frac{dN}{dE} \right|_{E=E_\nu(1+z)}$$

Number of
neutrinos
per decay

Sharp Spectral Features.

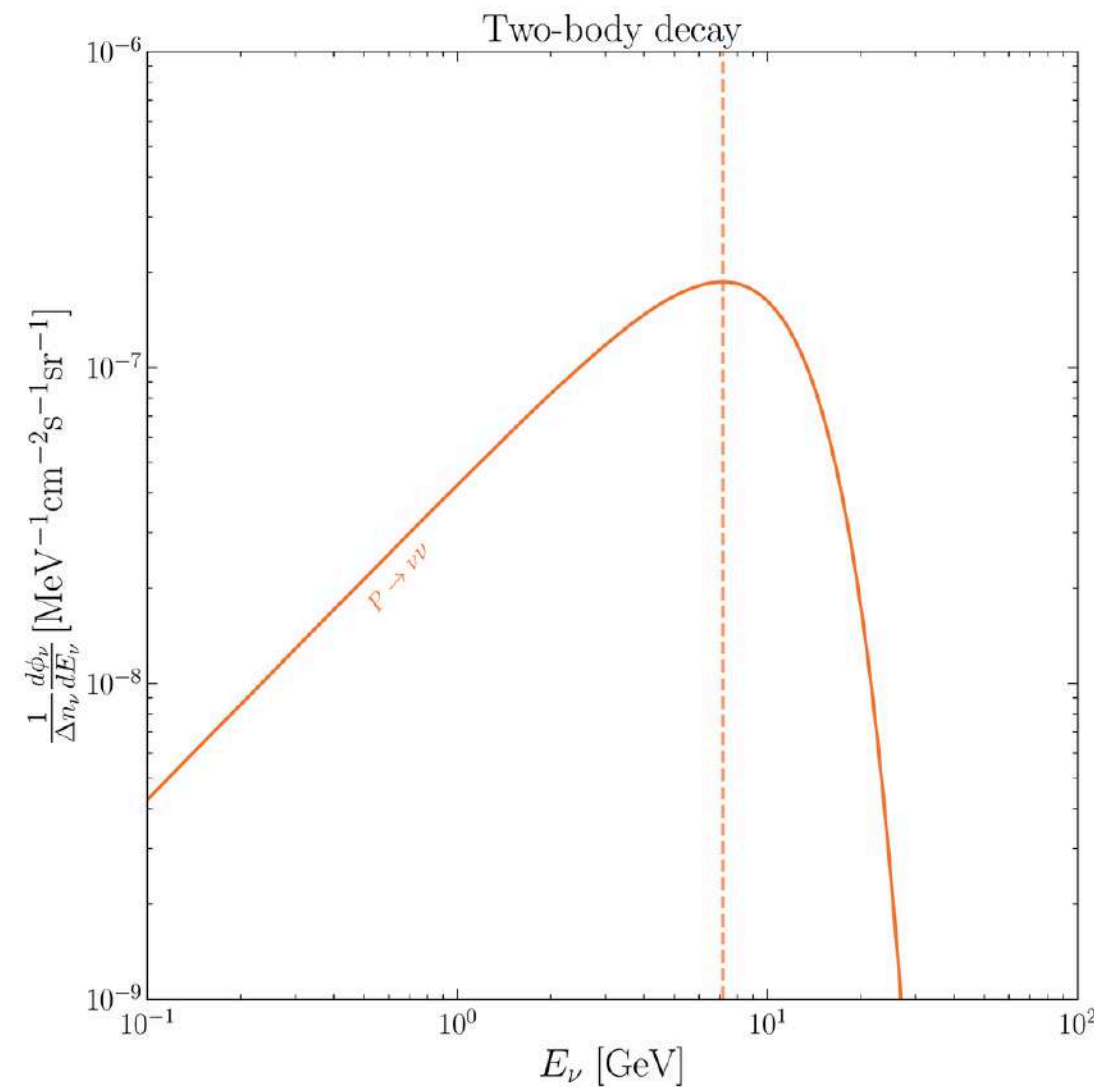


$$\frac{d\phi_\nu}{dE_\nu} = \frac{n\Omega_P^0 \rho_{crit}^0}{4\pi m_P \tau_P} \int_0^\infty dz \frac{e^{-t(z)/\tau_P}}{H(z)} \frac{dN}{dE} \Big|_{E=E_\nu(1+z)}$$

Number of neutrinos per decay

Isotropy

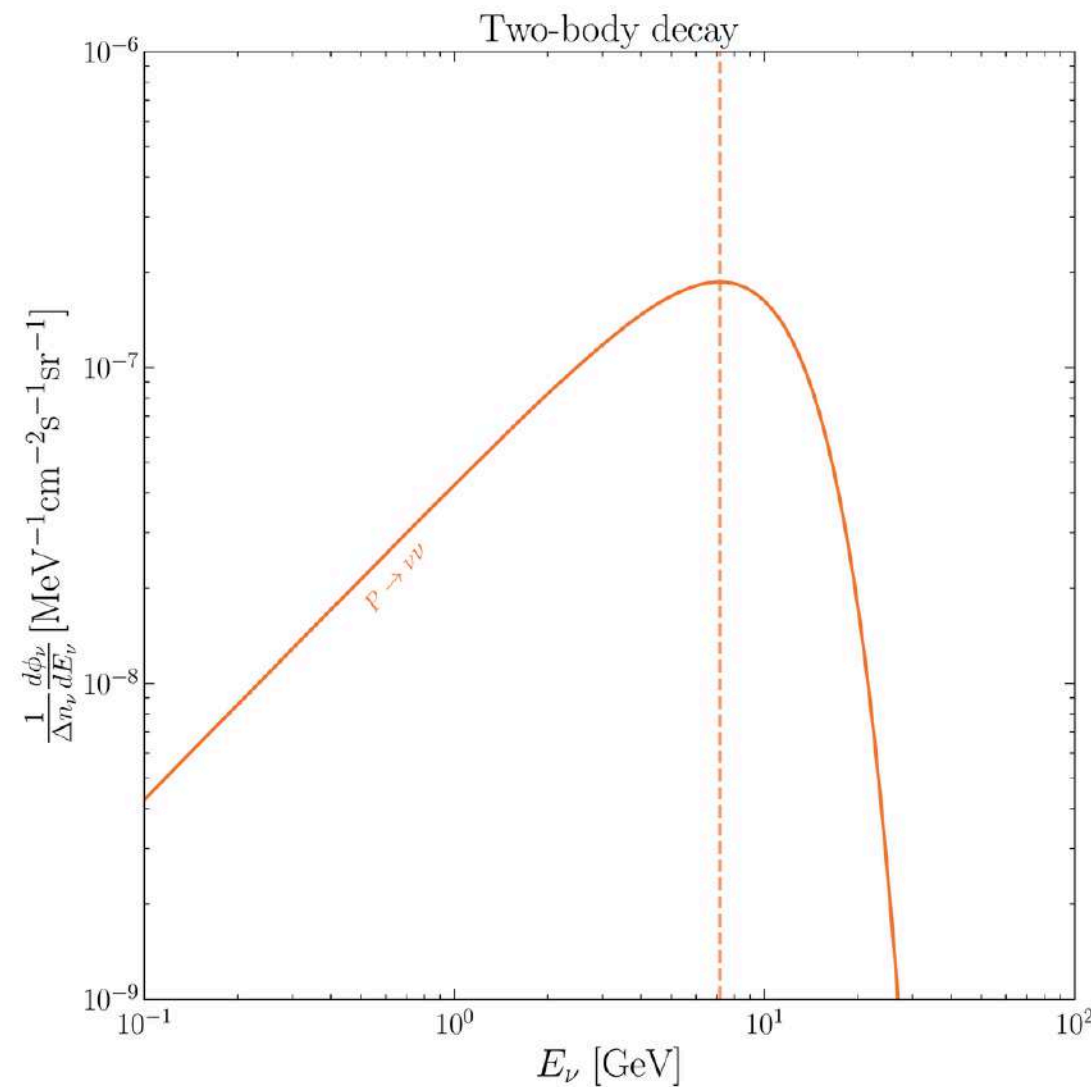
Sharp Spectral Features.



$$\frac{d\phi_\nu}{dE_\nu} = \frac{n\Omega_P^0 \rho_{crit}^0}{4\pi m_P \tau_P} \int_0^\infty dz \frac{e^{-t(z)/\tau_P}}{H(z)} \left. \frac{dN}{dE} \right|_{E=E_\nu(1+z)}$$

Number of neutrinos per decay \rightarrow $n\Omega_P^0 \rho_{crit}^0$
 Isotropy \rightarrow 4π
 Decaying particle density \rightarrow $m_P \tau_P$

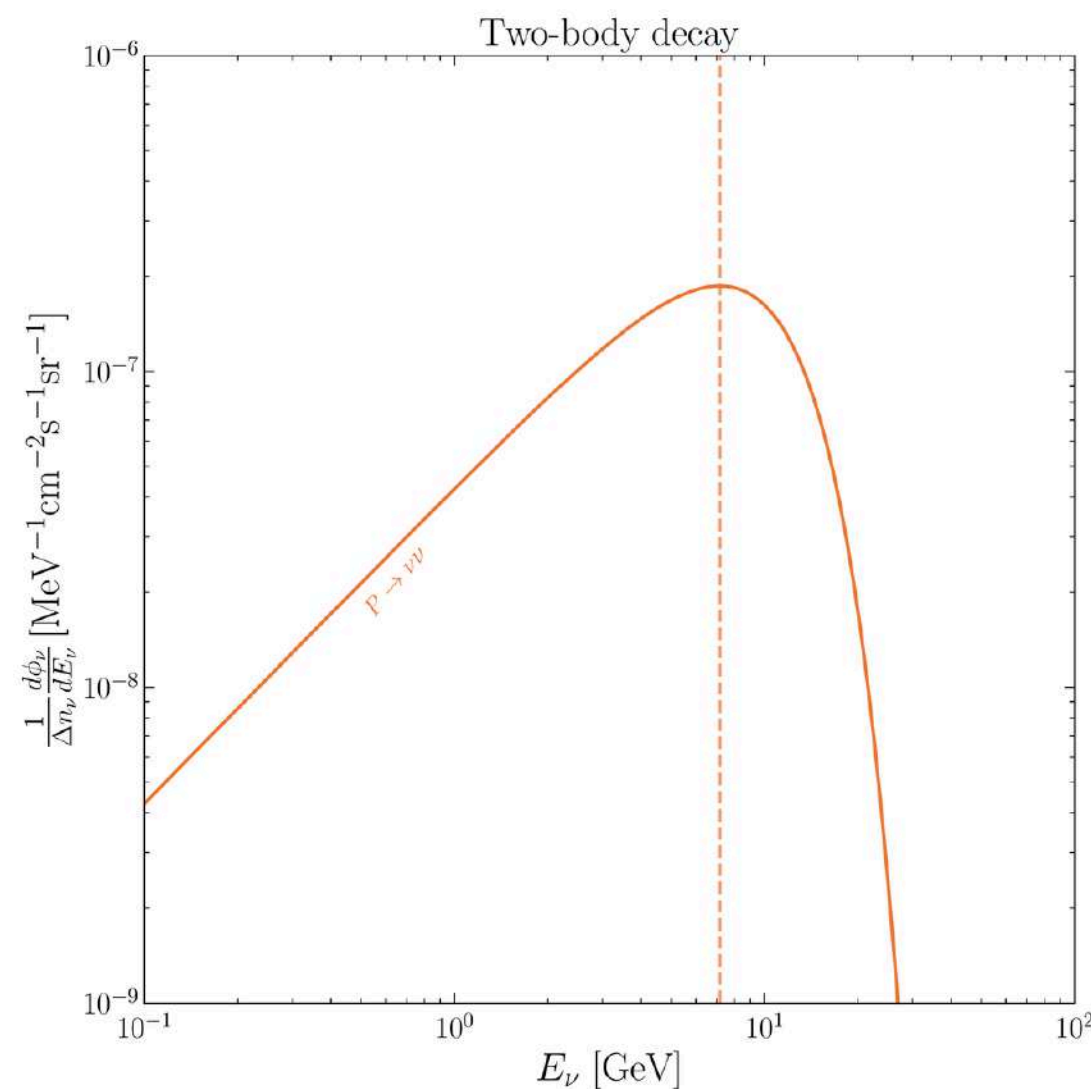
Sharp Spectral Features.



$$\frac{d\phi_\nu}{dE_\nu} = \frac{n\Omega_P^0 \rho_{crit}^0}{4\pi m_P \tau_P} \int_0^\infty dz \frac{e^{-t(z)/\tau_P}}{H(z)} \left. \frac{dN}{dE} \right|_{E=E_\nu(1+z)}$$

Number of neutrinos per decay
 Isotropy
 Decaying particle density
 decay rate

Sharp Spectral Features.



$$\frac{d\phi_\nu}{dE_\nu} = \frac{n\Omega_P^0 \rho_{crit}^0}{4\pi m_P \tau_P} \int_0^\infty dz \frac{e^{-t(z)/\tau_P}}{H(z)} \left. \frac{dN}{dE} \right|_{E=E_\nu(1+z)}$$

Number of neutrinos per decay

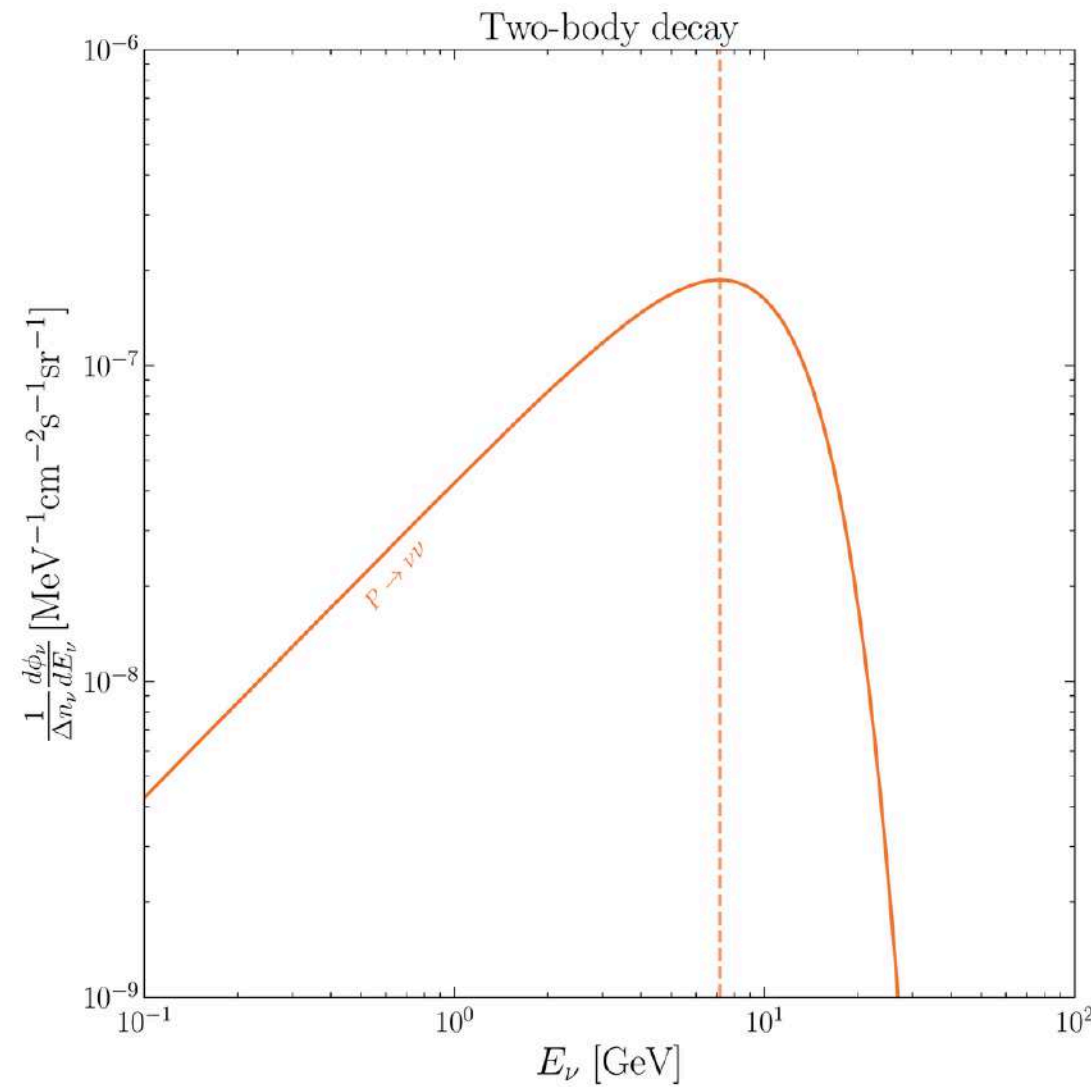
Isotropy

Decaying particle density

decay rate

Integration over the line of sight

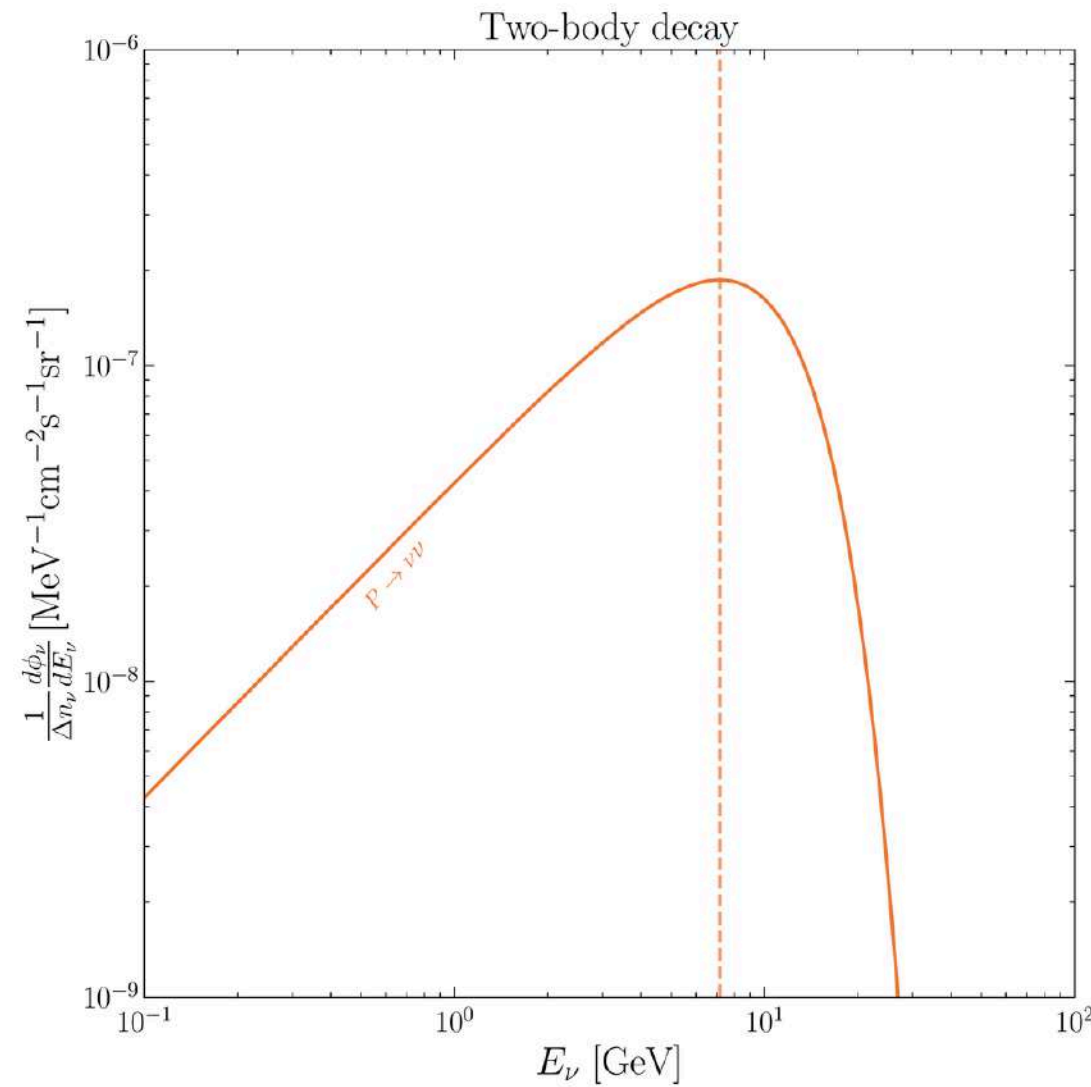
Sharp Spectral Features.



$$\frac{d\phi_\nu}{dE_\nu} = \frac{n\Omega_P^0 \rho_{crit}^0}{4\pi m_P \tau_P} \int_0^\infty dz \frac{e^{-t(z)/\tau_P}}{H(z)} \left. \frac{dN}{dE} \right|_{E=E_\nu(1+z)}$$

Number of neutrinos per decay \rightarrow $n\Omega_P^0 \rho_{crit}^0$
 Isotropy \rightarrow 4π
 Decaying particle density \rightarrow m_P
 decay rate \rightarrow τ_P
 Integration over the line of sight \rightarrow $\int_0^\infty dz$
 Exponential decay \rightarrow $e^{-t(z)/\tau_P}$

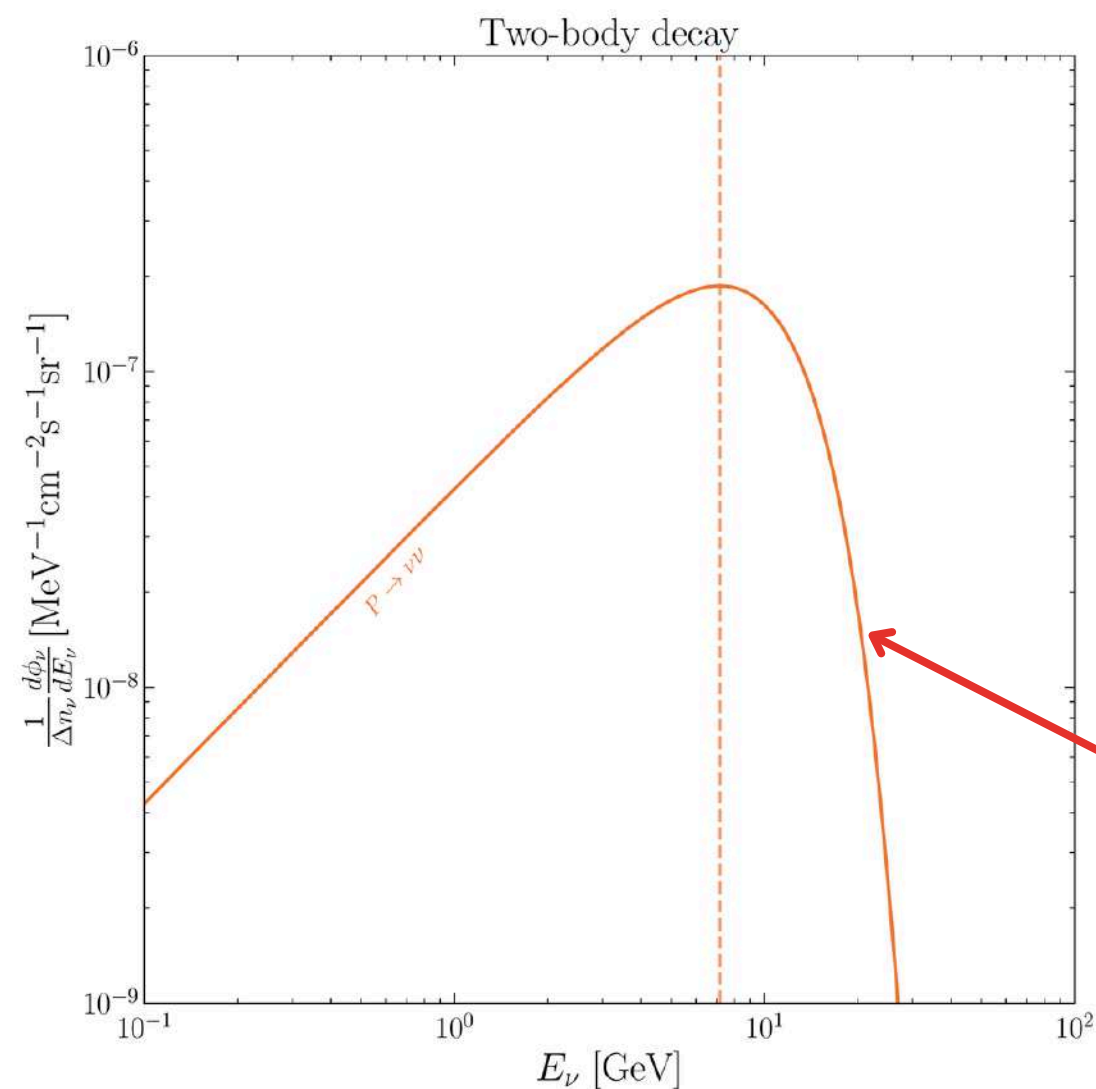
Sharp Spectral Features.



$$\frac{d\phi_\nu}{dE_\nu} = \frac{n\Omega_P^0 \rho_{crit}^0}{4\pi m_P \tau_P} \int_0^\infty dz \frac{e^{-t(z)/\tau_P}}{H(z)} \left. \frac{dN}{dE} \right|_{E=E_\nu(1+z)}$$

Number of neutrinos per decay \rightarrow $n\Omega_P^0 \rho_{crit}^0$
 Isotropy \rightarrow 4π
 Decaying particle density \rightarrow m_P
 decay rate \rightarrow τ_P
 Integration over the line of sight \rightarrow $\int_0^\infty dz$
 Exponential decay \rightarrow $e^{-t(z)/\tau_P}$
 Spectrum at production \rightarrow $\left. \frac{dN}{dE} \right|_{E=E_\nu(1+z)}$

Sharp Spectral Features.

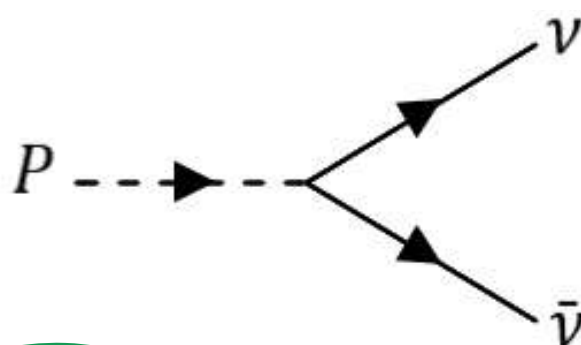


Gelmini, Gondolo, Sarkar 92'

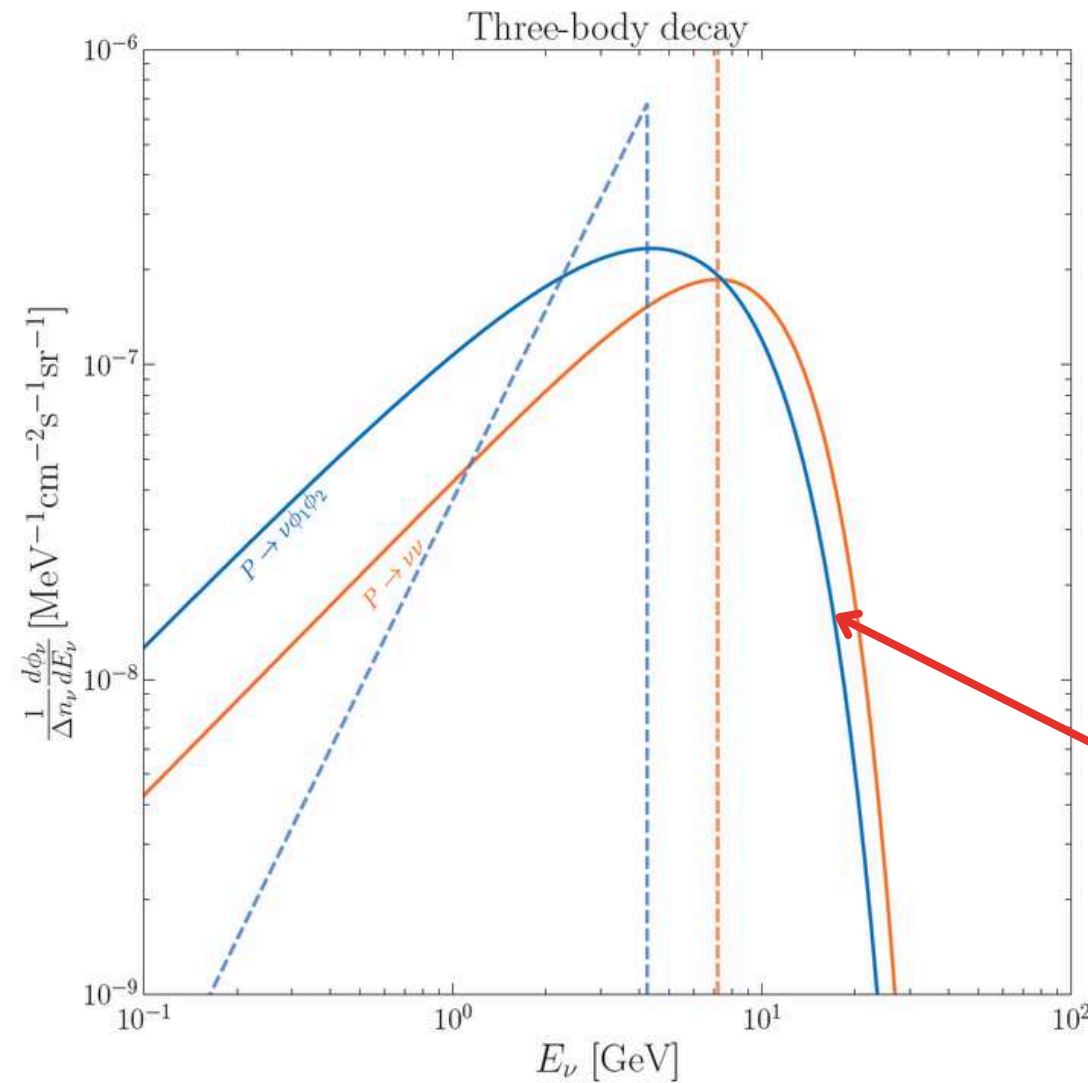
$$\frac{d\phi_\nu}{dE_\nu} = \frac{n\Omega_P^0 \rho_{crit}^0}{4\pi m_P \tau_P} \int_0^\infty dz \frac{e^{-t(z)/\tau_P}}{H(z)} \left. \frac{dN}{dE} \right|_{E=E_\nu(1+z)}$$

Number of neutrinos per decay (points to $n\Omega_P^0 \rho_{crit}^0$)
 Isotropy (points to 4π)
 Decaying particle density (points to m_P)
 decay rate (points to τ_P)
 Integration over the line of sight (points to $\int_0^\infty dz$)
 Exponential decay (points to $e^{-t(z)/\tau_P}$)
 Spectrum at production (points to $\left. \frac{dN}{dE} \right|_{E=E_\nu(1+z)}$)

2-body decay $P \rightarrow \nu \bar{\nu}$



Sharp Spectral Features.



$$\frac{d\phi_\nu}{dE_\nu} = \frac{n\Omega_P^0 \rho_{crit}^0}{4\pi m_P \tau_P} \int_0^\infty dz \frac{e^{-t(z)/\tau_P}}{H(z)} \left. \frac{dN}{dE} \right|_{E=E_\nu(1+z)}$$

Number of neutrinos per decay

Isotropy

Decaying particle density

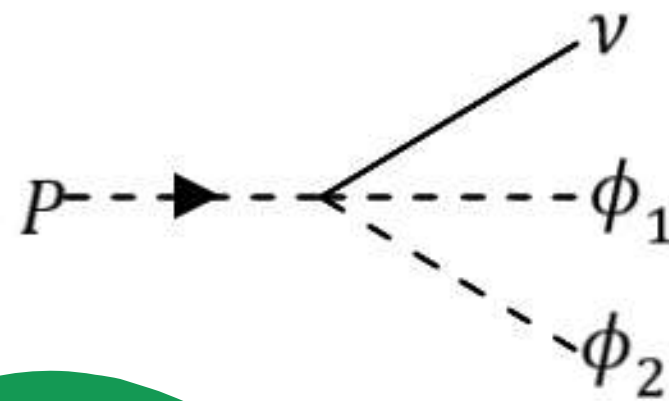
decay rate

Integration over the line of sight

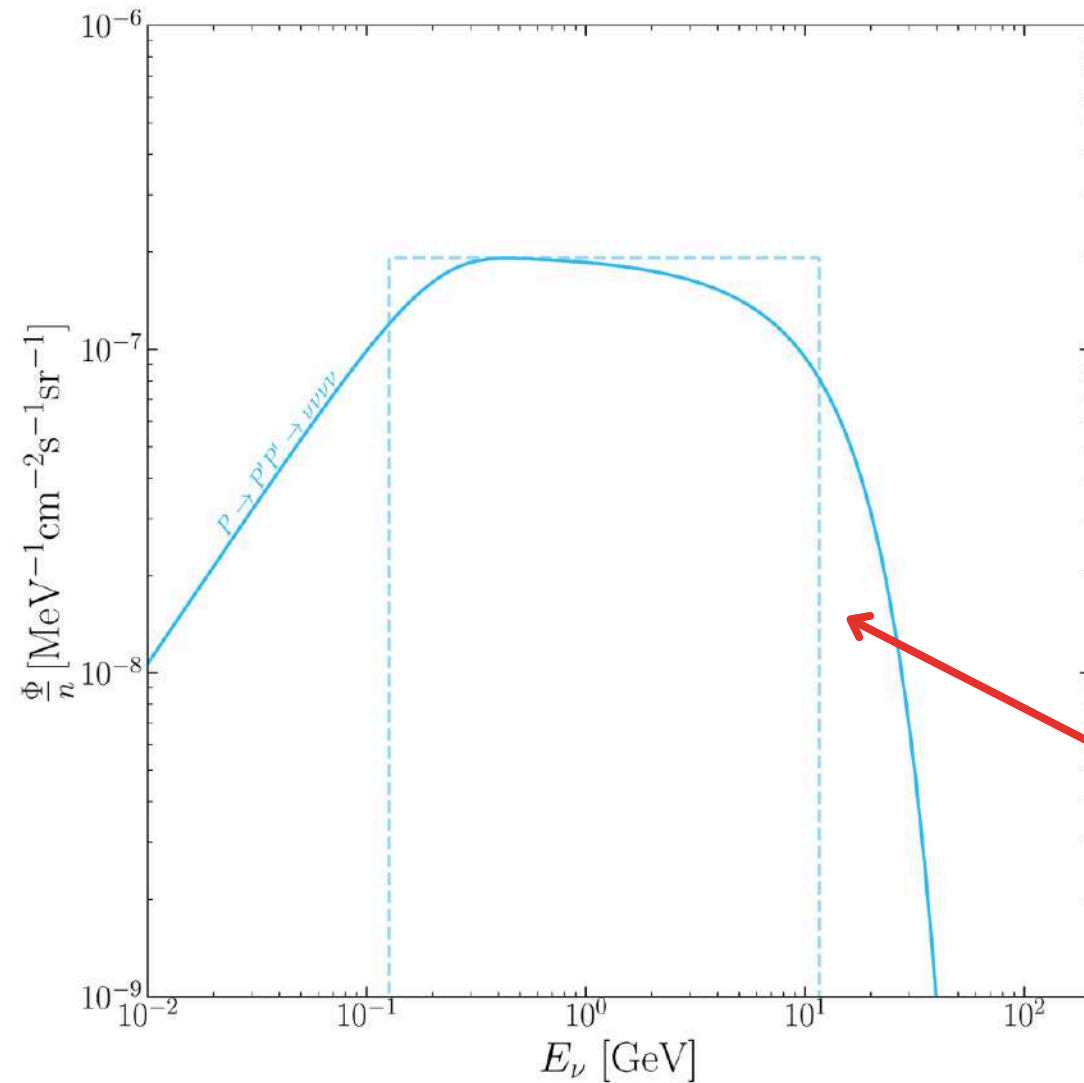
Exponential decay

Spectrum at production

3-body decay $P \rightarrow \nu\phi_1\phi_2$



Sharp Spectral Features.

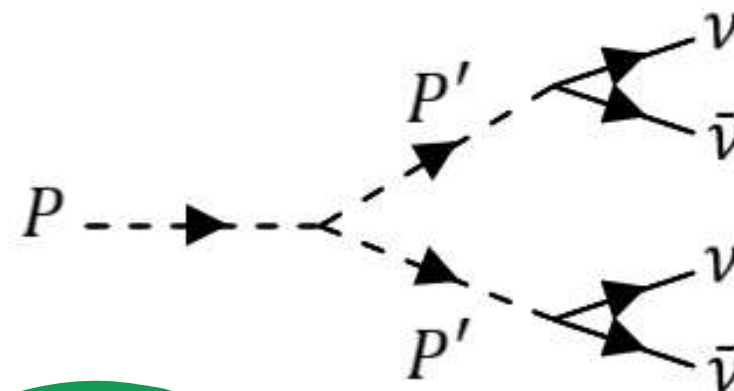


Ibarra, Lopez Gehler, Pato, Miguel, 12'

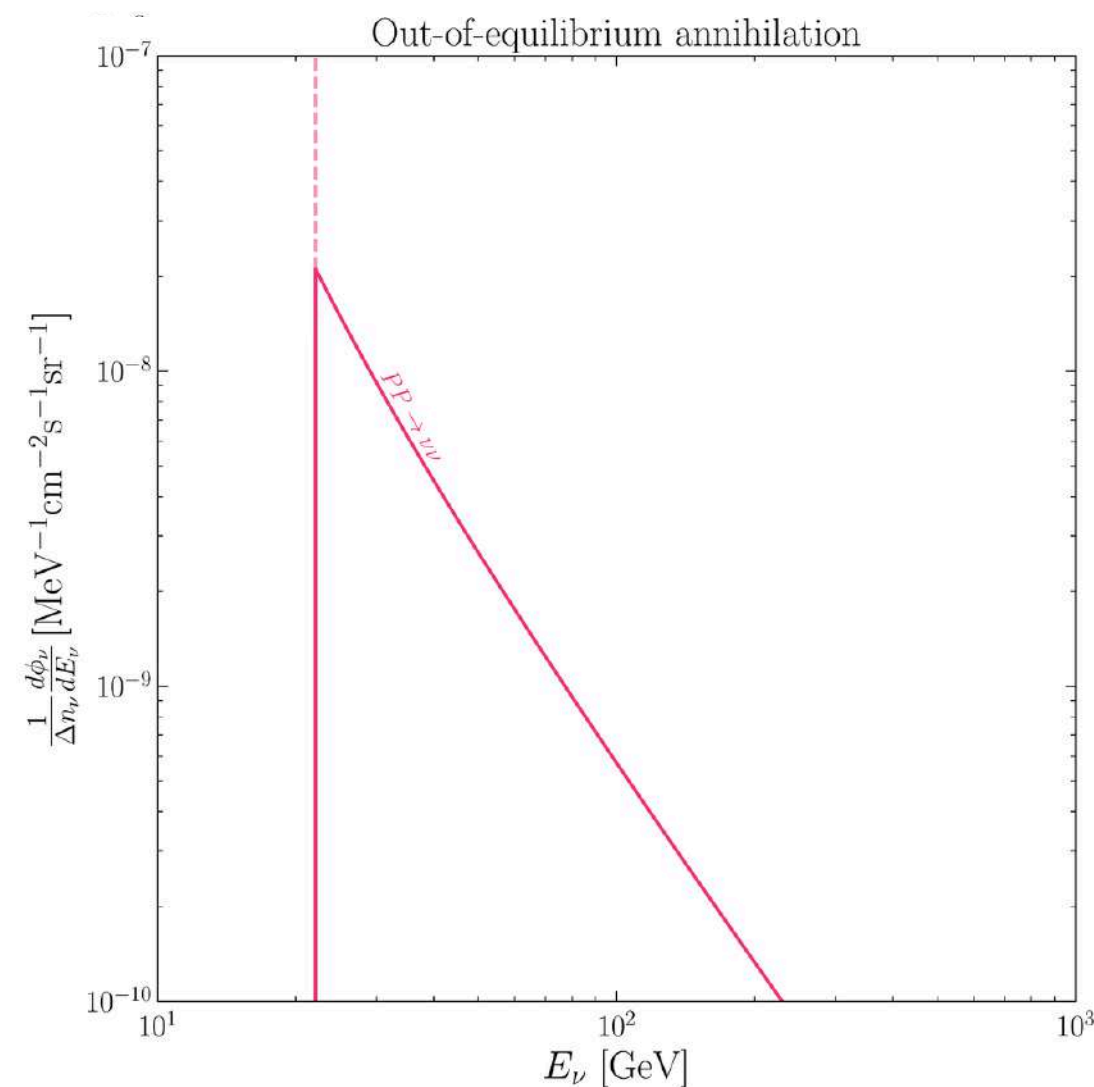
$$\frac{d\phi_\nu}{dE_\nu} = \frac{n\Omega_P^0 \rho_{crit}^0}{4\pi m_P \tau_P} \int_0^\infty dz \frac{e^{-t(z)/\tau_P}}{H(z)} \left. \frac{dN}{dE} \right|_{E=E_\nu(1+z)}$$

Number of neutrinos per decay (points to $n\Omega_P^0 \rho_{crit}^0$)
 Isotropy (points to 4π)
 Decaying particle density (points to m_P)
 decay rate (points to τ_P)
 Integration over the line of sight (points to $\int_0^\infty dz$)
 Exponential decay (points to $e^{-t(z)/\tau_P}$)
 Spectrum at production (points to $\left. \frac{dN}{dE} \right|_{E=E_\nu(1+z)}$)

Box shaped spectrum $P \rightarrow P' P' \rightarrow \nu \bar{\nu} \nu \bar{\nu}$



Sharp Spectral Features.

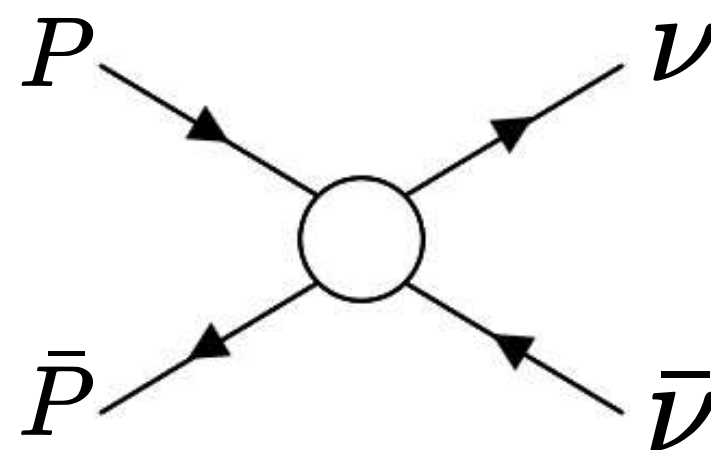


Out of equilibrium annihilation

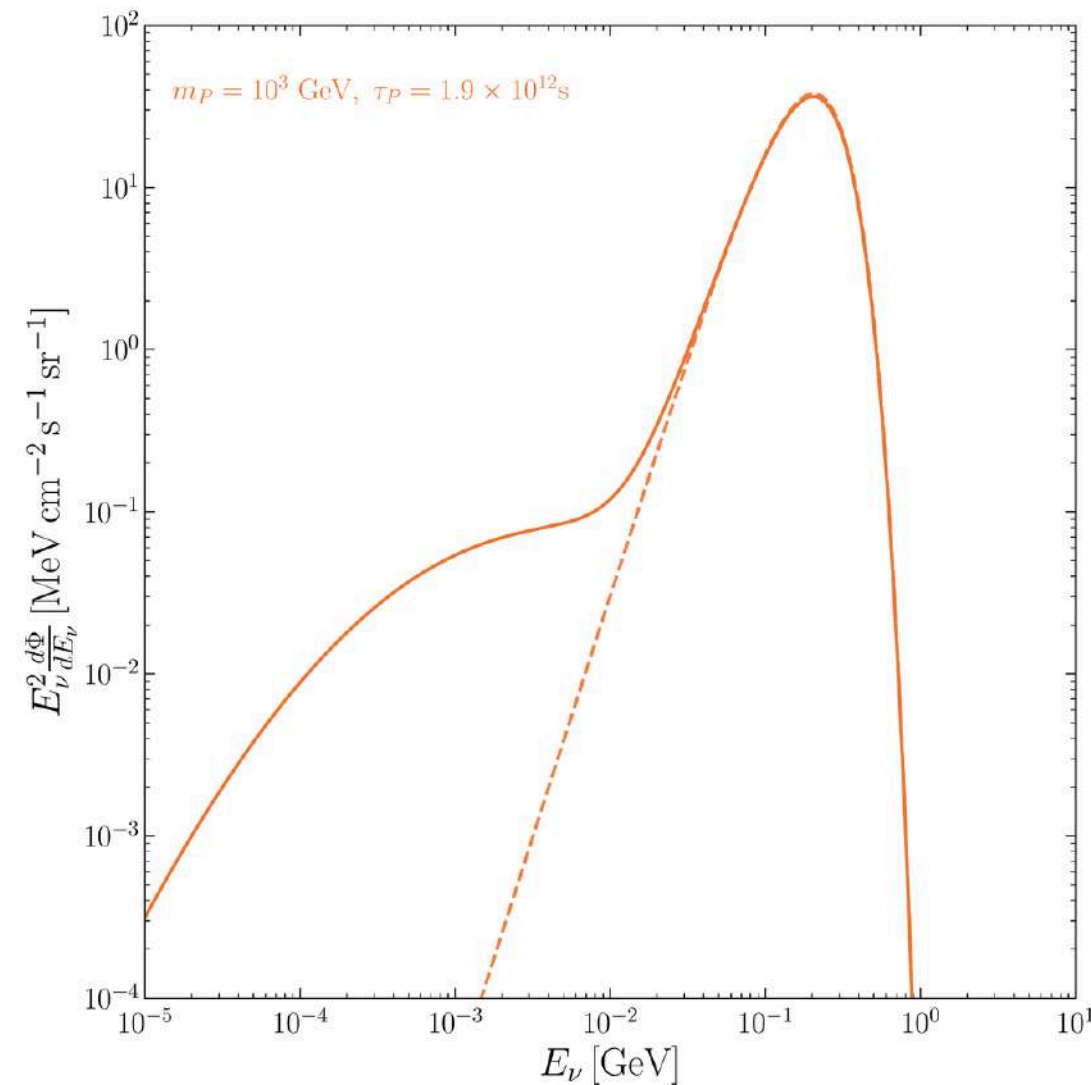
$$P\bar{P} \rightarrow \nu\bar{\nu}$$

New type of spectral feature

From, e.g., an asymmetric population of P
oscillating into anti-P after a phase transition

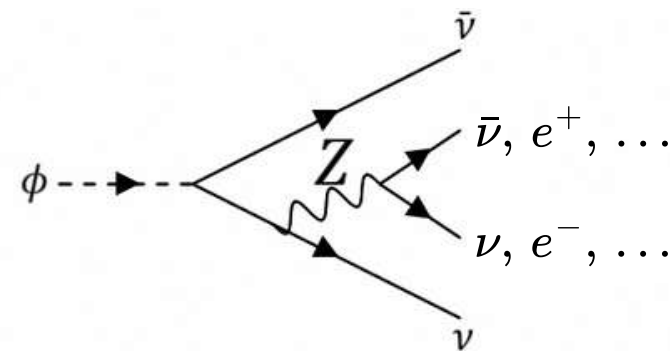


Sharp Spectral Features.

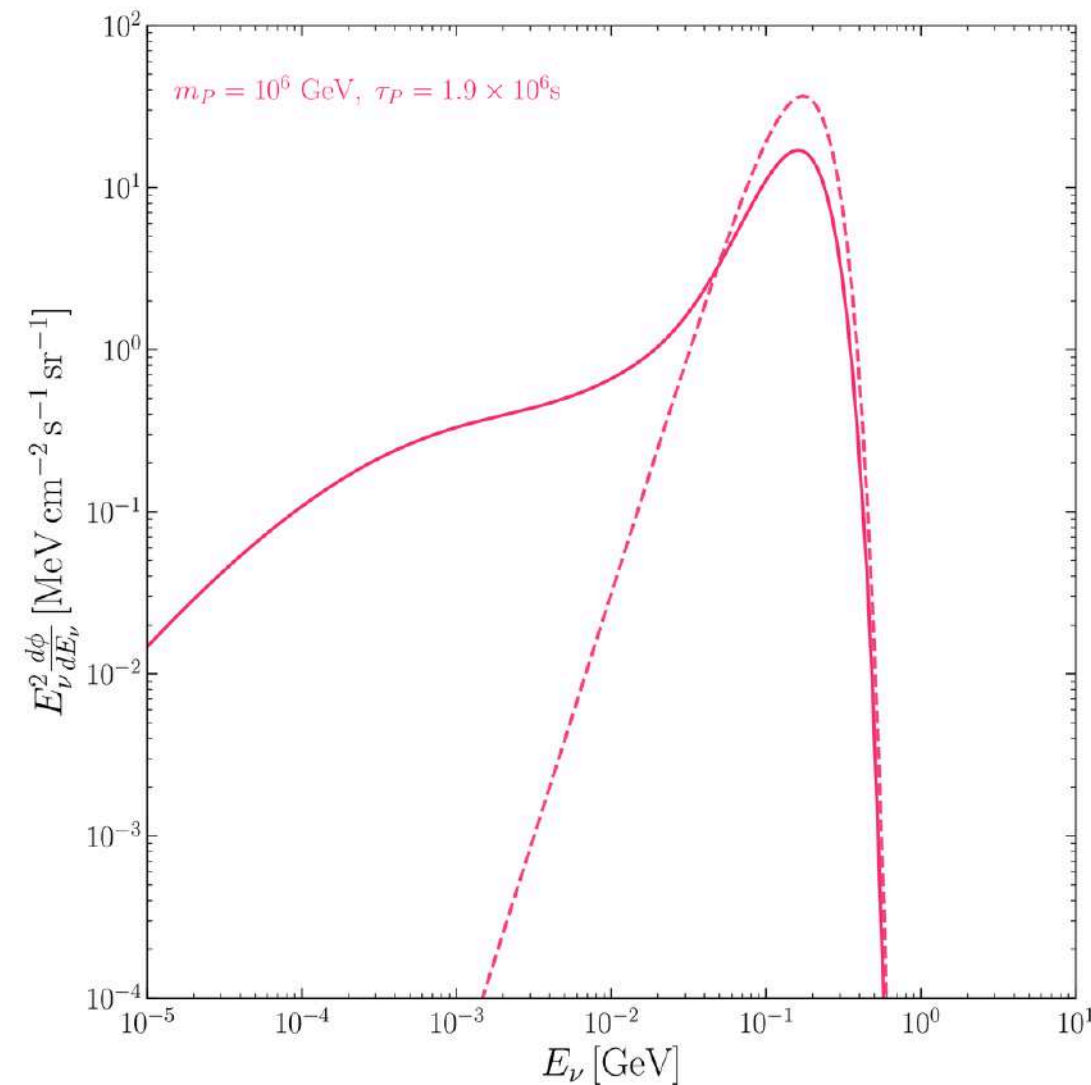


Final state radiation broadening

- If $E_\nu > M_{Z/W}$, gauge bosons can be radiated and generate a shower
- Production of (many) secondary neutrinos of lower energies
- Energy dependent process



Sharp Spectral Features.



Final state radiation broadening

- If $E_\nu > M_{Z/W}$, gauge bosons can be radiated and generate a shower
- Production of (many) secondary neutrinos of lower energies
- Energy dependent process



**Broadening of the peak
mostly due to redshift effect**

Medium interactions. ●

$$S_\nu(z_e, E_0) = \int_0^{z_e} \frac{dz}{(1+z)H(z)} \langle \sigma_\nu \rangle n_{\nu BG}$$

Medium interactions.

$$S_\nu(z_e, E_0) = \int_0^{z_e} \frac{dz}{(1+z)H(z)} \langle \sigma v \rangle n_{\nu BG}$$



Average number
of scattering

Medium interactions.

$$S_\nu(z_e, E_0) = \int_0^{z_e} \frac{dz}{(1+z)H(z)} \langle \sigma v \rangle n_{\nu BG}$$

Average number
of scattering

Integration
over the line of
sight

Medium interactions.

$$S_\nu(z_e, E_0) = \int_0^{z_e} \frac{dz}{(1+z)H(z)} \langle \sigma v \rangle n_{\nu BG}$$

Average number
of scattering

Integration
over the line of
sight

cross section
averaged over
target distribution
function

Medium interactions.

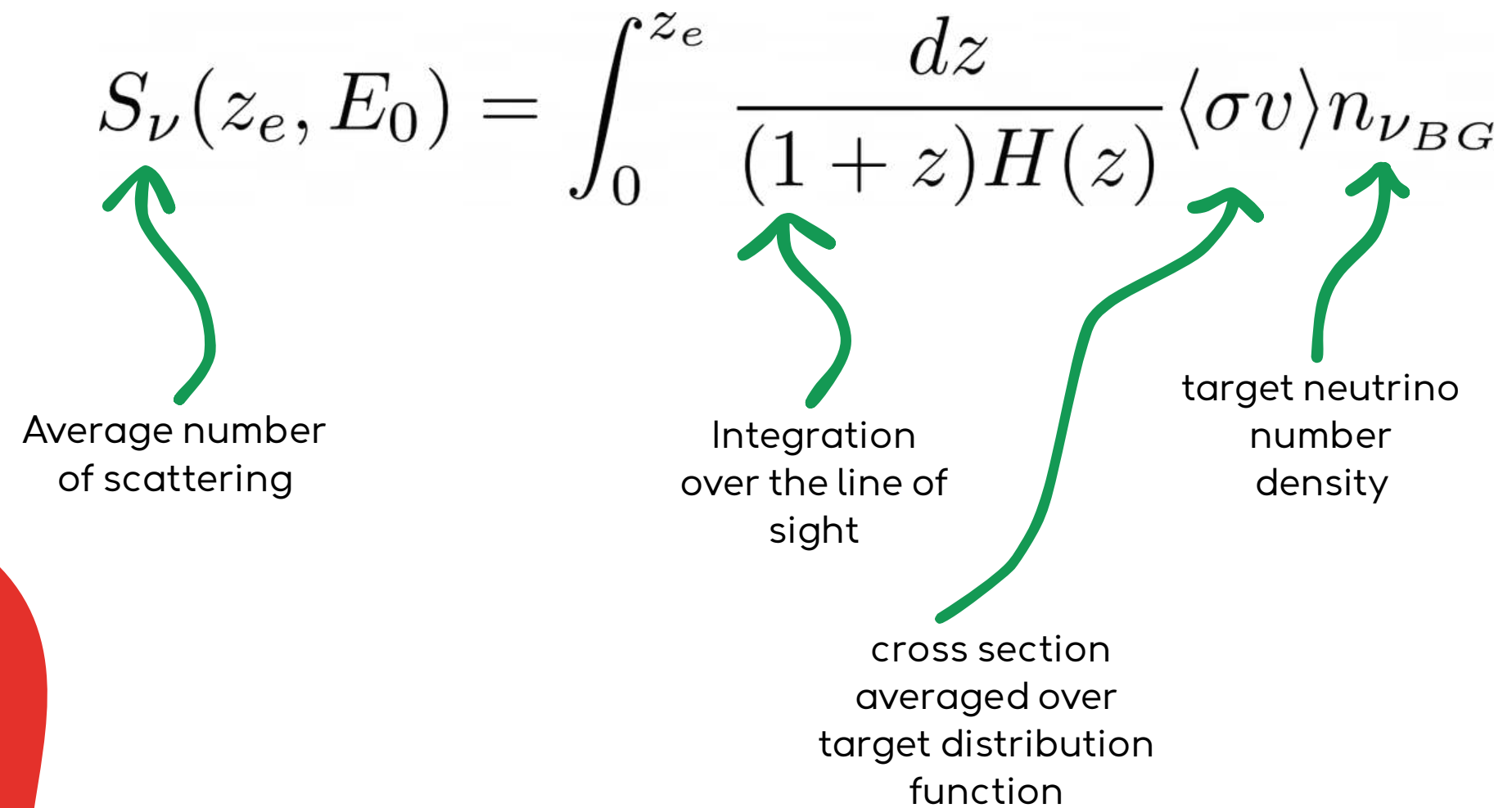
$$S_\nu(z_e, E_0) = \int_0^{z_e} \frac{dz}{(1+z)H(z)} \langle \sigma v \rangle n_{\nu BG}$$

Average number of scattering

Integration over the line of sight

cross section averaged over target distribution function

target neutrino number density

The diagram illustrates the components of the equation for the average number of scattering, $S_\nu(z_e, E_0)$. The equation is
$$S_\nu(z_e, E_0) = \int_0^{z_e} \frac{dz}{(1+z)H(z)} \langle \sigma v \rangle n_{\nu BG}$$
 Four green arrows point from descriptive text to parts of the equation: 1. An arrow points from "Average number of scattering" to the left side of the equation, $S_\nu(z_e, E_0)$. 2. An arrow points from "Integration over the line of sight" to the integral symbol $\int_0^{z_e}$. 3. An arrow points from "cross section averaged over target distribution function" to the term $\langle \sigma v \rangle$. 4. An arrow points from "target neutrino number density" to the term $n_{\nu BG}$.

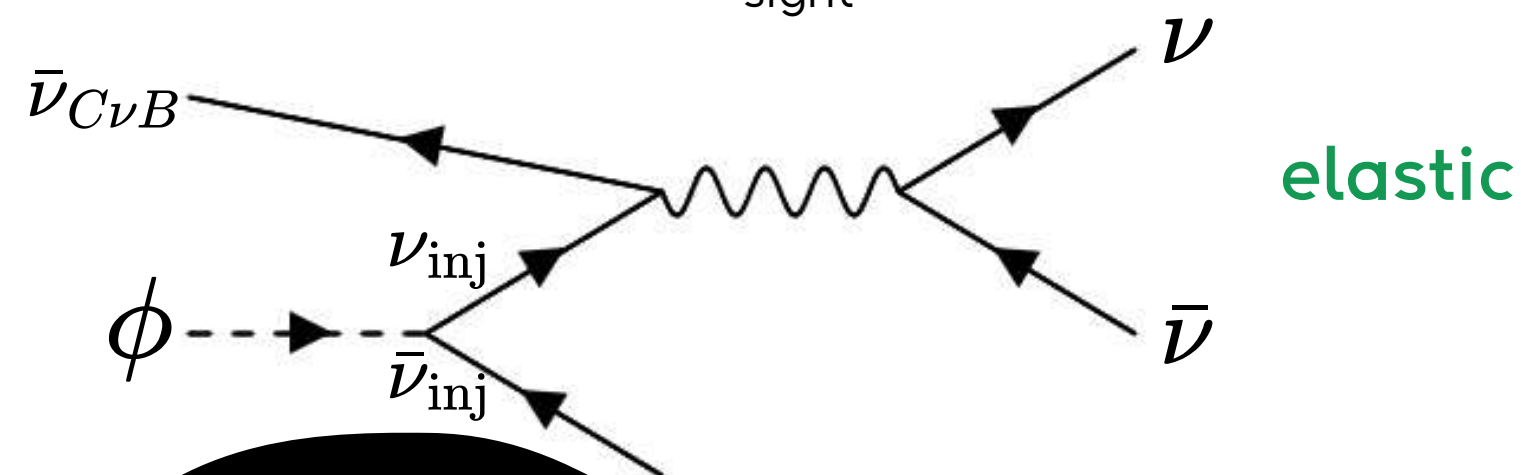
Medium interactions.

$$S_\nu(z_e, E_0) = \int_0^{z_e} \frac{dz}{(1+z)H(z)} \langle \sigma v \rangle n_{\nu BG}$$

Average number
of scattering

Integration
over the line of
sight

target neutrino
number
density



CνB:

- Decoupled at $T \sim 1$ MeV from the thermal bath
- Has a present density of 336 cm^{-3}
- Non-relativistic today

$$T_{C\nu B}^0 = \left(\frac{4}{11} \right)^{1/3} T_{\text{CMB}}^0 \simeq 1.95 \text{ K}$$

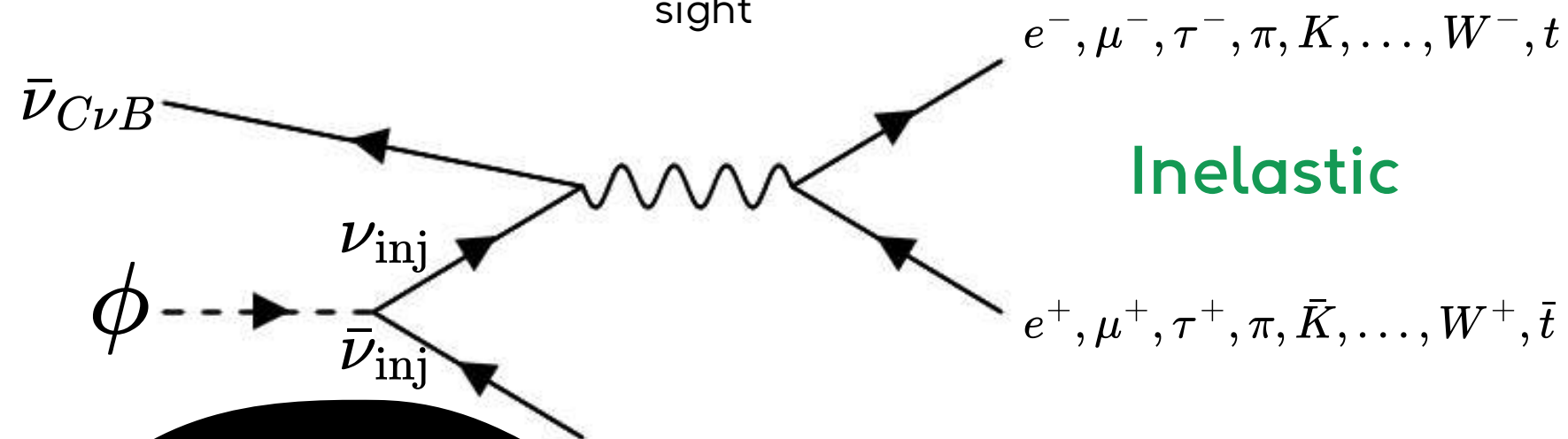
Medium interactions.

$$S_\nu(z_e, E_0) = \int_0^{z_e} \frac{dz}{(1+z)H(z)} \langle \sigma v \rangle n_{\nu BG}$$

Average number of scattering

Integration over the line of sight

target neutrino number density



CνB:

- Decoupled at T~1 MeV from the thermal bath
- Has a present density of 336 cm⁻³
- Non-relativistic today

$$T_{C\nu B}^0 = \left(\frac{4}{11} \right)^{1/3} T_{\text{CMB}}^0 \simeq 1.95\text{K}$$

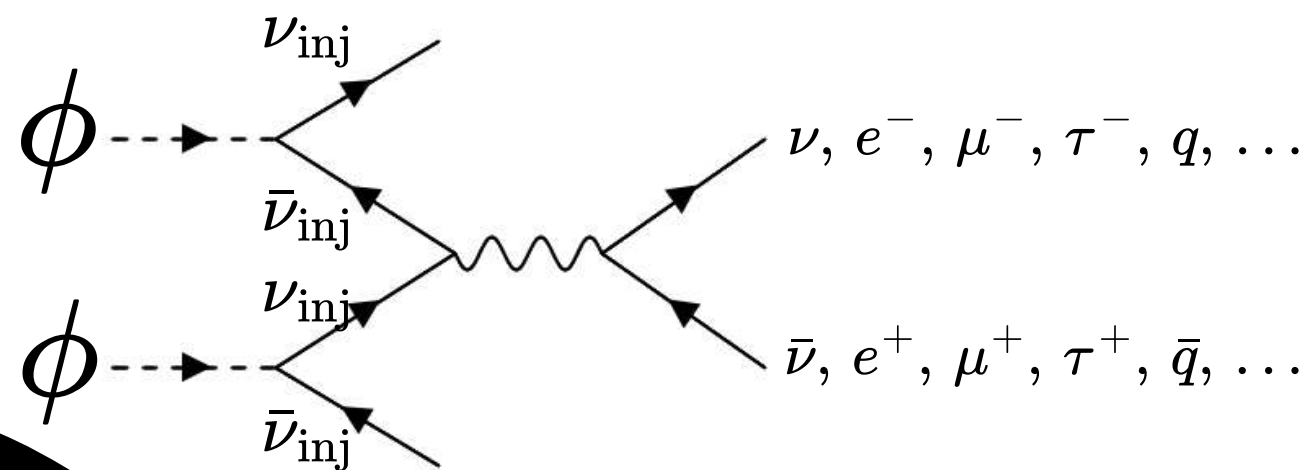
Medium interactions.

$$S_\nu(z_e, E_0) = \int_0^{z_e} \frac{dz}{(1+z)H(z)} \langle \sigma v \rangle n_{\nu BG}$$

Average number
of scattering

Integration
over the line of
sight

target neutrino
number
density



Self-scattering:

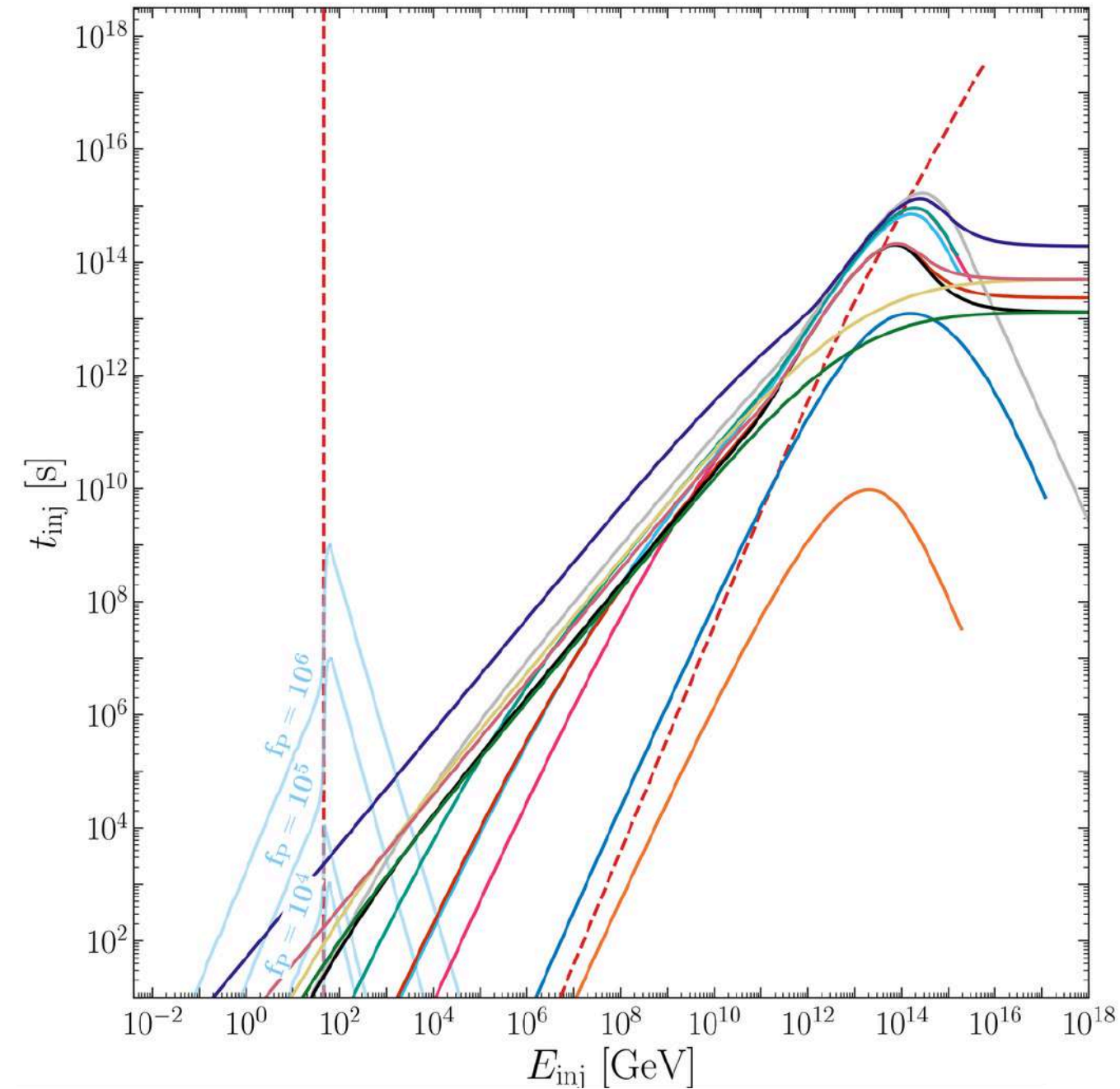
- Very low density, but high energies
 - Numerically hard (triple integral)
- Assume instantaneous decay, i.e. all neutrinos produced at the same redshift with energy $m/2$

Medium interactions.

$$S_\nu(z_e, E_0) = \int_0^{z_e} \frac{dz}{(1+z)H(z)} \langle \sigma v \rangle n_{\nu BG}$$

Average number of scattering
 Integration over the line of sight
 cross section averaged over target distribution function
 target neutrino number density

$$f = \frac{\Omega_P^0}{\Omega_{DM}^0}$$

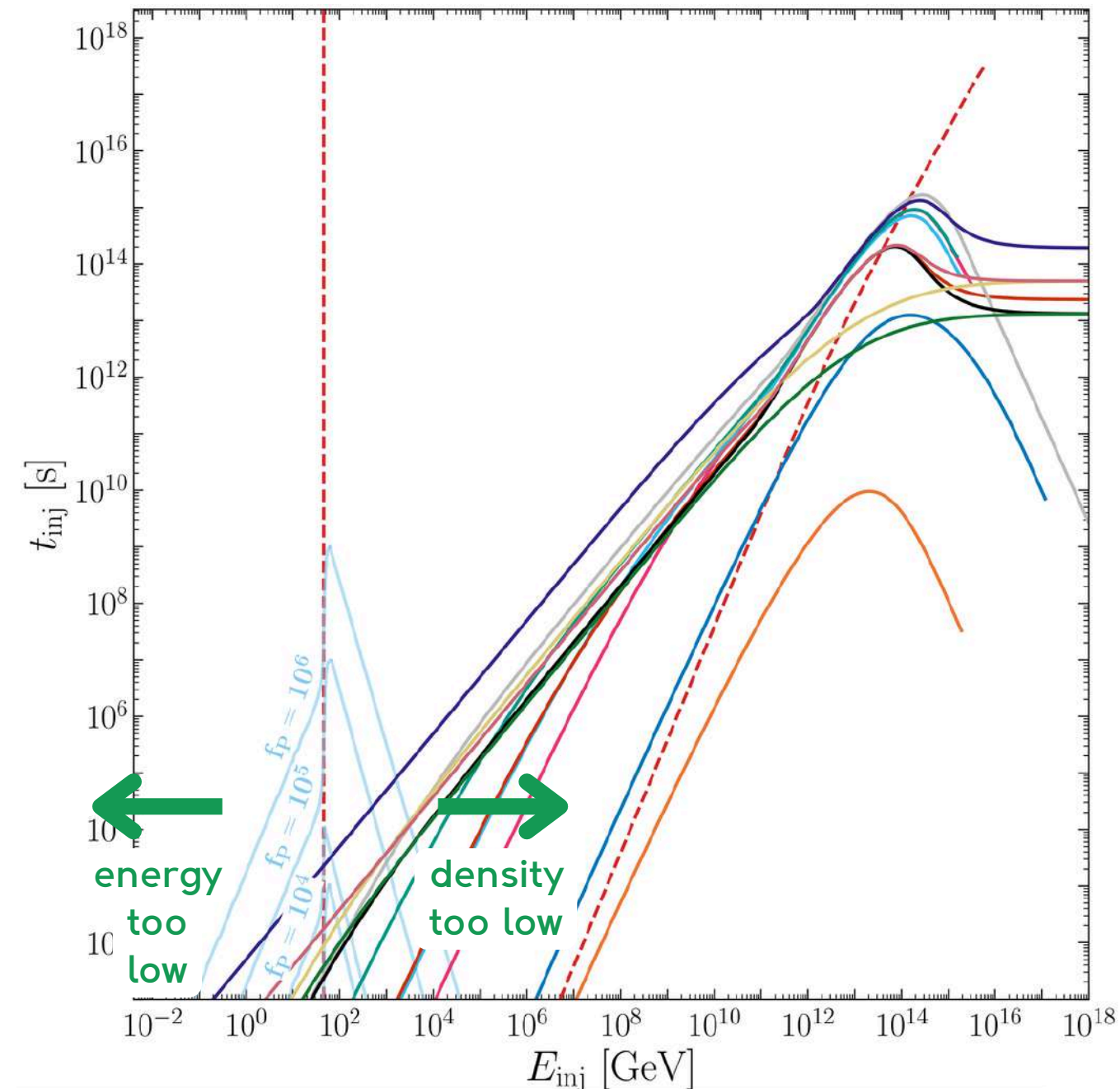


Medium interactions.

$$S_\nu(z_e, E_0) = \int_0^{z_e} \frac{dz}{(1+z)H(z)} \langle \sigma v \rangle n_{\nu BG}$$

Average number of scattering
 Integration over the line of sight
 cross section averaged over target distribution function
 target neutrino number density

$$f = \frac{\Omega_P^0}{\Omega_{DM}^0}$$



Medium interactions.

$$S_\nu(z_e, E_0) = \int_0^{z_e} \frac{dz}{(1+z)H(z)} \langle \sigma v \rangle n_{\nu BG}$$

Average number of scattering

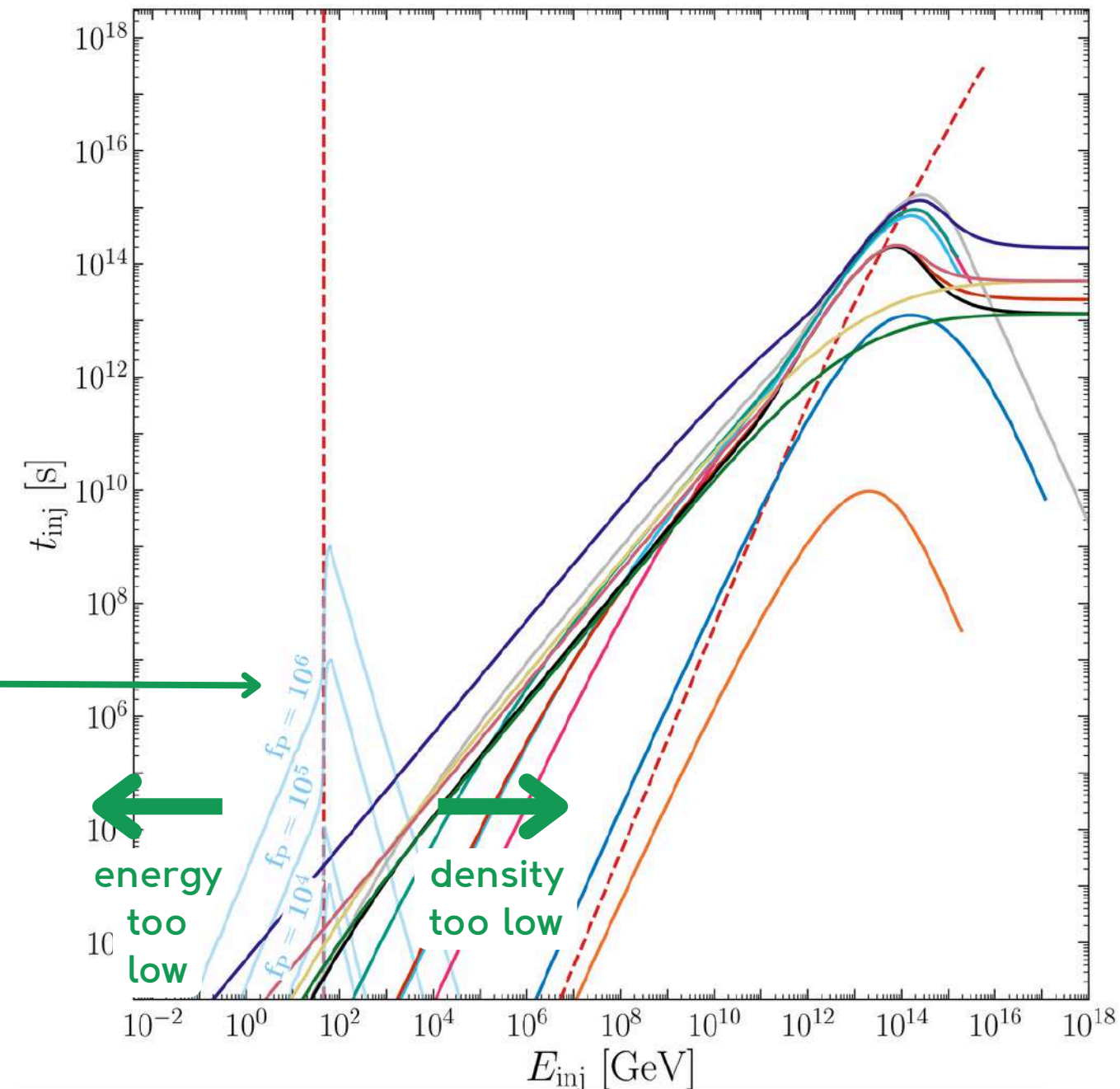
Integration over the line of sight

target neutrino number density

cross section averaged over target distribution function

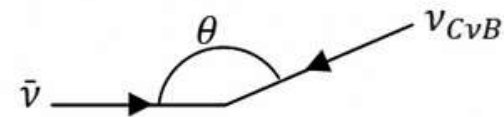
Self-scatterings are negligible except around the Z resonance

$$f = \frac{\Omega_P^0}{\Omega_{DM}^0}$$



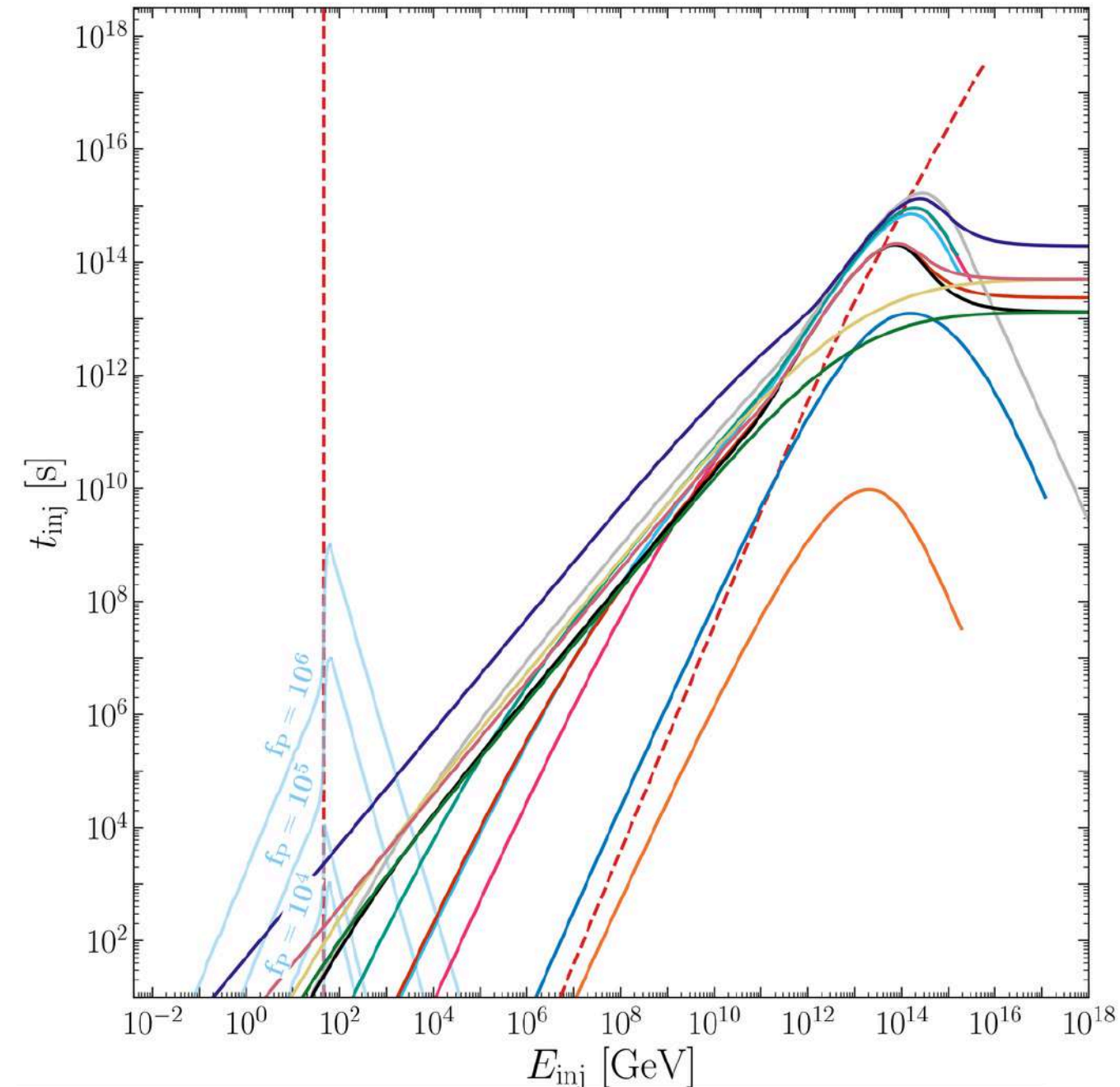
Medium interactions.

$$s = 2E_\nu E_{C\nu B}(1 - \cos(\theta))$$



$$E_\nu^{\text{res}} = \frac{m_Z^2}{4 \cdot 3.15 T_{\nu_{BG}}}$$

- $\nu_e \nu_{BG}^{(-)} \rightarrow \nu_x \nu_y^{(-)(-)}$
- $\nu_e \nu_{BG}^- \rightarrow e^- e^+$
- $\nu_e \nu_{BG}^- \rightarrow \mu^- e^+$
- $\nu_e \nu_{BG}^- \rightarrow e^- \mu^+$
- $\nu_e \nu_{BG}^- \rightarrow \mu^- \mu^+$
- $\nu_e \nu_{BG}^- \rightarrow \pi \pi$
- $\nu_e \nu_{BG}^- \rightarrow K \bar{K}$
- $\nu_e \nu_{BG}^- \rightarrow \tau^- \tau^+$
- $\nu_e \nu_{BG}^- \rightarrow D \bar{D}$
- $\nu_e \nu_{BG}^- \rightarrow B \bar{B}$
- $\nu_e \nu_{BG}^- \rightarrow W^- W^+$
- $\nu_e \nu_{BG}^- \rightarrow t \bar{t}$
- $s = m_Z^2$



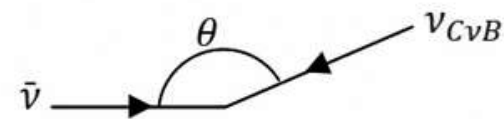
Average number of scattering

Integration over the line of sight

cross section averaged target distribution function

Medium interactions.

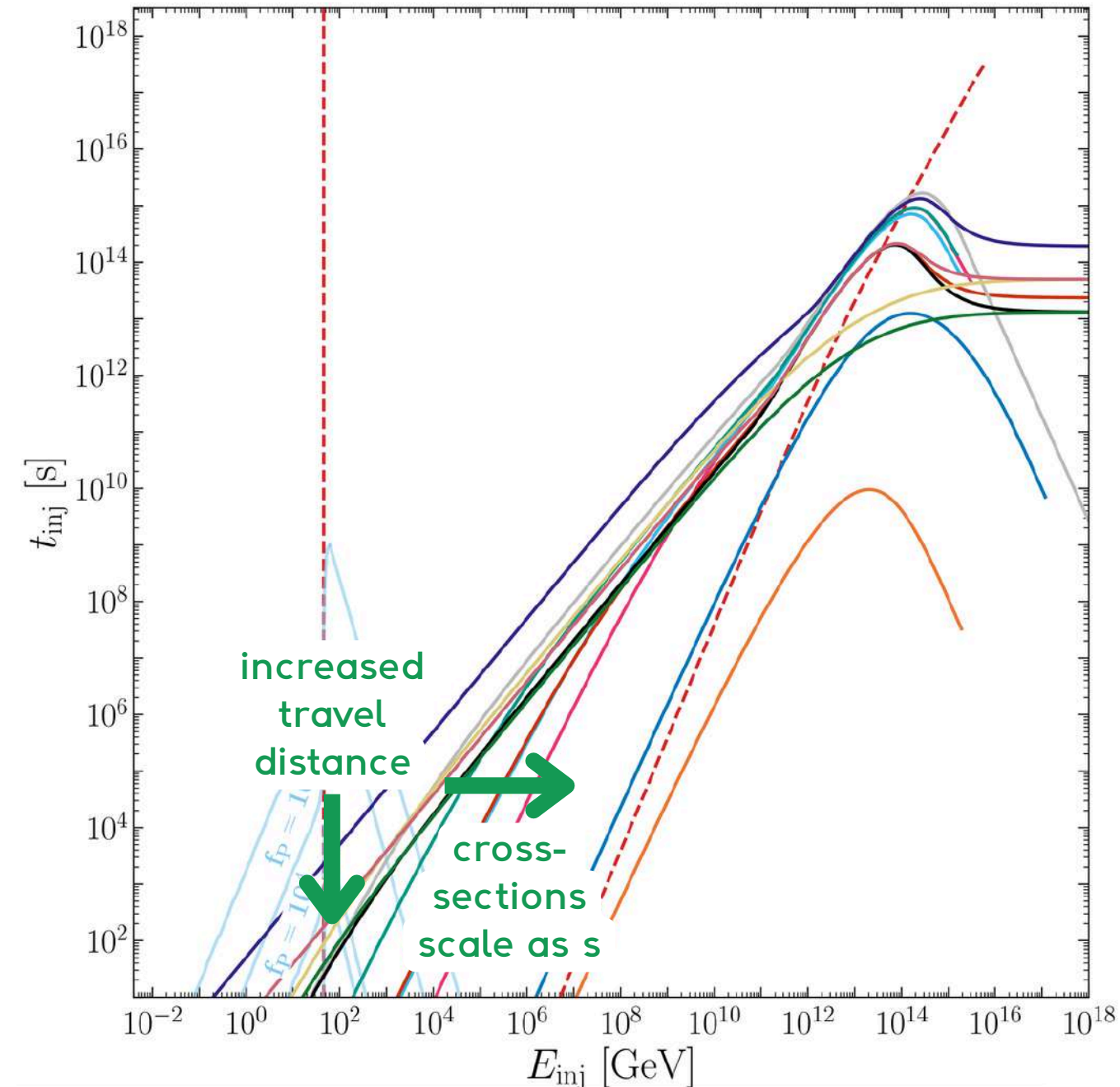
$$s = 2E_\nu E_{C\nu B}(1 - \cos(\theta))$$



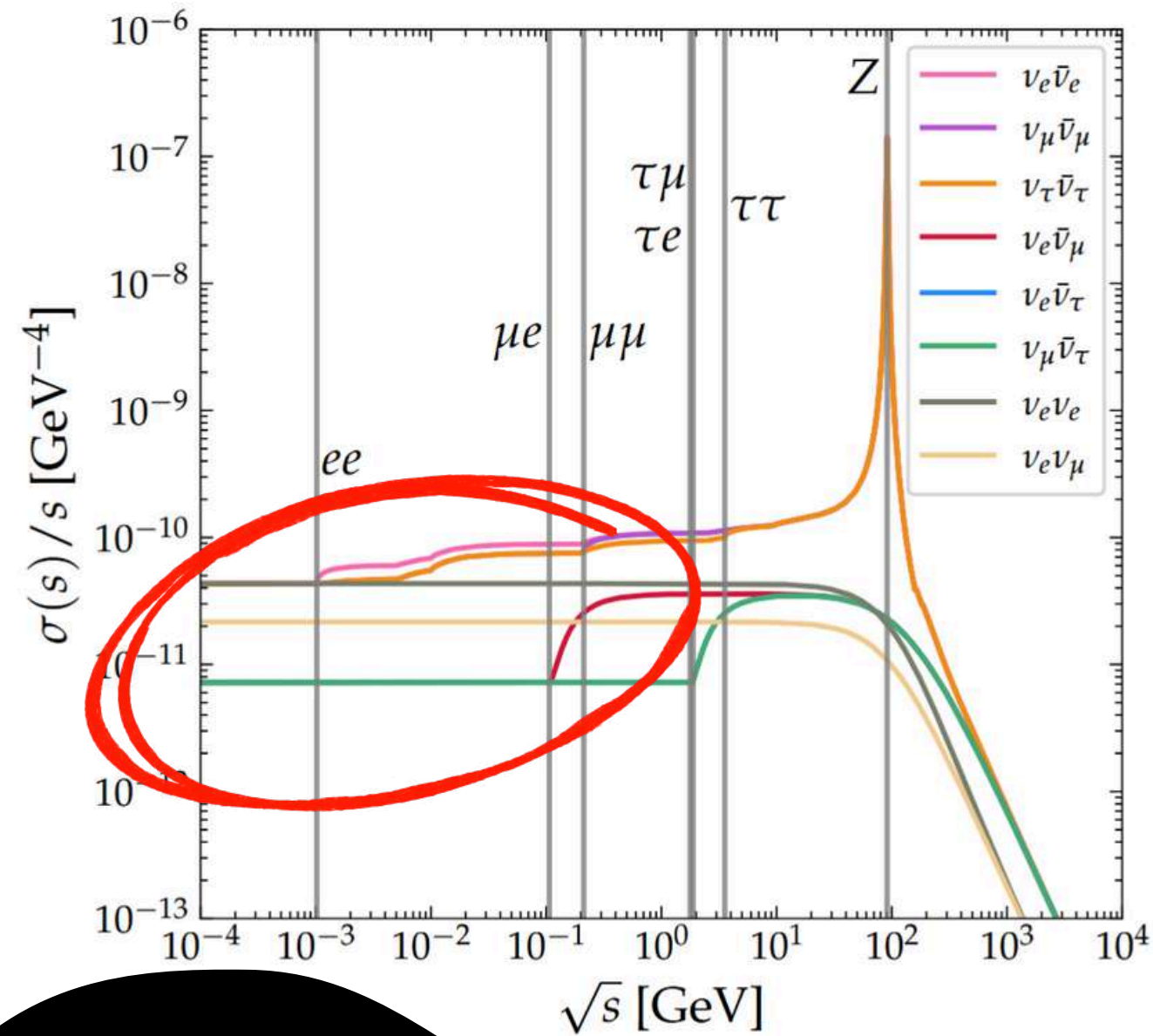
$$E_{inj} \ll \ll E_\nu^{res}$$

$$E_\nu^{res} = \frac{m_Z^2}{4 \cdot 3.15 T_{\nu_{BG}}}$$

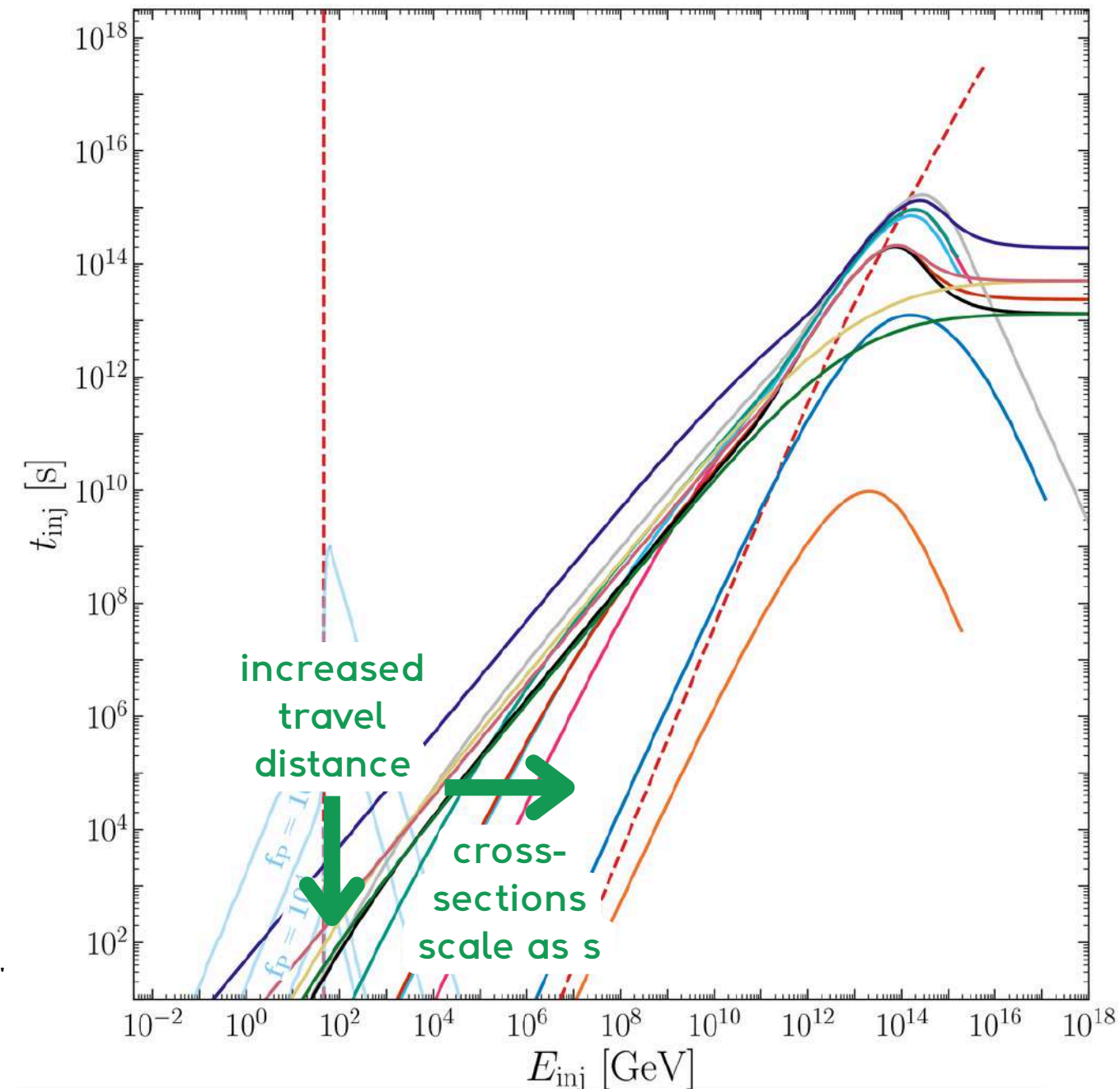
- $\nu_e \nu_{BG}^{(-)} \rightarrow \nu_x \nu_y^{(-)(-)}$
- $\nu_e \nu_{BG}^- \rightarrow e^- e^+$
- $\nu_e \nu_{BG}^- \rightarrow \mu^- e^+$
- $\nu_e \nu_{BG}^- \rightarrow e^- \mu^+$
- $\nu_e \nu_{BG}^- \rightarrow \mu^- \mu^+$
- $\nu_e \nu_{BG}^- \rightarrow \pi \pi$
- $\nu_e \nu_{BG}^- \rightarrow K \bar{K}$
- $\nu_e \nu_{BG}^- \rightarrow \tau^- \tau^+$
- $\nu_e \nu_{BG}^- \rightarrow D \bar{D}$
- $\nu_e \nu_{BG}^- \rightarrow B \bar{B}$
- $\nu_e \nu_{BG}^- \rightarrow W^- W^+$
- $\nu_e \nu_{BG}^- \rightarrow t \bar{t}$
- $s = m_Z^2$



Medium interactions.



Bianco, Depta, Frerick, Hambye, Hufnagel, Schmidt-Hoberg 25'

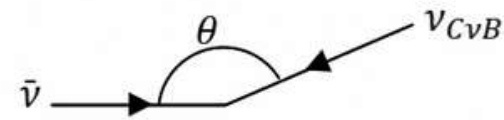


$S_\nu(z_i)$
 Average num
 of scatterin

ν_{BG}
 trino

Medium interactions.

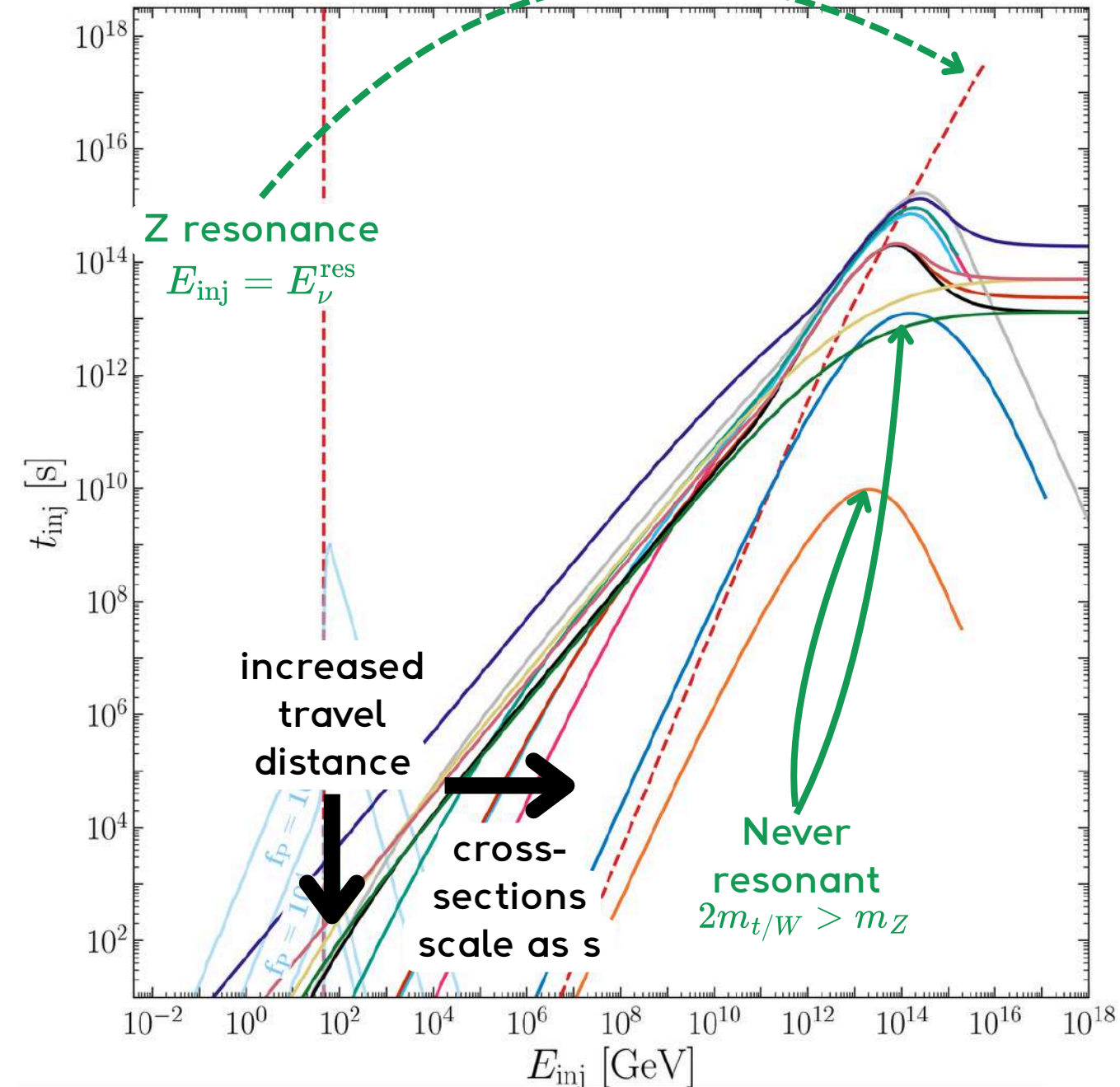
$$s = 2E_\nu E_{C\nu B}(1 - \cos(\theta))$$



$$E_{inj} \sim E_\nu^{res}$$

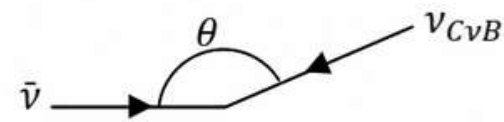
$$E_\nu^{res} = \frac{m_Z^2}{4 \cdot 3.15 T_{\nu_{BG}}}$$

- $\nu_e \nu_{BG}^{(-)} \rightarrow \nu_x \nu_y^{(-)(-)}$
- $\nu_e \nu_{BG}^- \rightarrow e^- e^+$
- $\nu_e \nu_{BG}^- \rightarrow \mu^- e^+$
- $\nu_e \nu_{BG}^- \rightarrow e^- \mu^+$
- $\nu_e \nu_{BG}^- \rightarrow \mu^- \mu^+$
- $\nu_e \nu_{BG}^- \rightarrow \pi \pi$
- $\nu_e \nu_{BG}^- \rightarrow K \bar{K}$
- $\nu_e \nu_{BG}^- \rightarrow \tau^- \tau^+$
- $\nu_e \nu_{BG}^- \rightarrow D \bar{D}$
- $\nu_e \nu_{BG}^- \rightarrow B \bar{B}$
- $\nu_e \nu_{BG}^- \rightarrow W^- W^+$
- $\nu_e \nu_{BG}^- \rightarrow t \bar{t}$
- $s = m_Z^2$



Medium interactions.

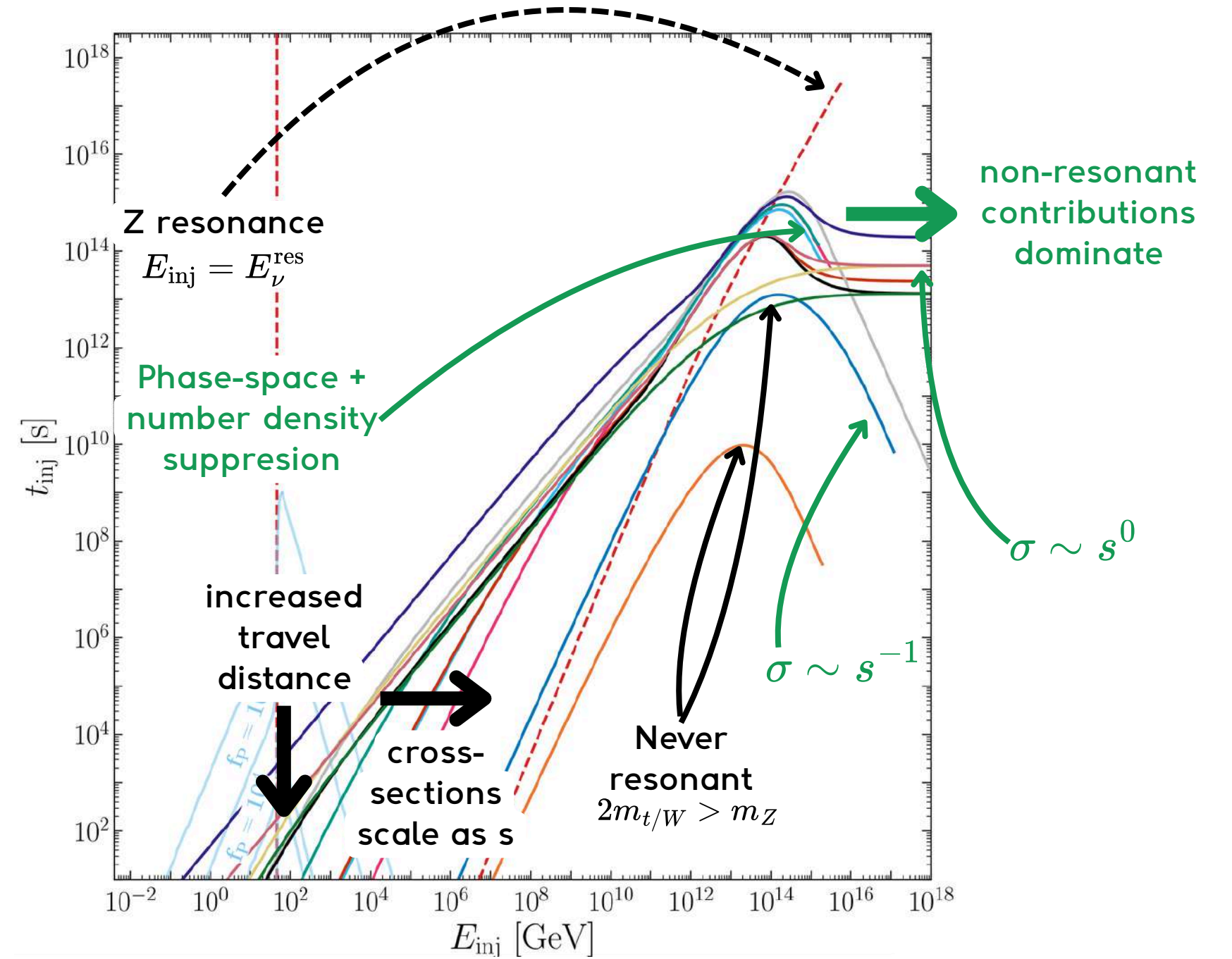
$$s = 2E_\nu E_{C\nu B}(1 - \cos(\theta))$$



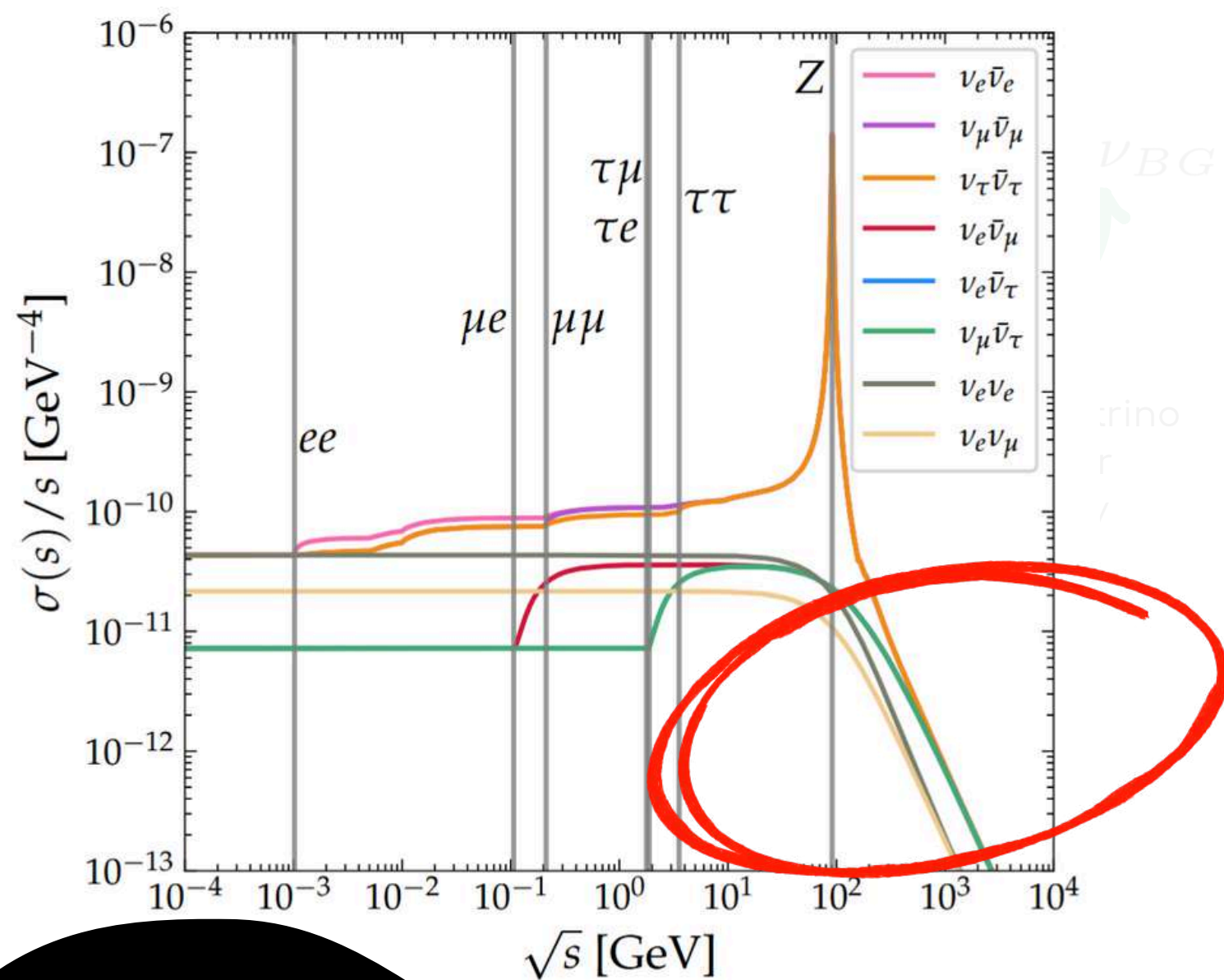
$$E_{inj} \gg \gg E_\nu^{res}$$

$$E_\nu^{res} = \frac{m_Z^2}{4 \cdot 3.15 T_{\nu_{BG}}}$$

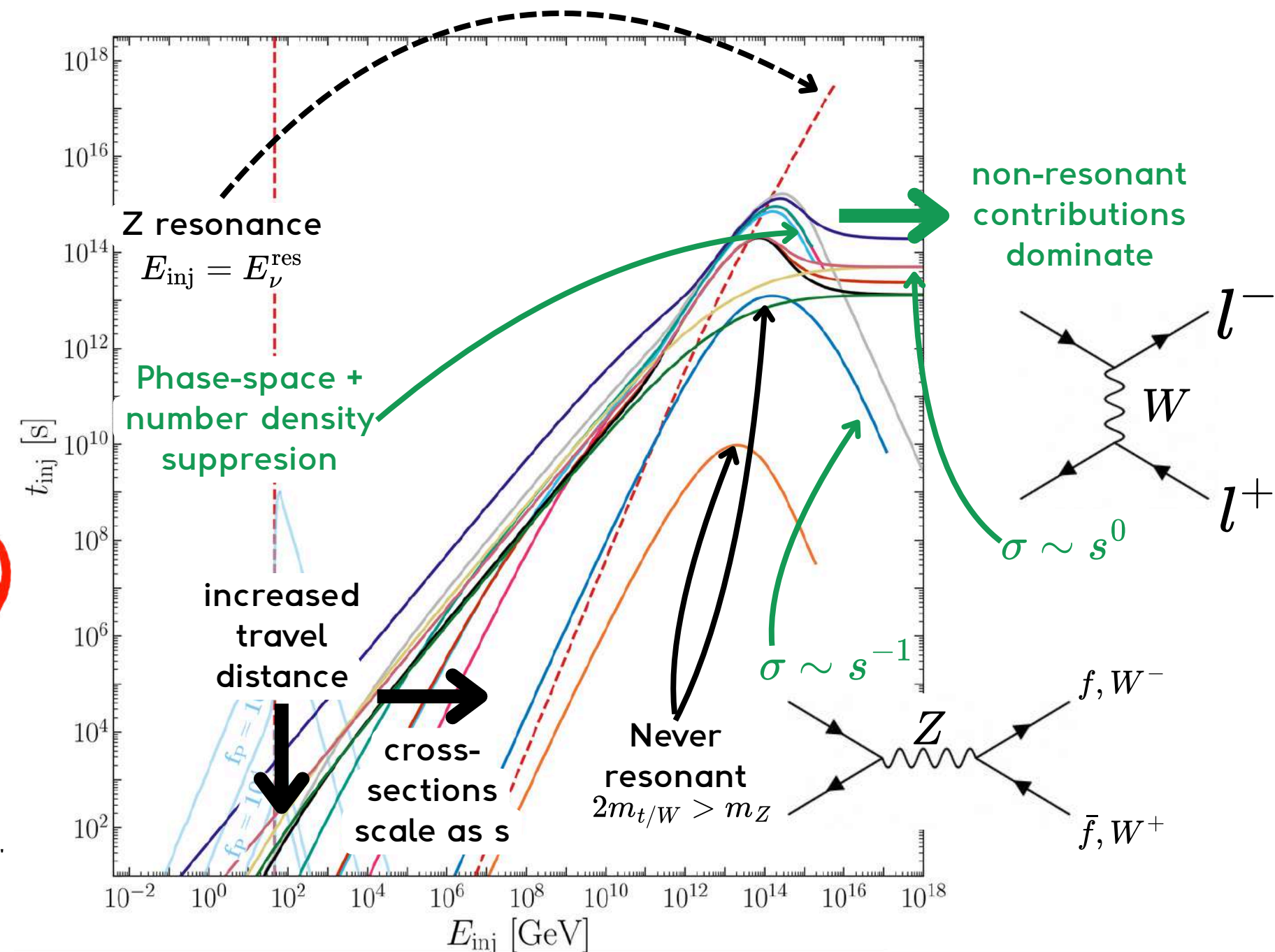
- $\nu_e \nu_{BG} \rightarrow \nu_x \nu_y$
- $\nu_e \nu_{BG} \rightarrow e^- e^+$
- $\nu_e \nu_{BG} \rightarrow \mu^- e^+$
- $\nu_e \nu_{BG} \rightarrow e^- \mu^+$
- $\nu_e \nu_{BG} \rightarrow \mu^- \mu^+$
- $\nu_e \nu_{BG} \rightarrow \pi \pi$
- $\nu_e \nu_{BG} \rightarrow K \bar{K}$
- $\nu_e \nu_{BG} \rightarrow \tau^- \tau^+$
- $\nu_e \nu_{BG} \rightarrow D \bar{D}$
- $\nu_e \nu_{BG} \rightarrow B \bar{B}$
- $\nu_e \nu_{BG} \rightarrow W^- W^+$
- $\nu_e \nu_{BG} \rightarrow t \bar{t}$
- - - $s = m_Z^2$



Medium interactions.



Bianco, Depta, Frerick, Hambye, Hufnagel, Schmidt-Hoberg 25'

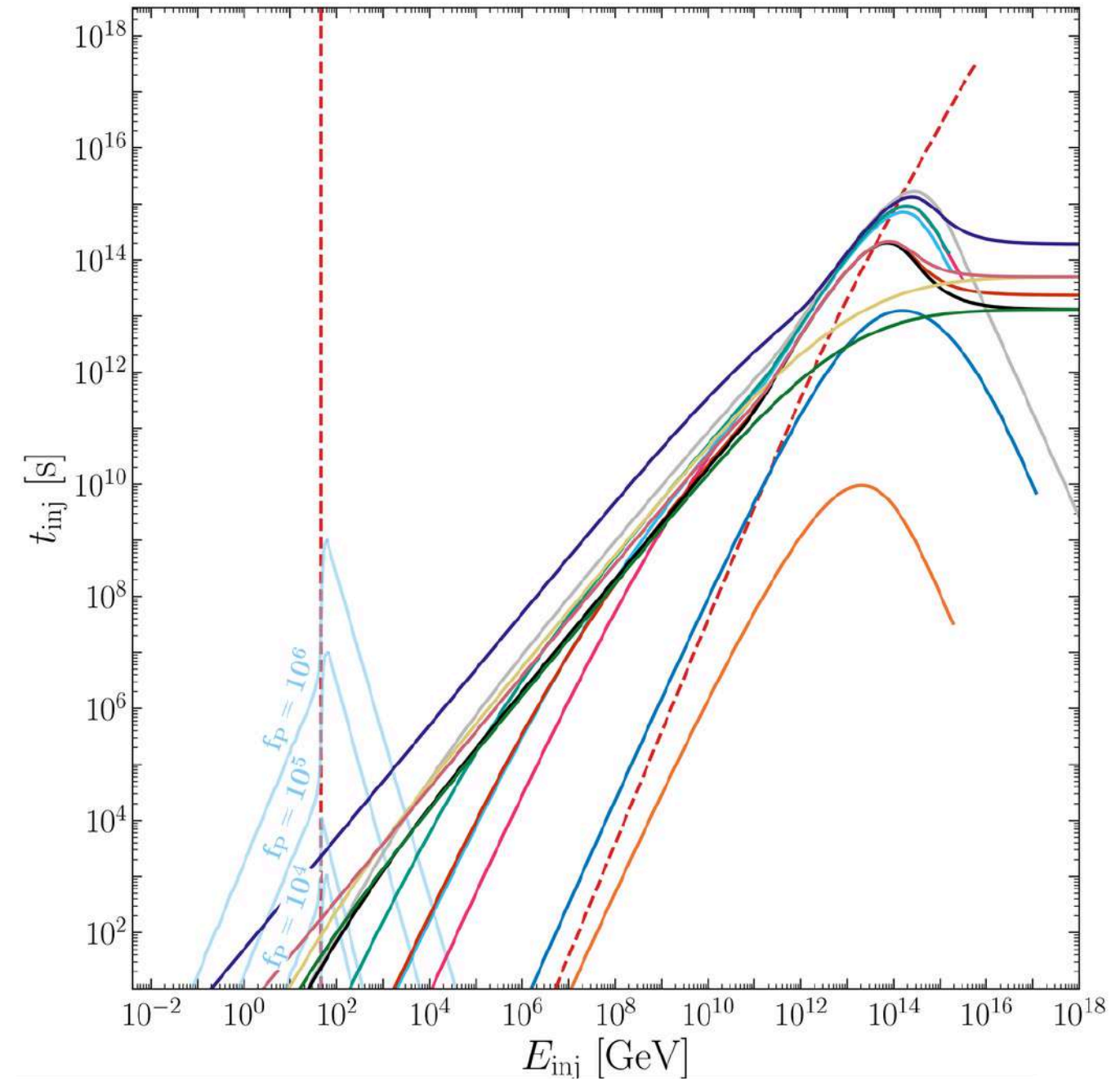


Medium interactions.

$S_\nu(z_e, E_0) = \int_0^{z_e} \frac{dz}{(1+z)I}$

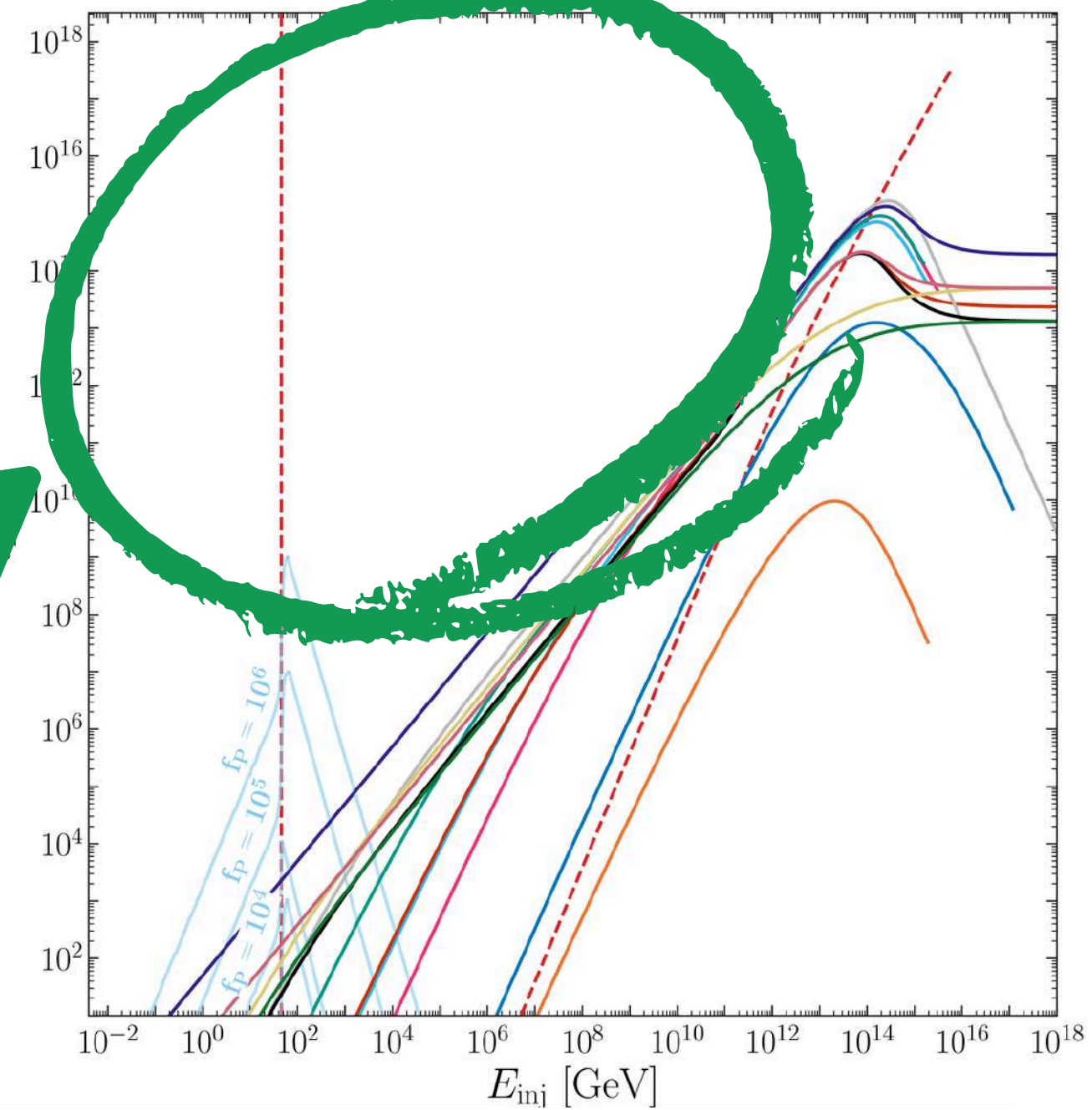
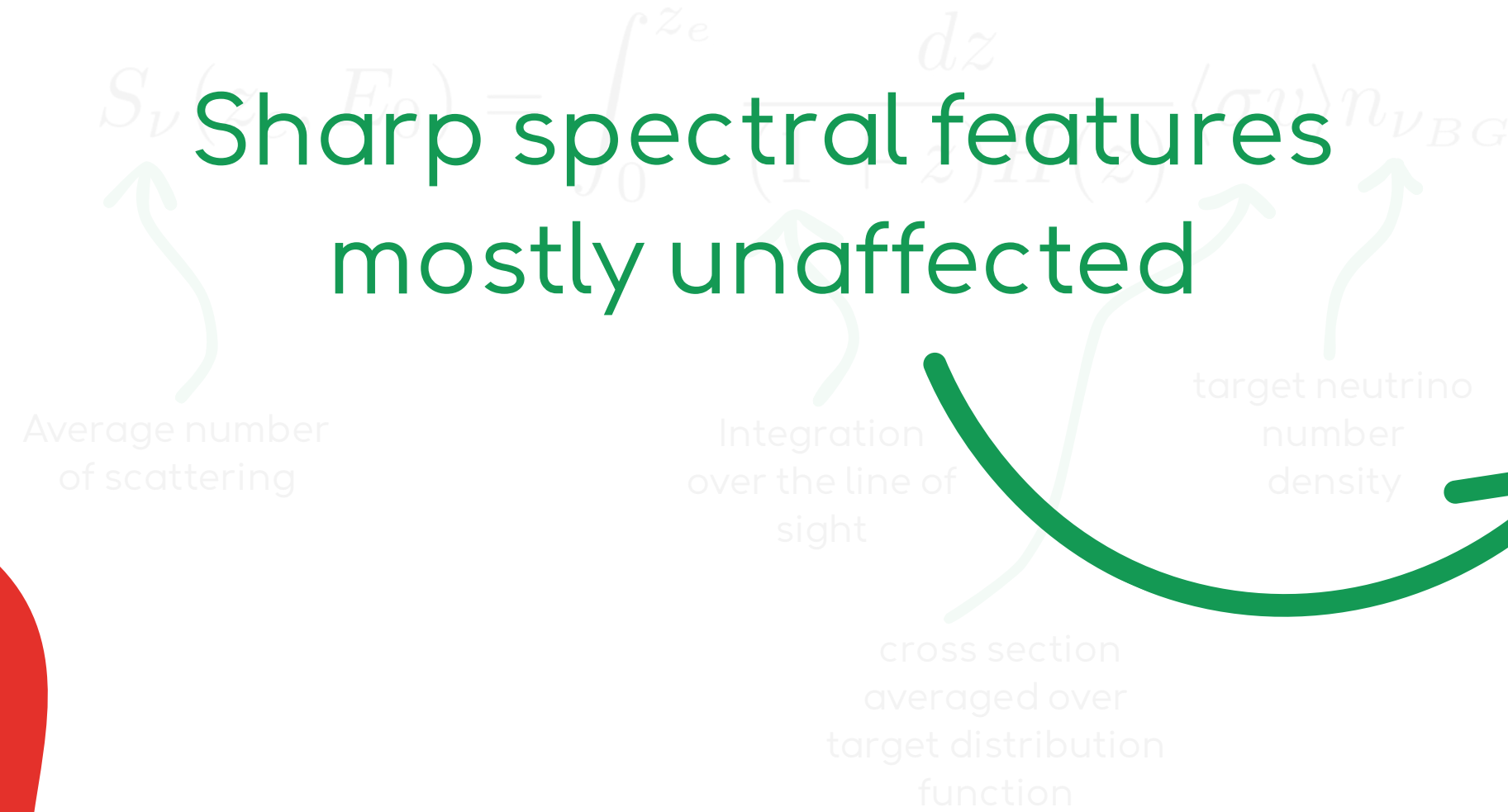
Average number of scattering
 Integration over the line of sight
 cross section averaged over target distribution function

- $\nu_e \nu_{BG}^{(-)} \rightarrow \nu_x \nu_y^{(-)(-)}$
- $\nu_e \nu_{BG}^- \rightarrow e^- e^+$
- $\nu_e \nu_{BG}^- \rightarrow \mu^- e^+$
- $\nu_e \nu_{BG}^- \rightarrow e^- \mu^+$
- $\nu_e \nu_{BG}^- \rightarrow \mu^- \mu^+$
- $\nu_e \nu_{BG}^- \rightarrow \pi \pi$
- $\nu_e \nu_{BG}^- \rightarrow K \bar{K}$
- $\nu_e \nu_{BG}^- \rightarrow \tau^- \tau^+$
- $\nu_e \nu_{BG}^- \rightarrow D \bar{D}$
- $\nu_e \nu_{BG}^- \rightarrow B \bar{B}$
- $\nu_e \nu_{BG}^- \rightarrow W^- W^+$
- $\nu_e \nu_{BG}^- \rightarrow t \bar{t}$
- $s = m_Z^2$

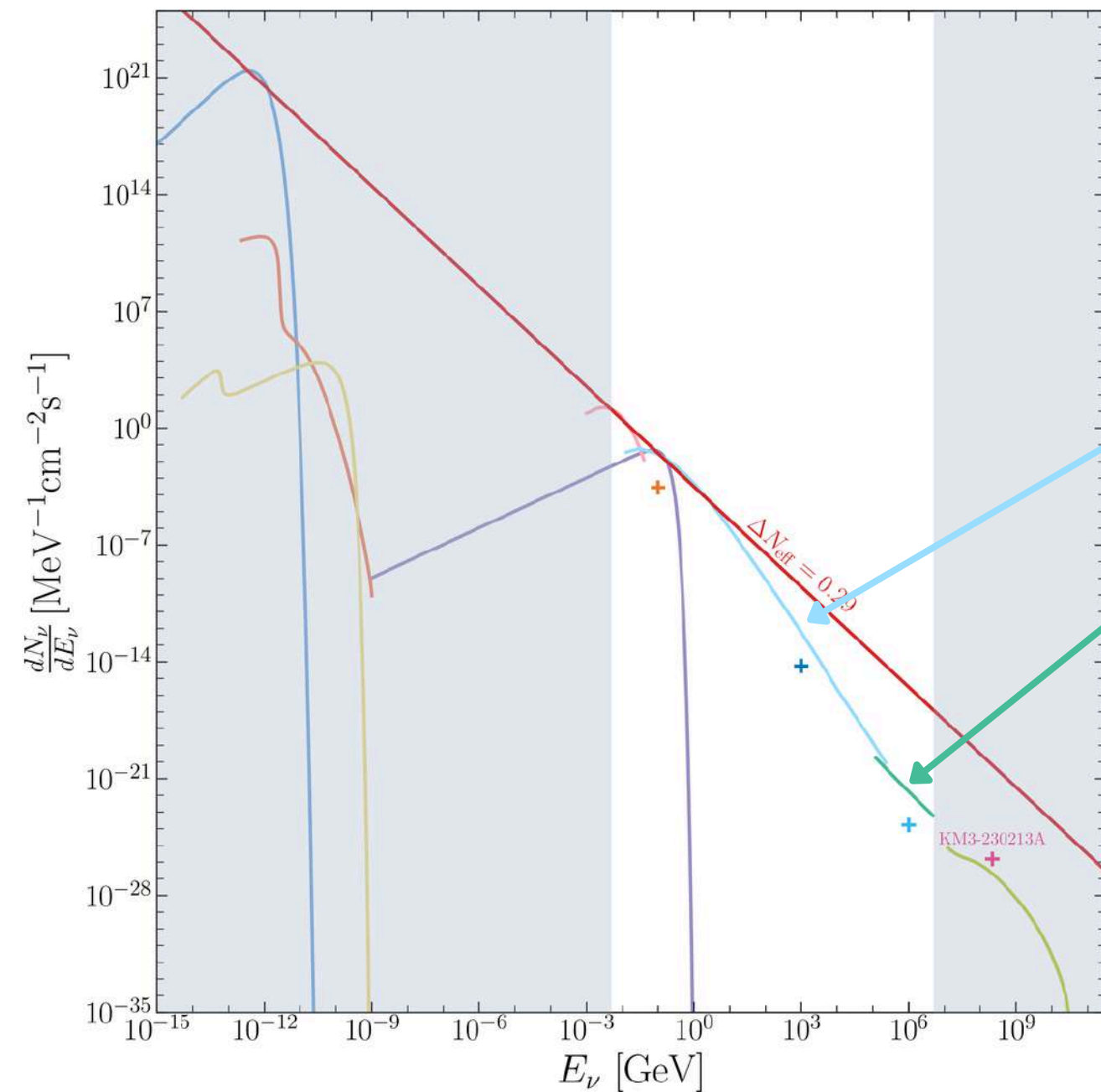


Medium interactions.

Sharp spectral features mostly unaffected



Constraints.

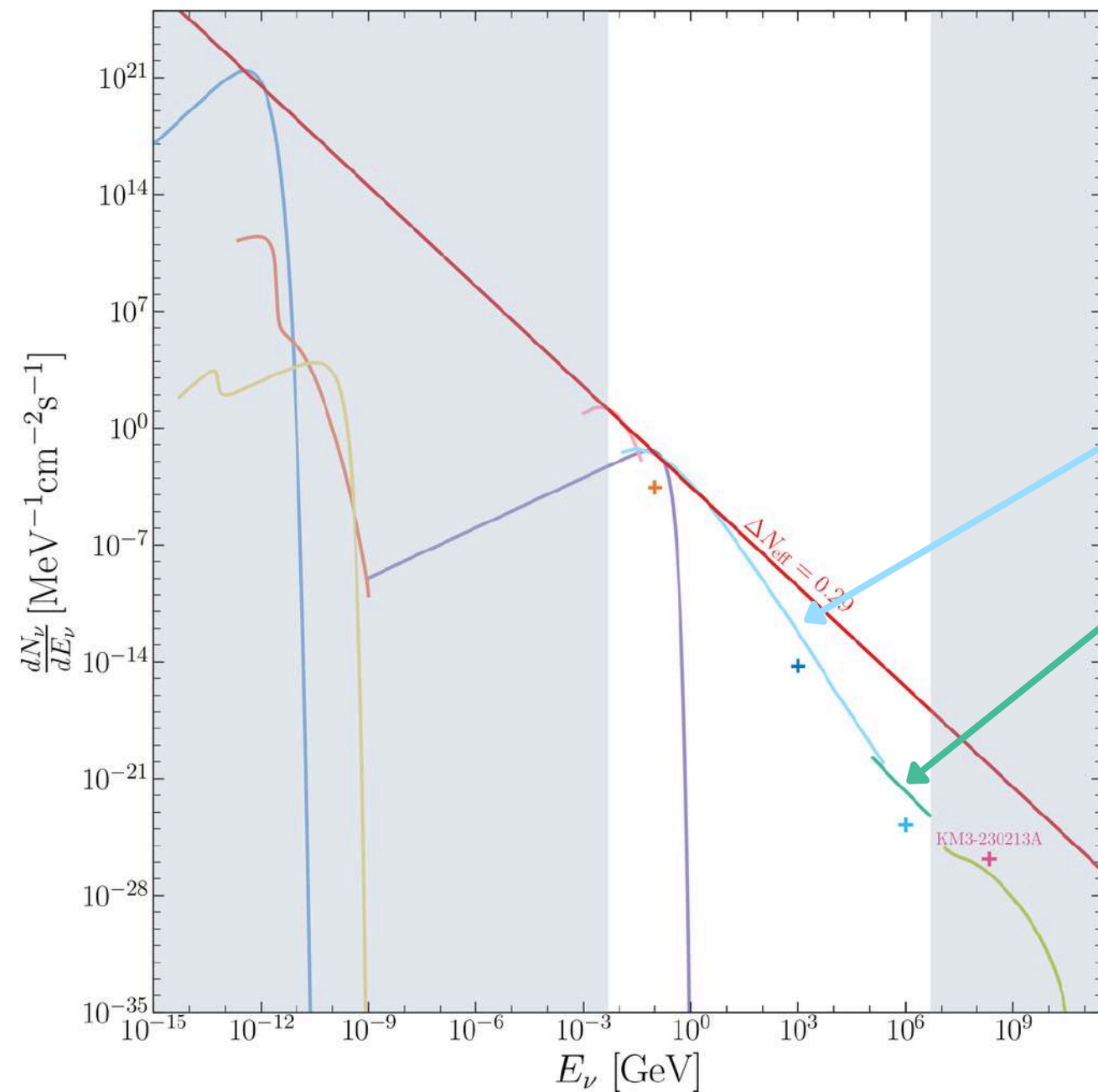


Vitagliano, Tamborra, Raffelt 19'

Observational:

- Atmospheric flux (SuperKamiokande, Icecube) > 50 MeV
- Astrophysical flux (Icecube) < 5 PeV
- DSNB > 5 MeV (Soon)

Constraints.



Vitagliano, Tamborra, Raffelt 19'

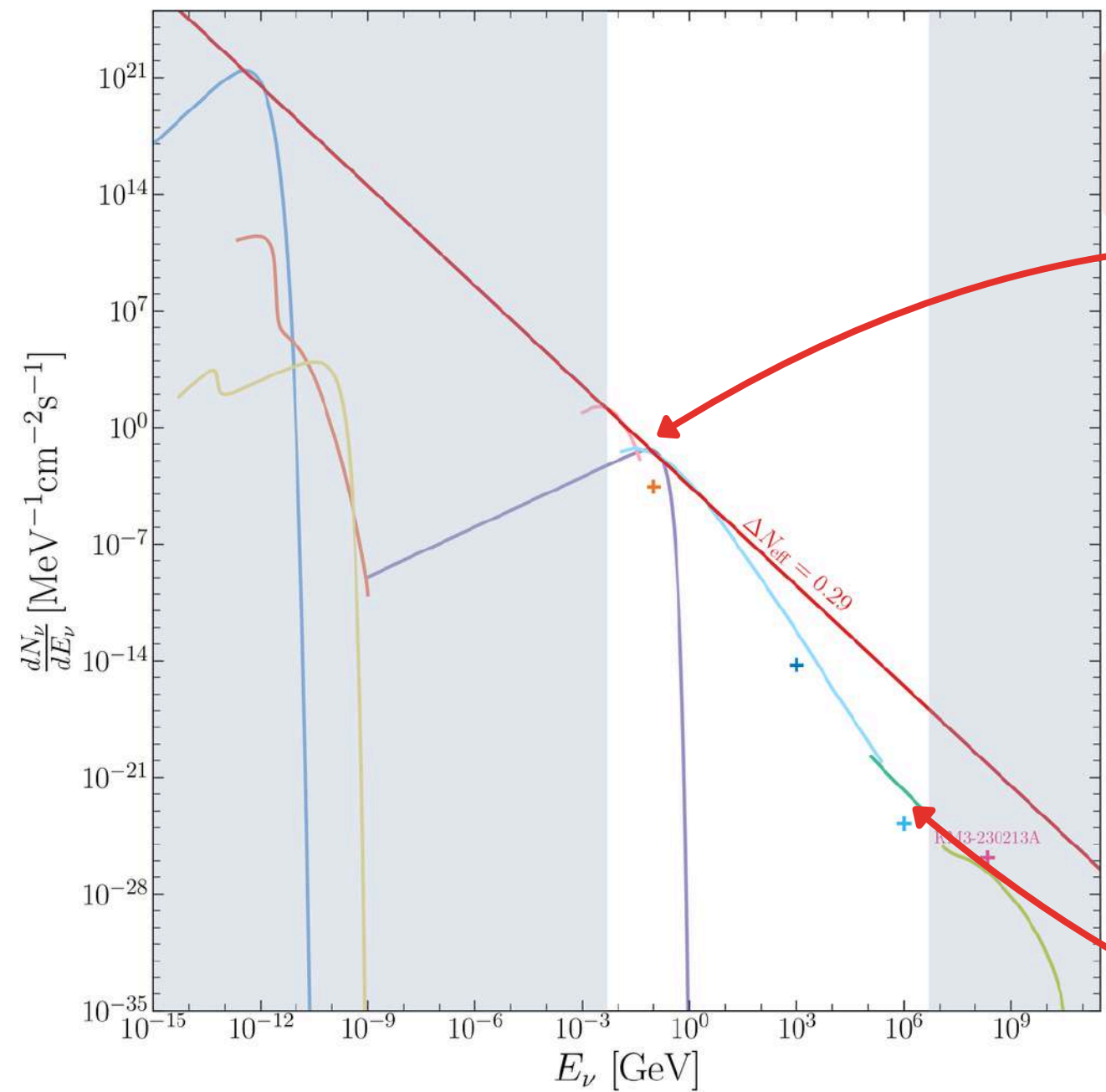
Observational:

- Atmospheric flux (SuperKamiokande, Icecube) > 50 MeV
- Astrophysical flux (Icecube) < 5 PeV
- DSNB > 5 MeV (Soon)

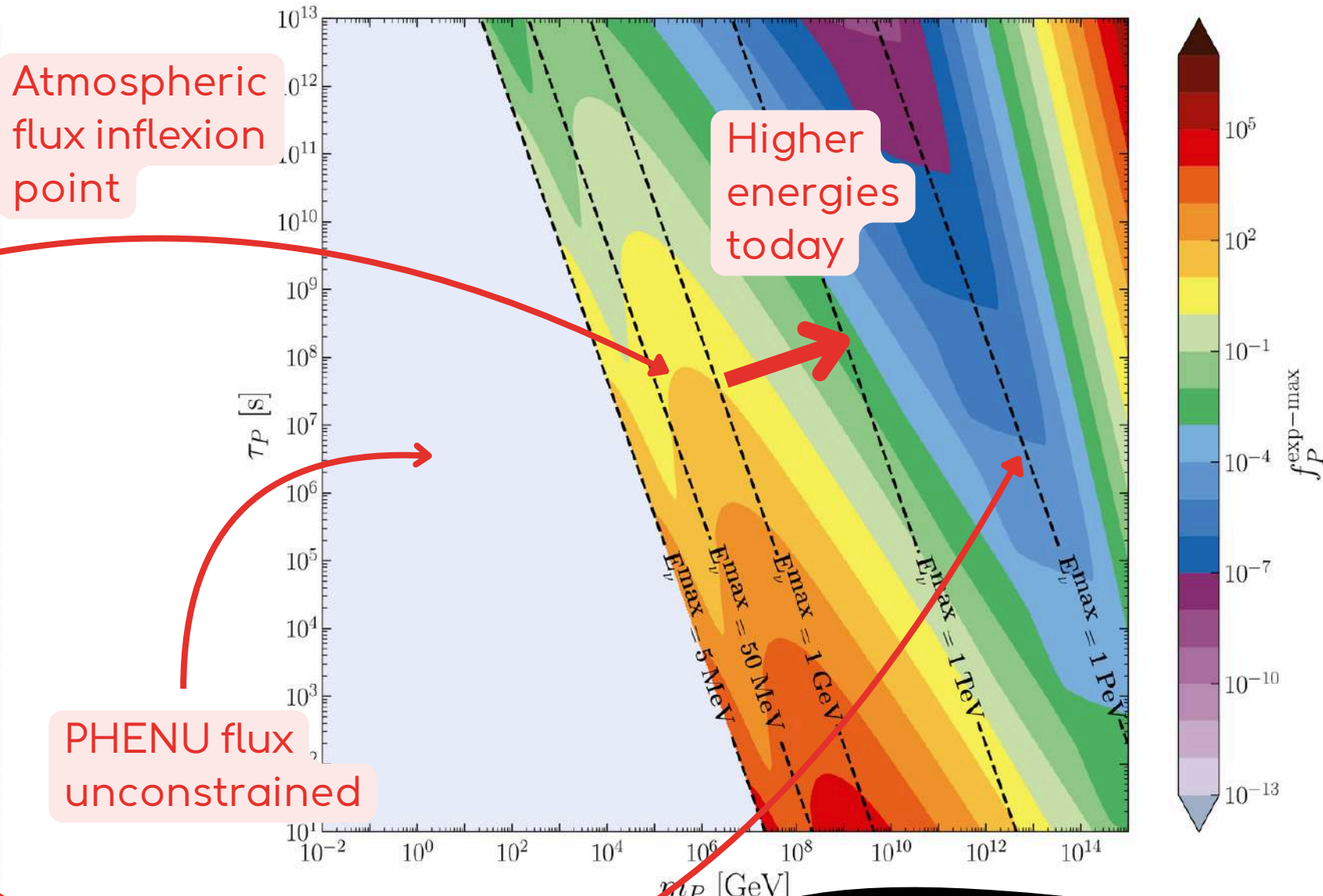
PHENU flux must be at most of the value of the observed flux

→ Upper bound on f

Constraints.



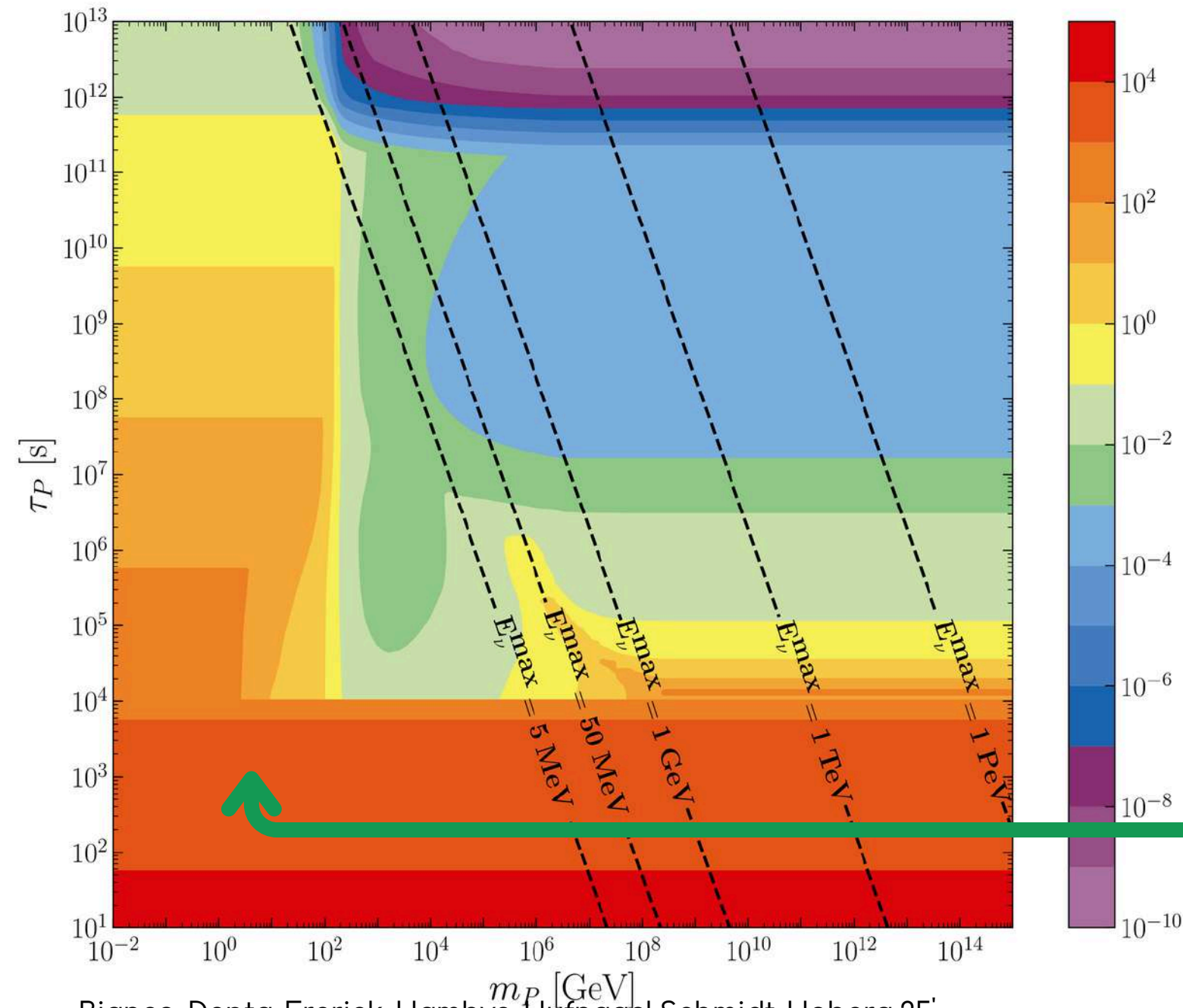
Vitagliano, Tamborra, Raffelt 19'



$$\frac{dN^{\text{PHENU}}}{dE} \propto E^{-2}$$

$$\frac{dN^{\text{Astro}}}{dE} \propto E^{-2}$$

Constraints



Bianco, Depta, Frerick, Hambye, Hufnagel, Schmidt-Hoberg 25'
 Hambye, Hufnagel, Lucca, 21'
 Acharya, Khatri, 19'

Cosmological:

Pl18[TT,TE,EE+lowE]	Λ CDM+ N_{eff}	$2.92^{+0.36}_{-0.37}$
		Planck '18

N_{eff} bound on additional neutrino energy density

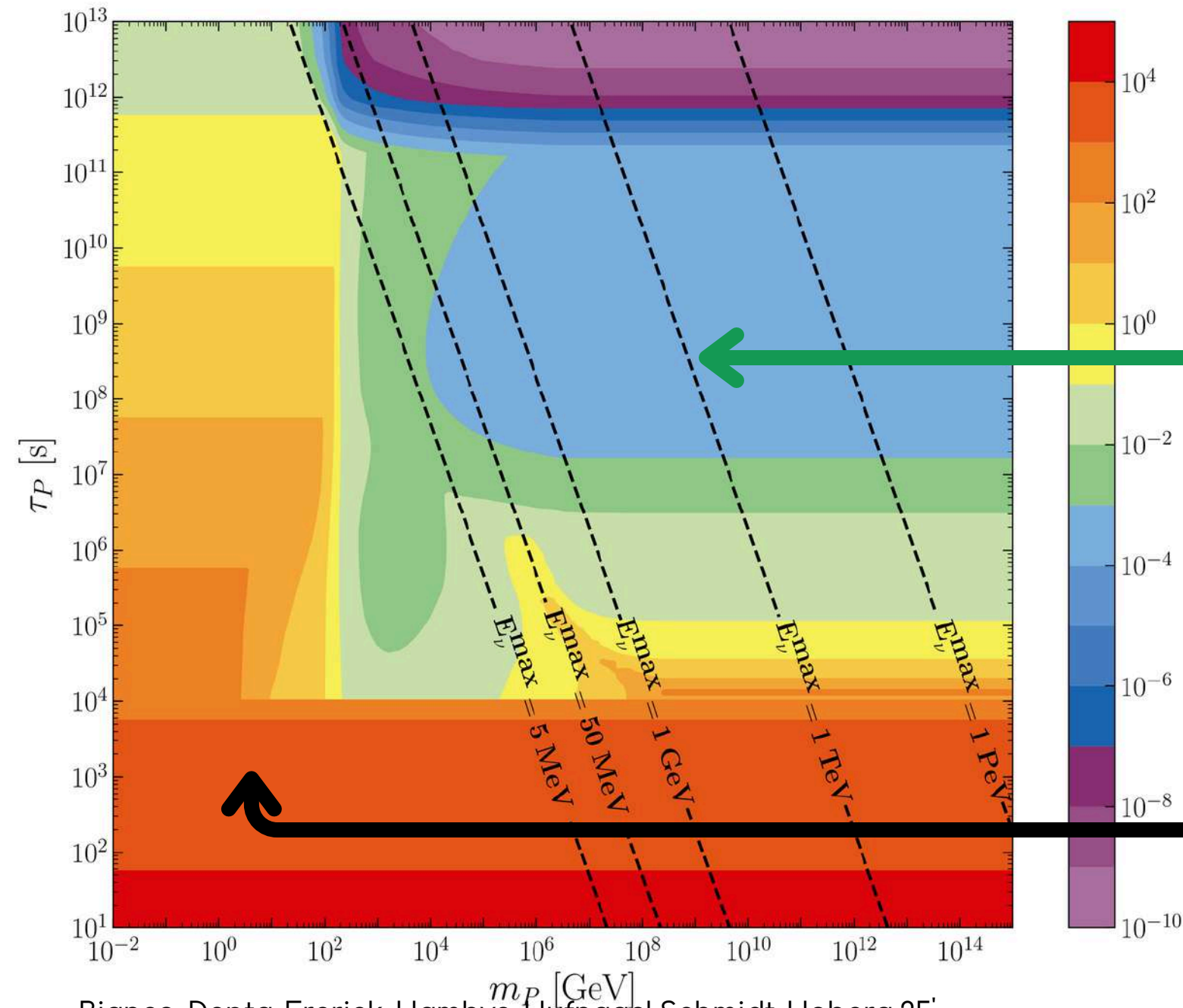
$$N_{\text{eff}}^{\text{SM}} \equiv \frac{8}{7} \left(\frac{11}{4} \right)^{4/3} \left(\frac{\rho_\nu}{\rho_\gamma} \right)$$

$$= 3.0432(2) \simeq 3.043$$

Cielo, Escudero, Mangano, Pisanti '23

Constraints

Cosmological:

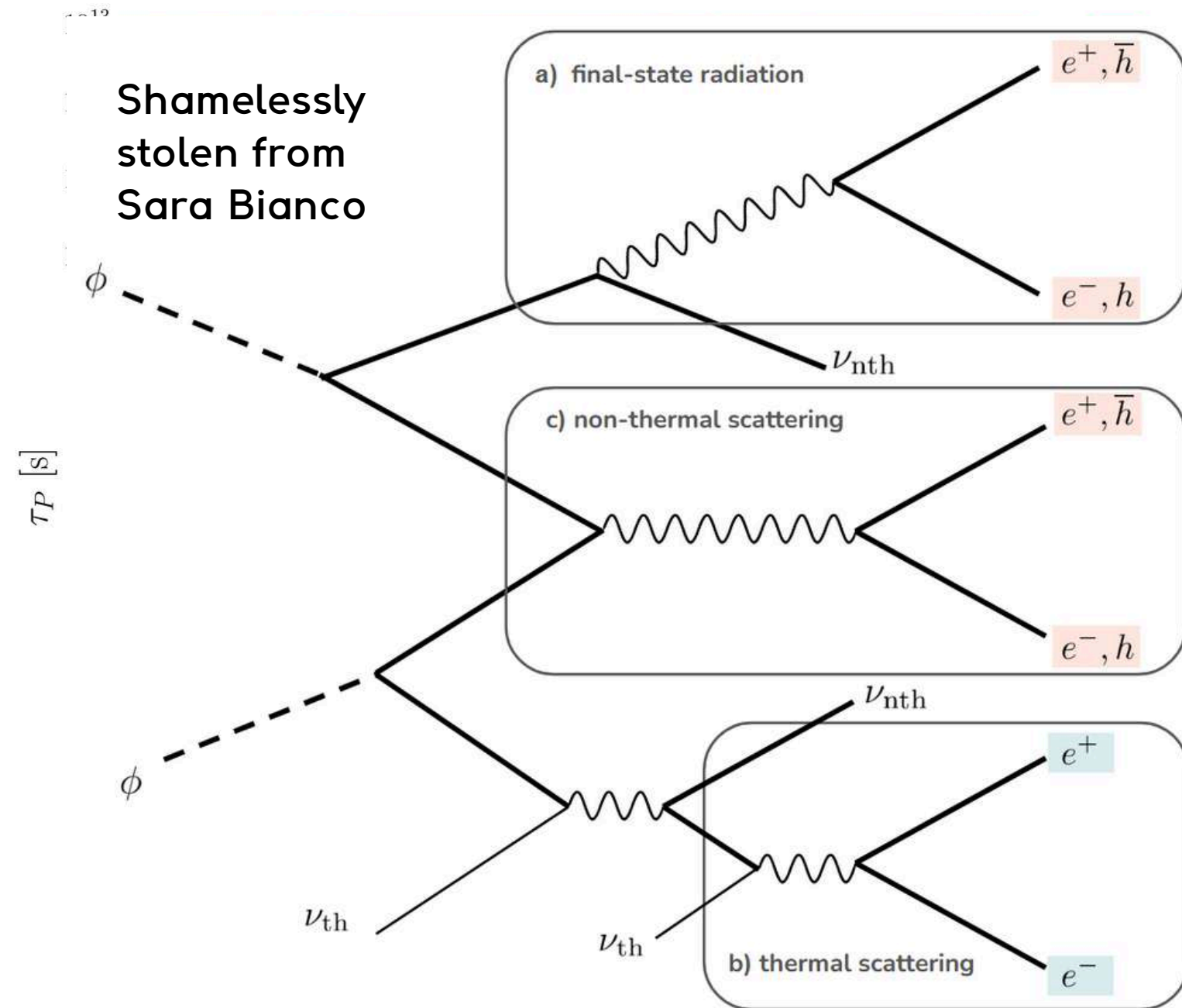


BBN bound from photo and hadro disintegration of light elements

N_{eff} bound on additional neutrino energy density

Bianco, Depta, Frerick, Hambye, Hufnagel, Schmidt-Hoberg 25'
 Hambye, Hufnagel, Lucca, 21'
 Acharya, Khatri, 19'

Constraints.



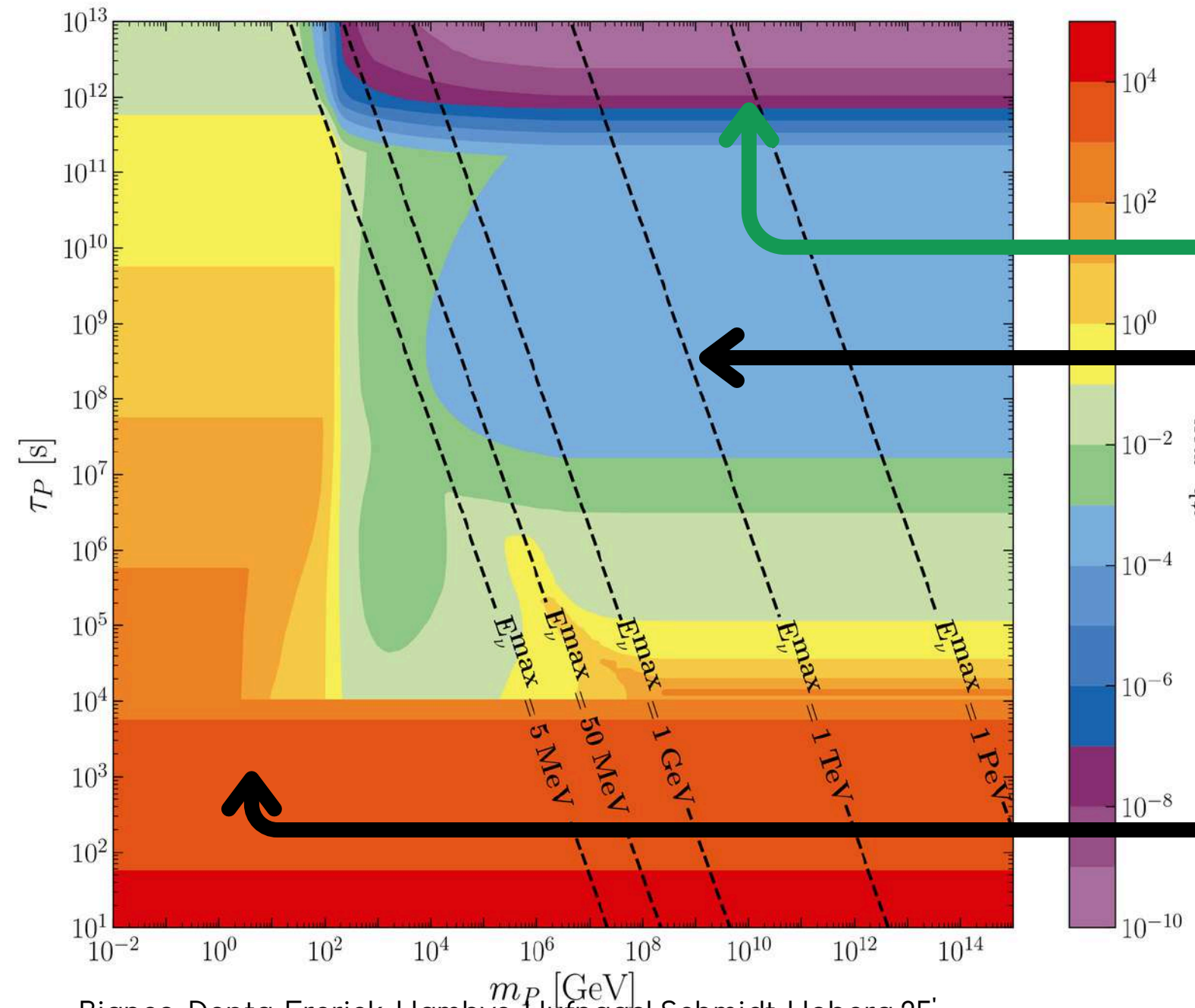
Cosmological:

BBN bound from photo and hadro disintegration of light elements

N_{eff} bound on additional neutrino energy density

Bianco, Depta, Frerick, Hambye, Hufnagel, Schmidt-Hoberg 25'
 Hambye, Hufnagel, Lucca, 21'
 Acharya, Khatri, 19'

Constraints



Cosmological:

CMB anisotropies bound

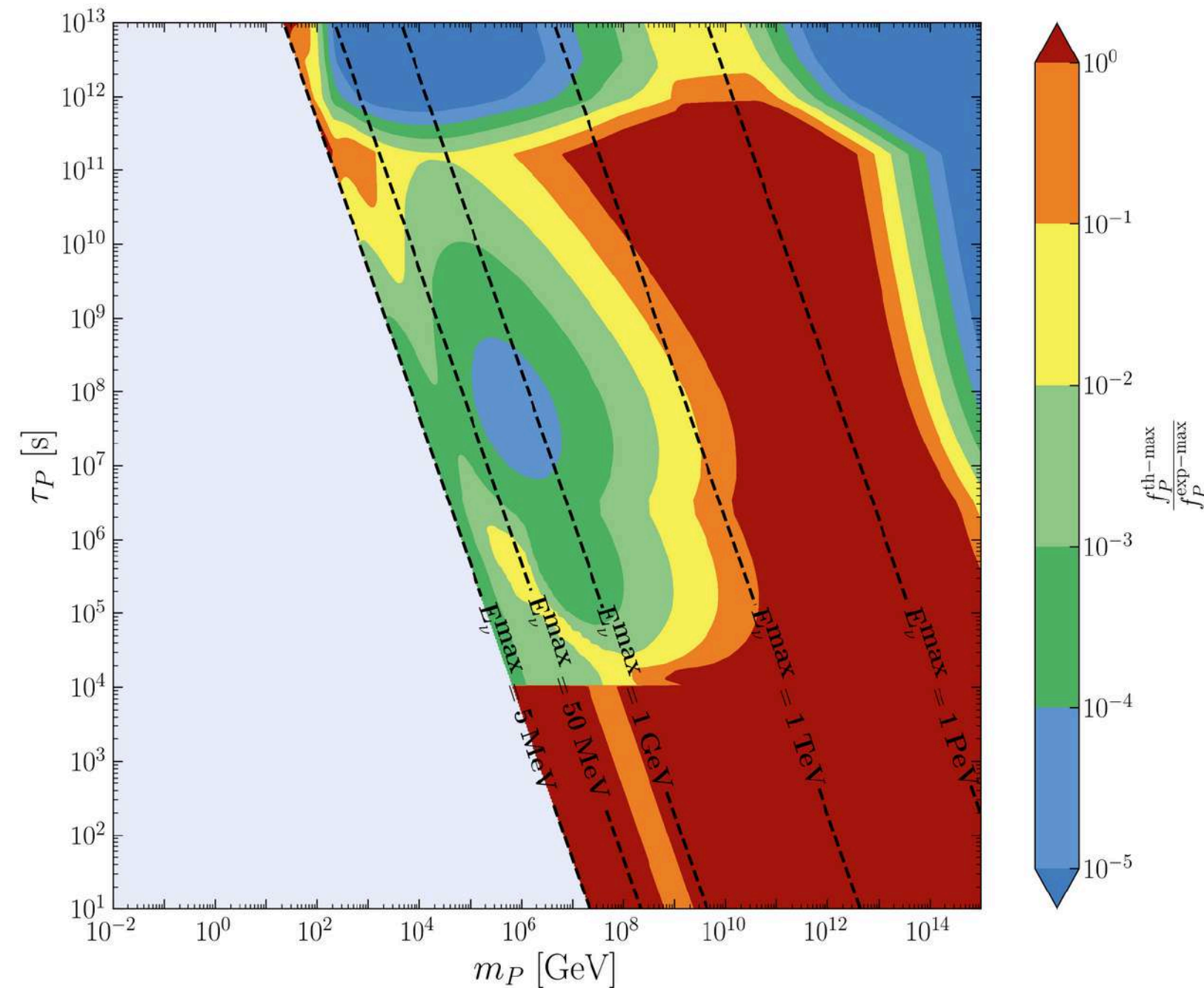
BBN bound from photo and hadro disintegration of light elements

N_{eff} bound on additional neutrino energy density

Competing bounds
with observations

Bianco, Depta, Frerick, Hambye, Hufnagel, Schmidt-Hoberg 25'
 Hambye, Hufnagel, Lucca, 21'
 Acharya, Khatri, 19'

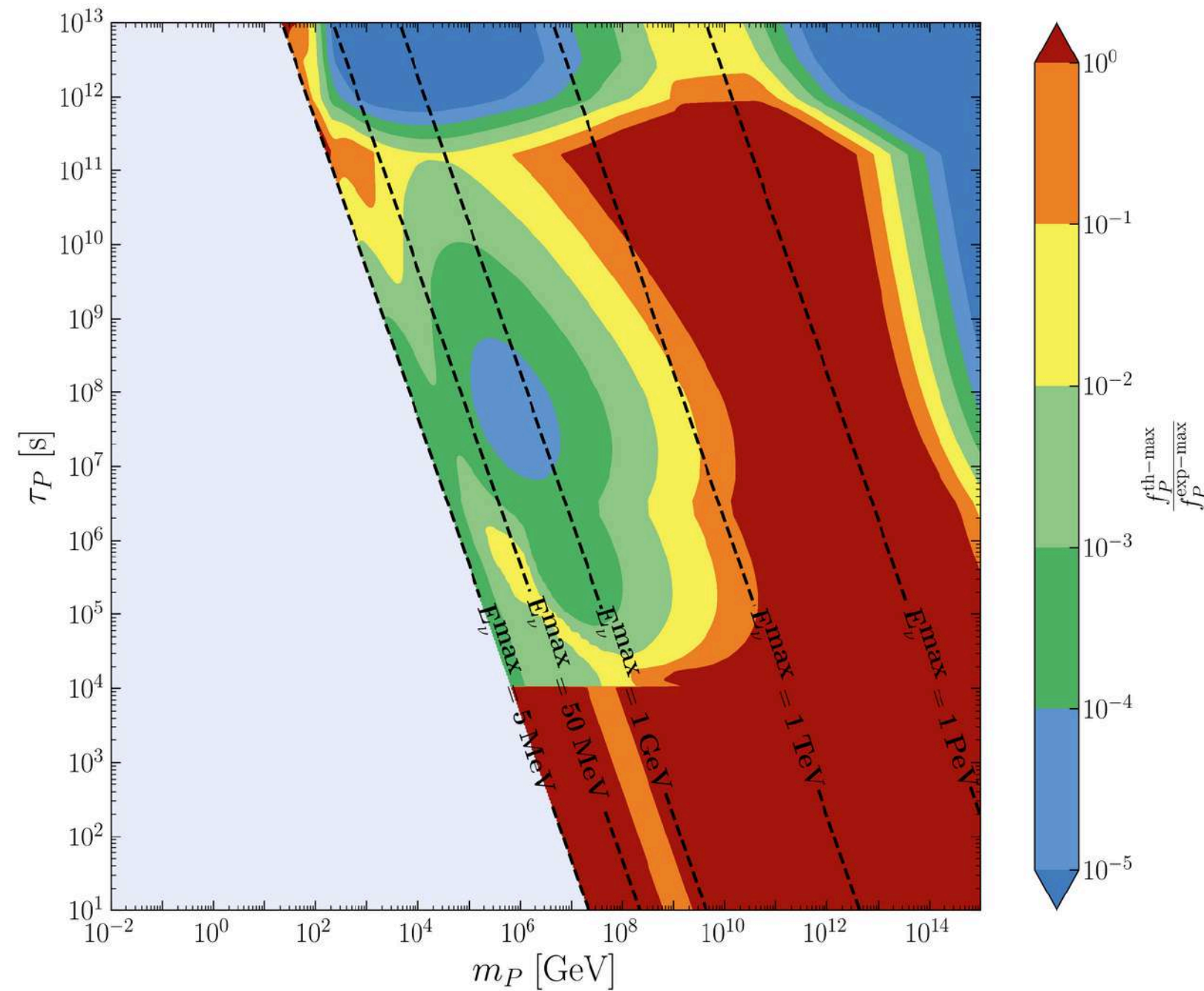
Constraints .



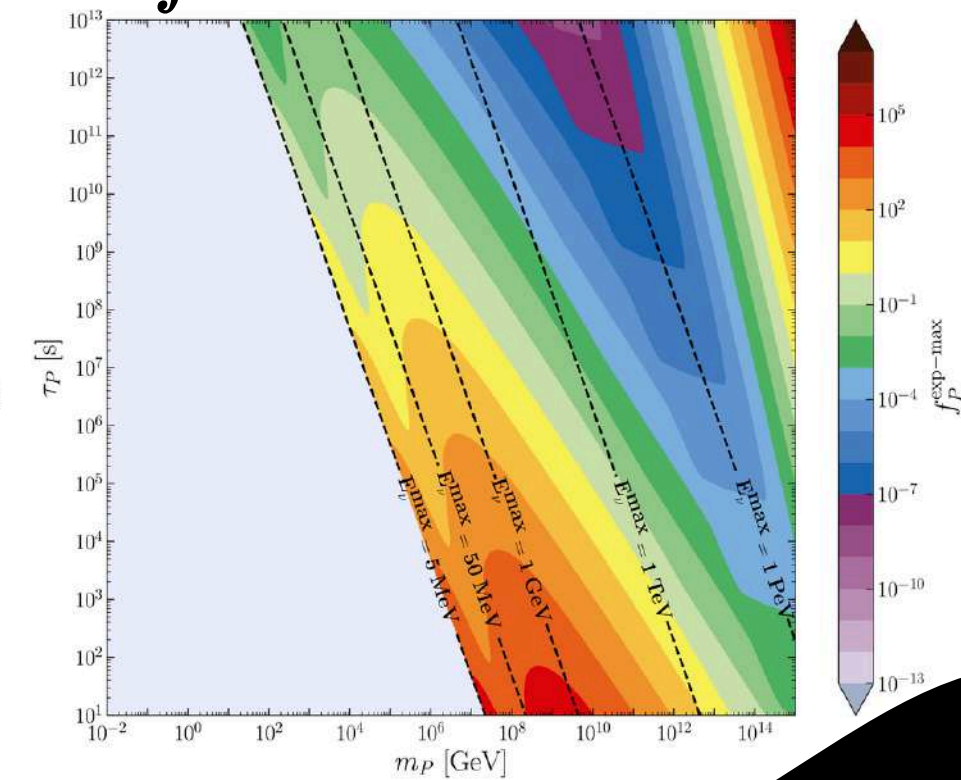
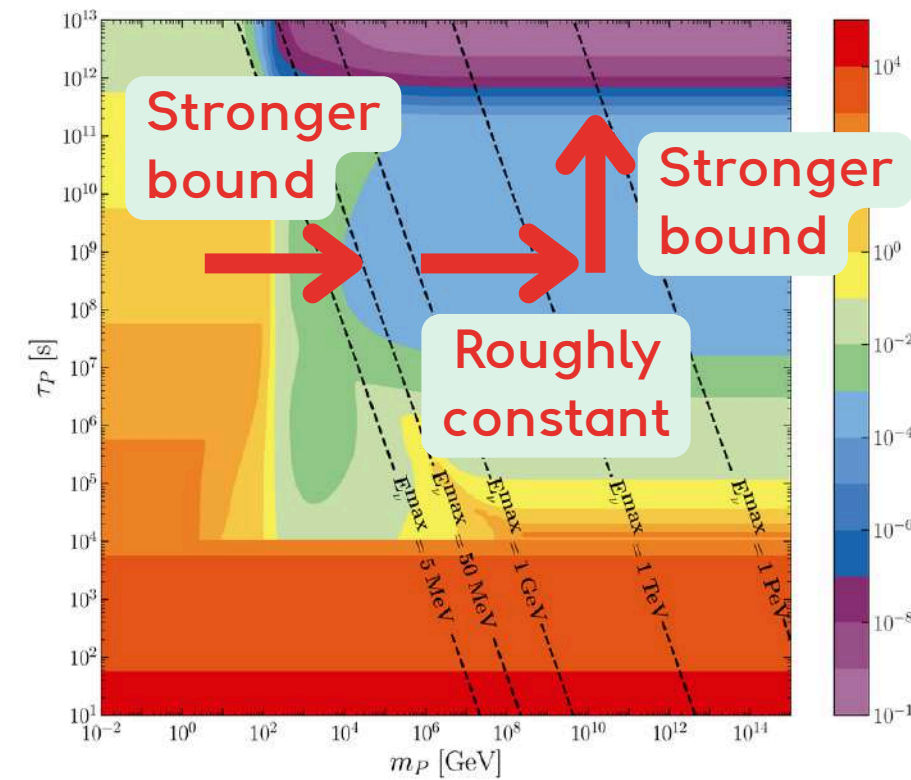
Combination: $\frac{f^{\text{cosmo}}}{f^{\text{obs}}}$

- Ratio > 1 : Unconstrained by theoretical bounds
- Ratio $> 10^{-2}$: Potentially **observable today**
- Ratio $< 10^{-2}$: Signal too weak to be observed
- Ratio $< 10^{-5}$: Hopeless

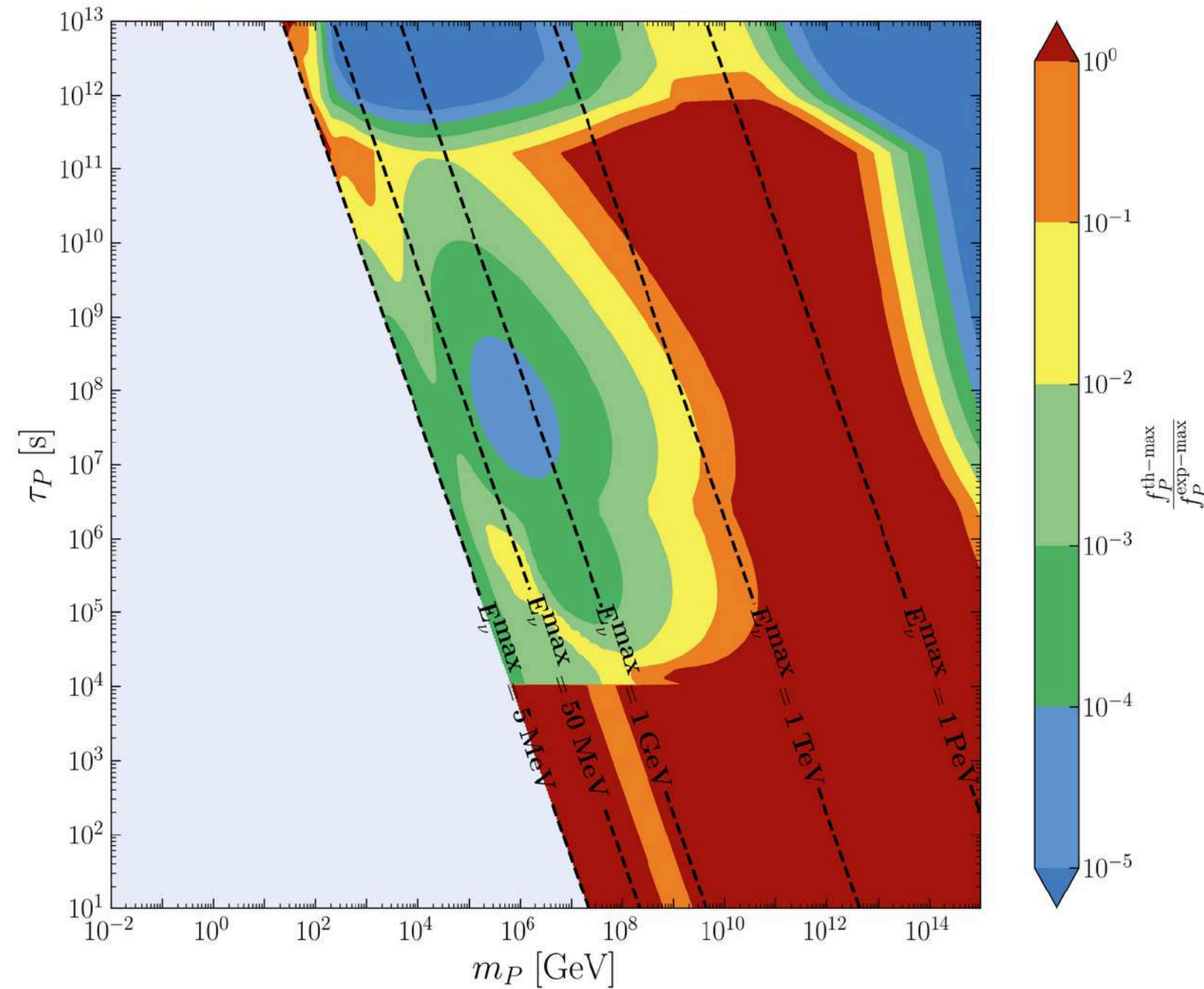
Constraints



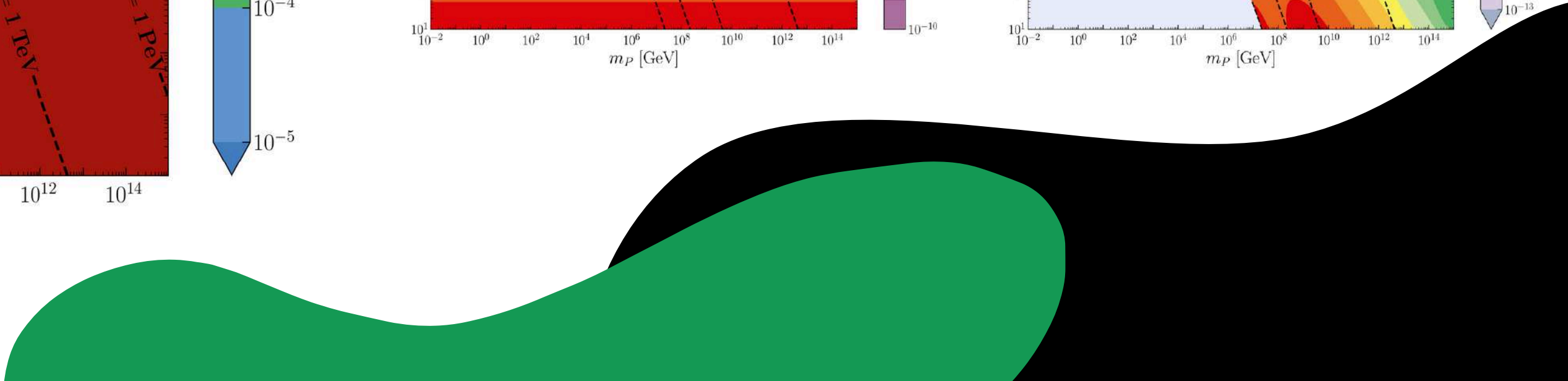
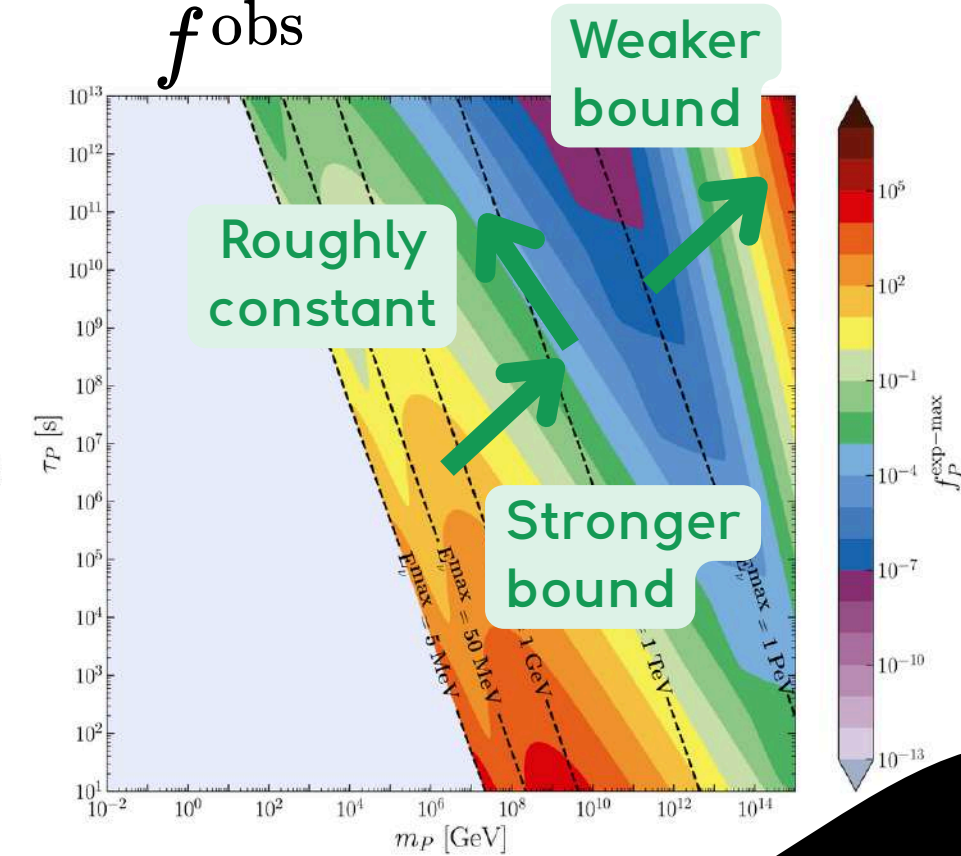
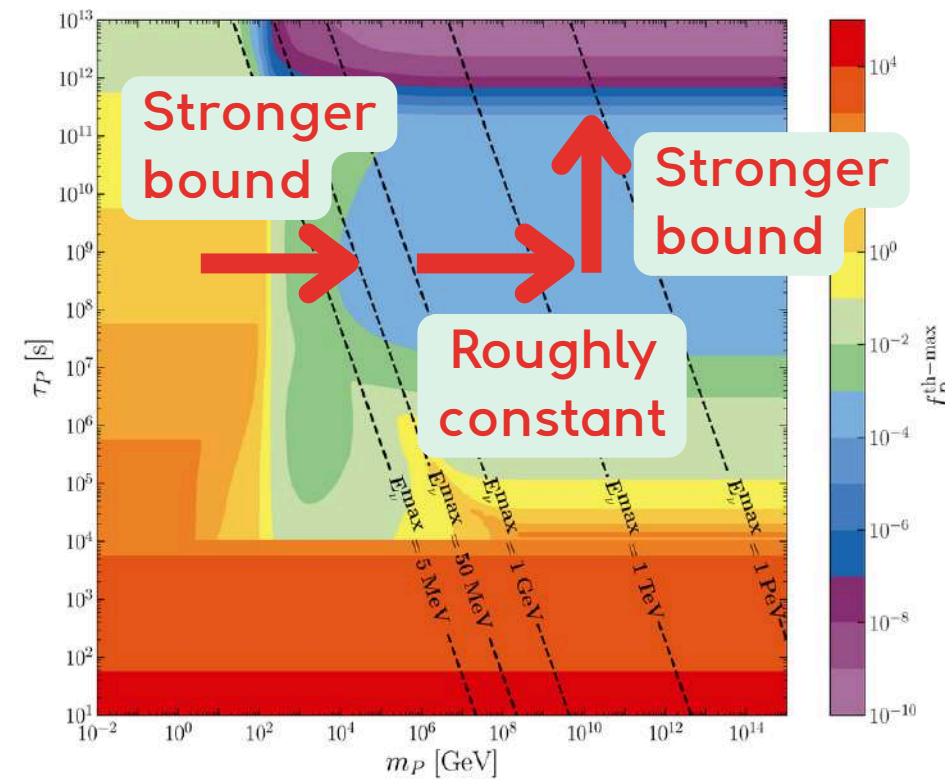
Combination: $\frac{f^{\text{cosmo}}}{f^{\text{obs}}}$



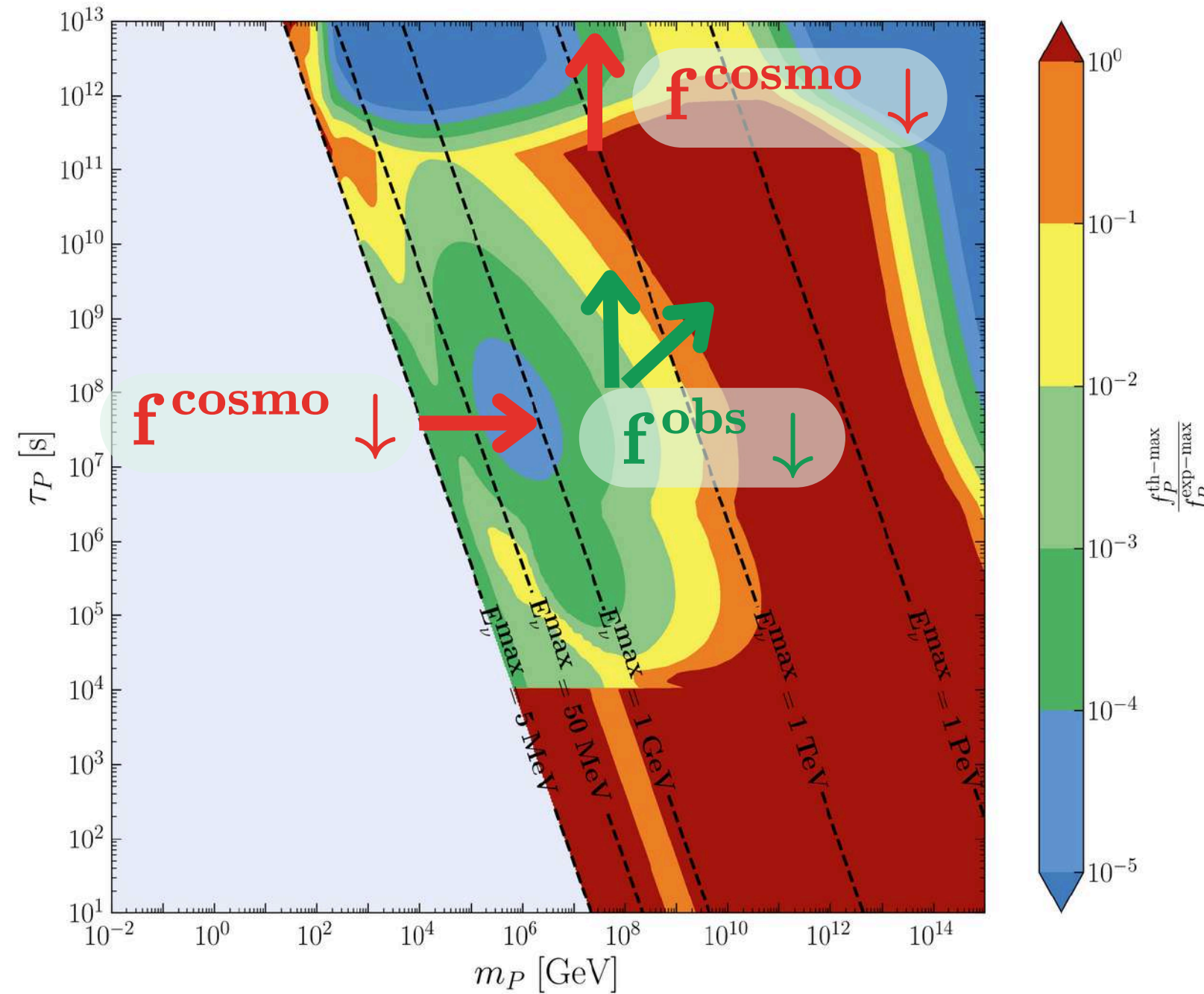
Constraints



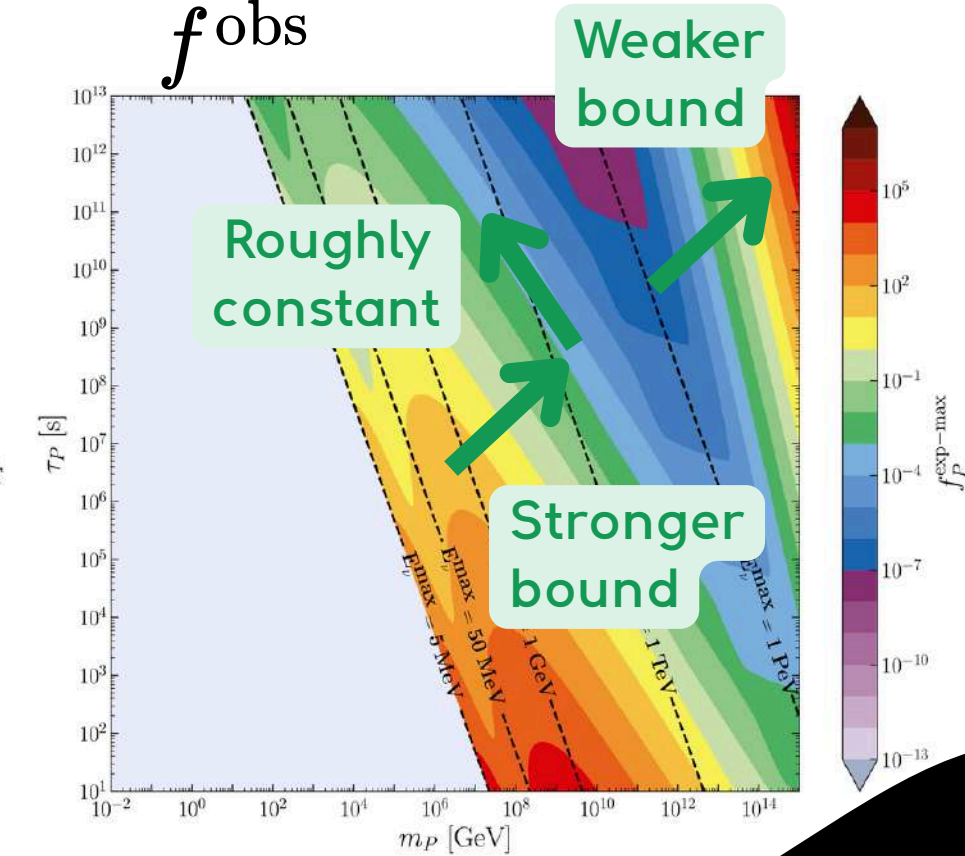
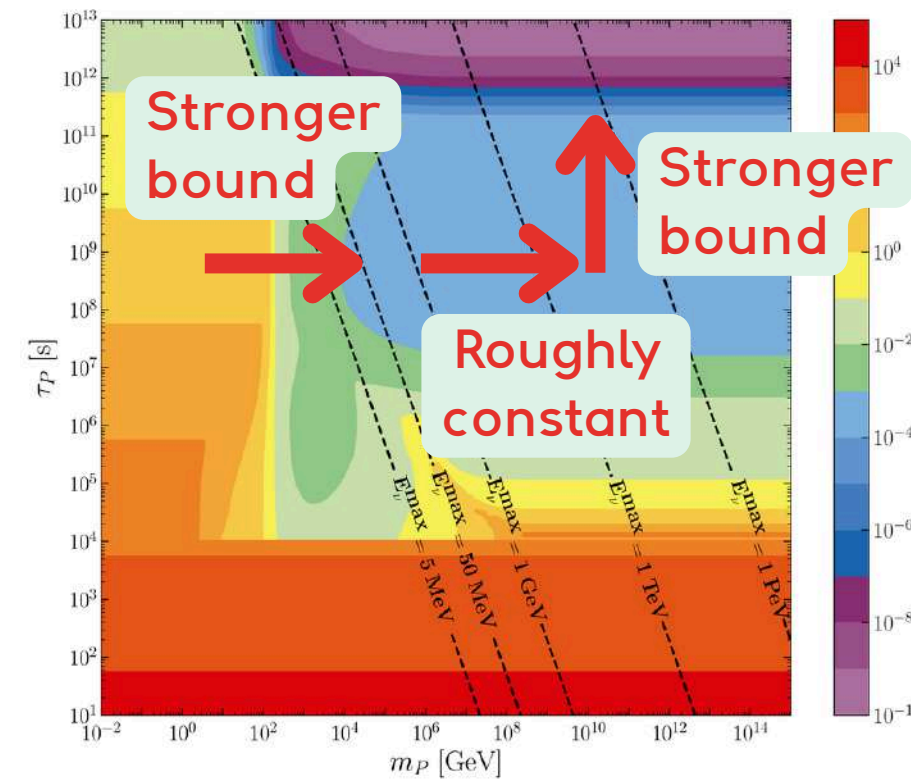
Combination: $\frac{f^{\text{cosmo}}}{f^{\text{obs}}}$



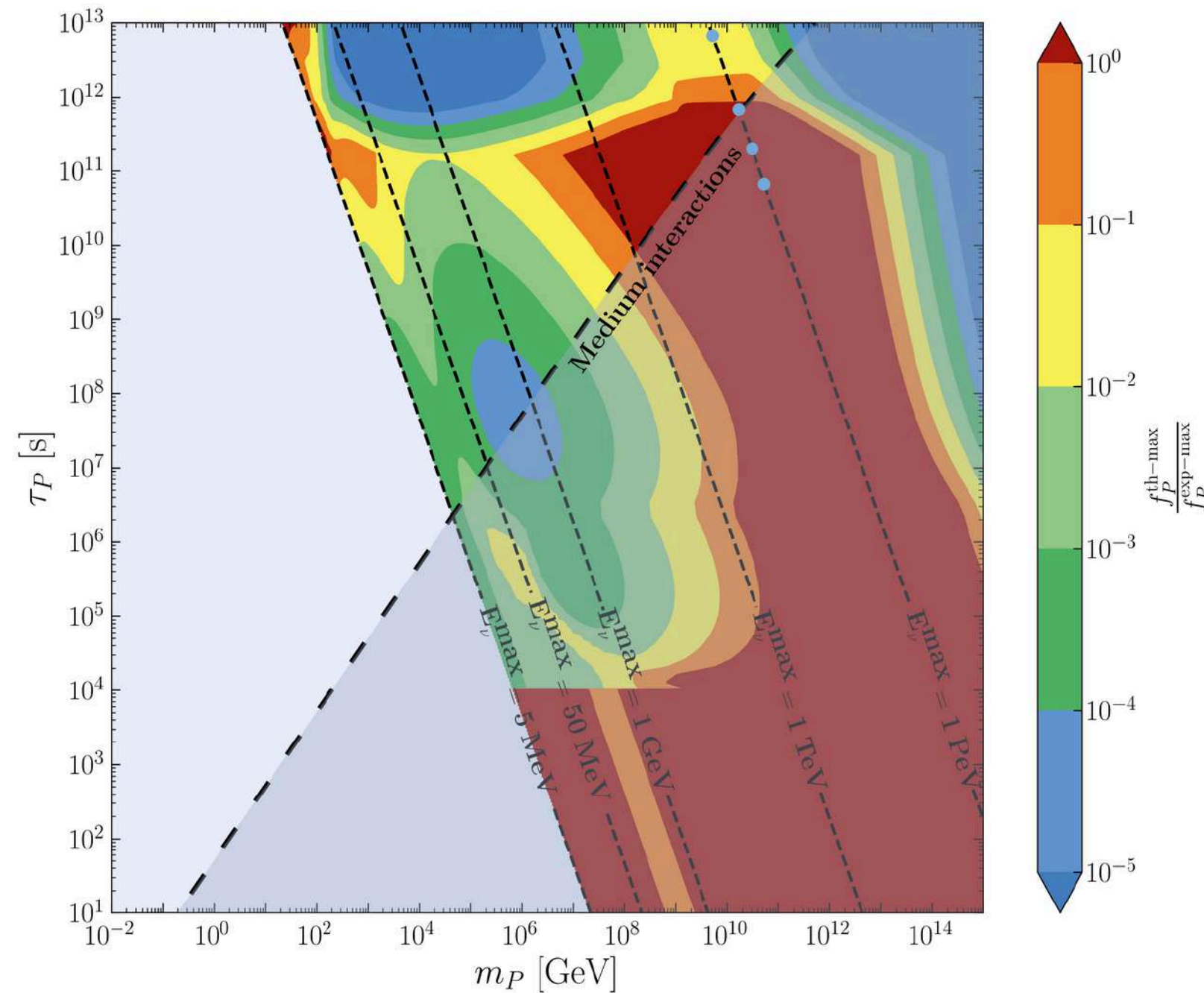
Constraints



Combination: $\frac{f^{\text{cosmo}}}{f^{\text{obs}}}$



Constraints



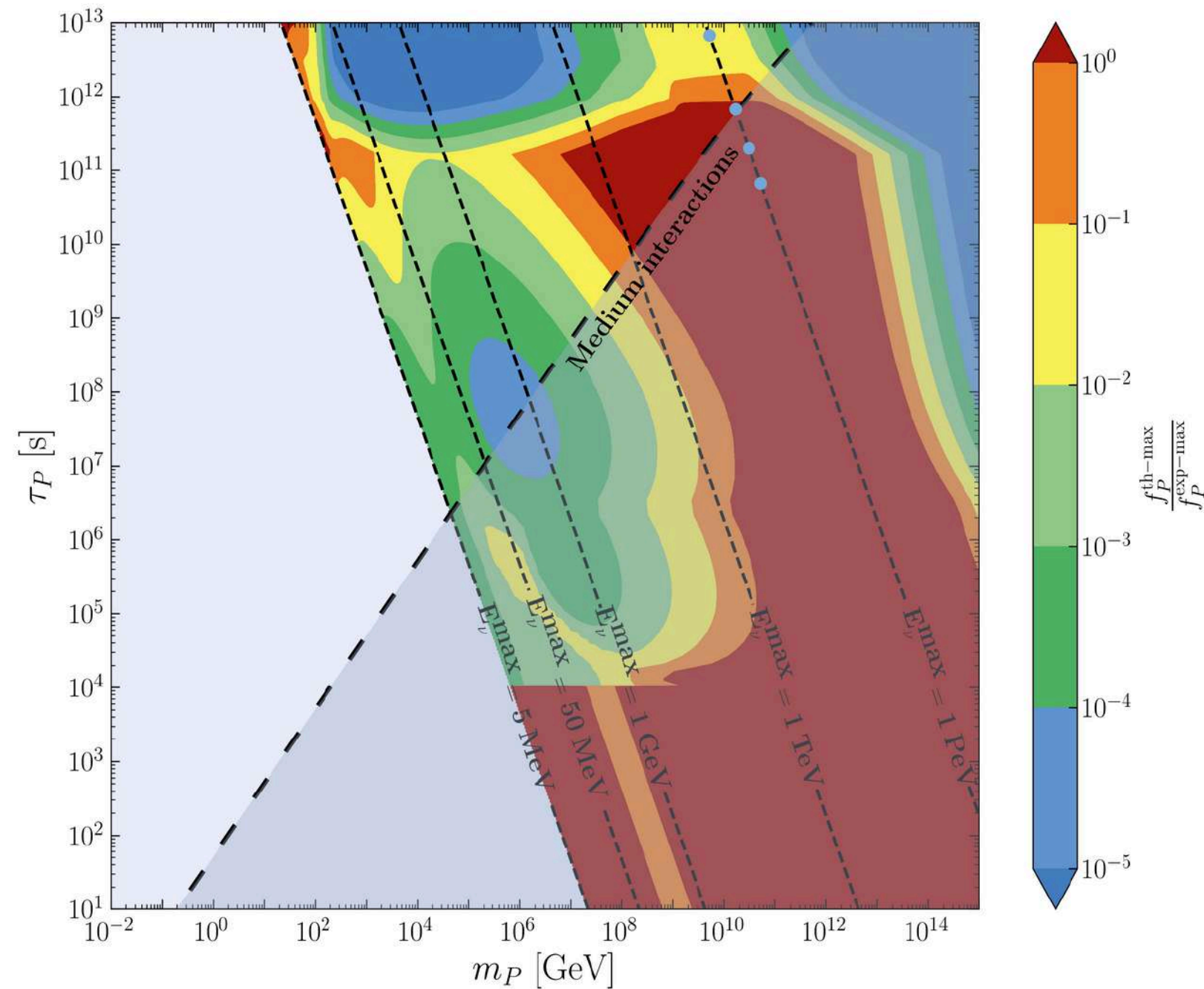
Combination: $\frac{f^{\text{cosmo}}}{f^{\text{obs}}}$

- Ratio > 1: Unconstrained by theoretical bounds
- Ratio > 10⁻²: Potentially **observable today**
- Ratio < 10⁻²: Signal too weak to be observed
- Ratio < 10⁻⁵: Hopeless

$$10 \text{ TeV} \lesssim m_P \lesssim 10^{11} \text{ GeV} \quad 10^{-8} \lesssim f_P \lesssim 10^{-2}$$

$$10^9 \text{ s} \lesssim \tau_P \lesssim 10^{12.5} \text{ s}$$

Constraints



Combination: $\frac{f^{\text{cosmo}}}{f^{\text{obs}}}$

- Ratio > 1: Unconstrained by theoretical bounds
- Ratio > 10⁻²: Potentially observable today
- Ratio < 10⁻²: Signal too weak to be observed
- Ratio < 10⁻⁵: Hopeless

$$10 \text{ TeV} \lesssim m_P \lesssim 10^{11} \text{ GeV}$$

$$10^9 \text{ s} \lesssim \tau_P \lesssim 10^{12.5} \text{ s}$$

$$10^{-8} \lesssim f_P \lesssim 10^{-2}$$

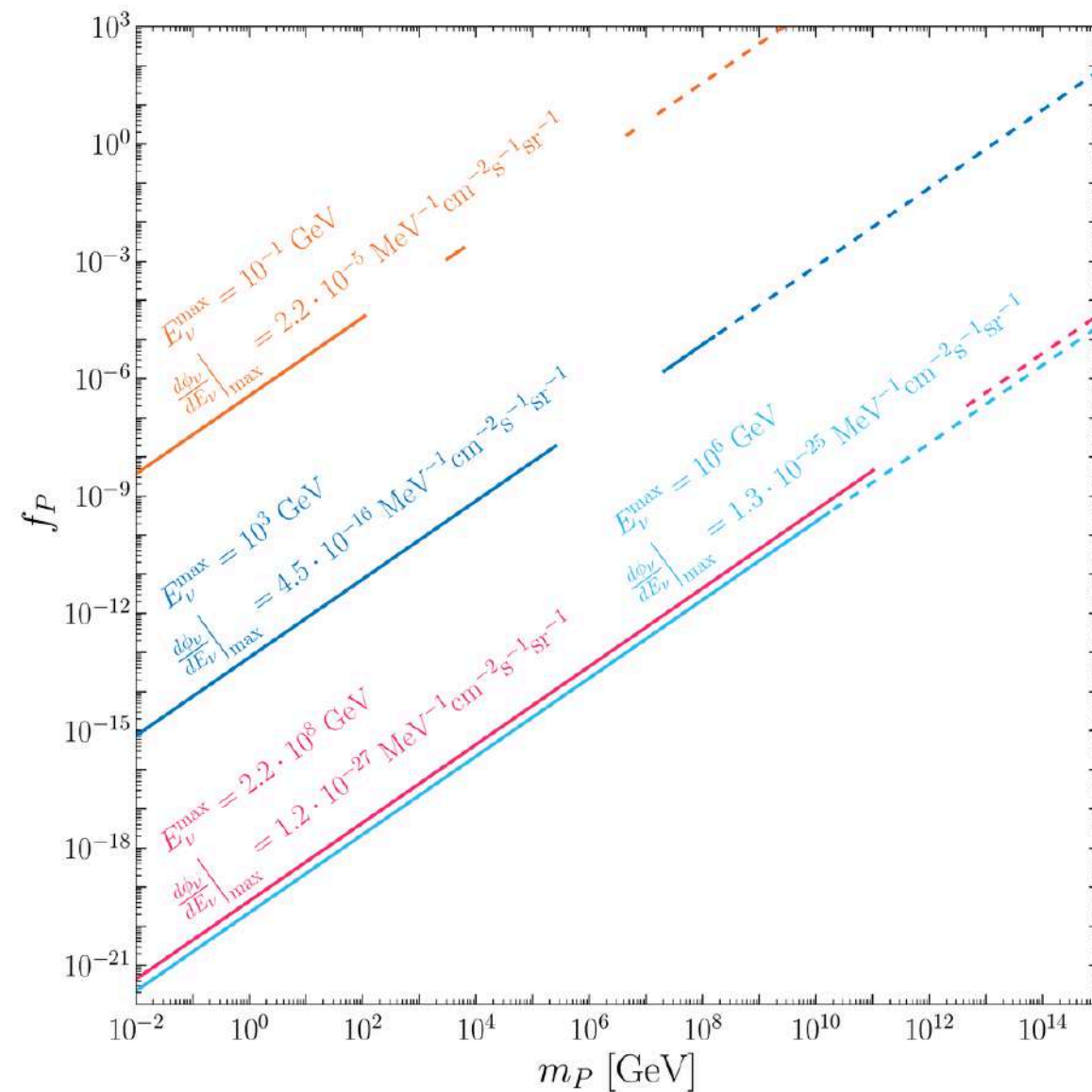
Potentially observable in IceCube,
HyperK, KM3NeT

Constraints.

Reconstruction of the heavy relic parameters:

Given the energy at the peak and the amplitude of a spectrum, 2 parameters can be reconstructed:

- Abundance and mass

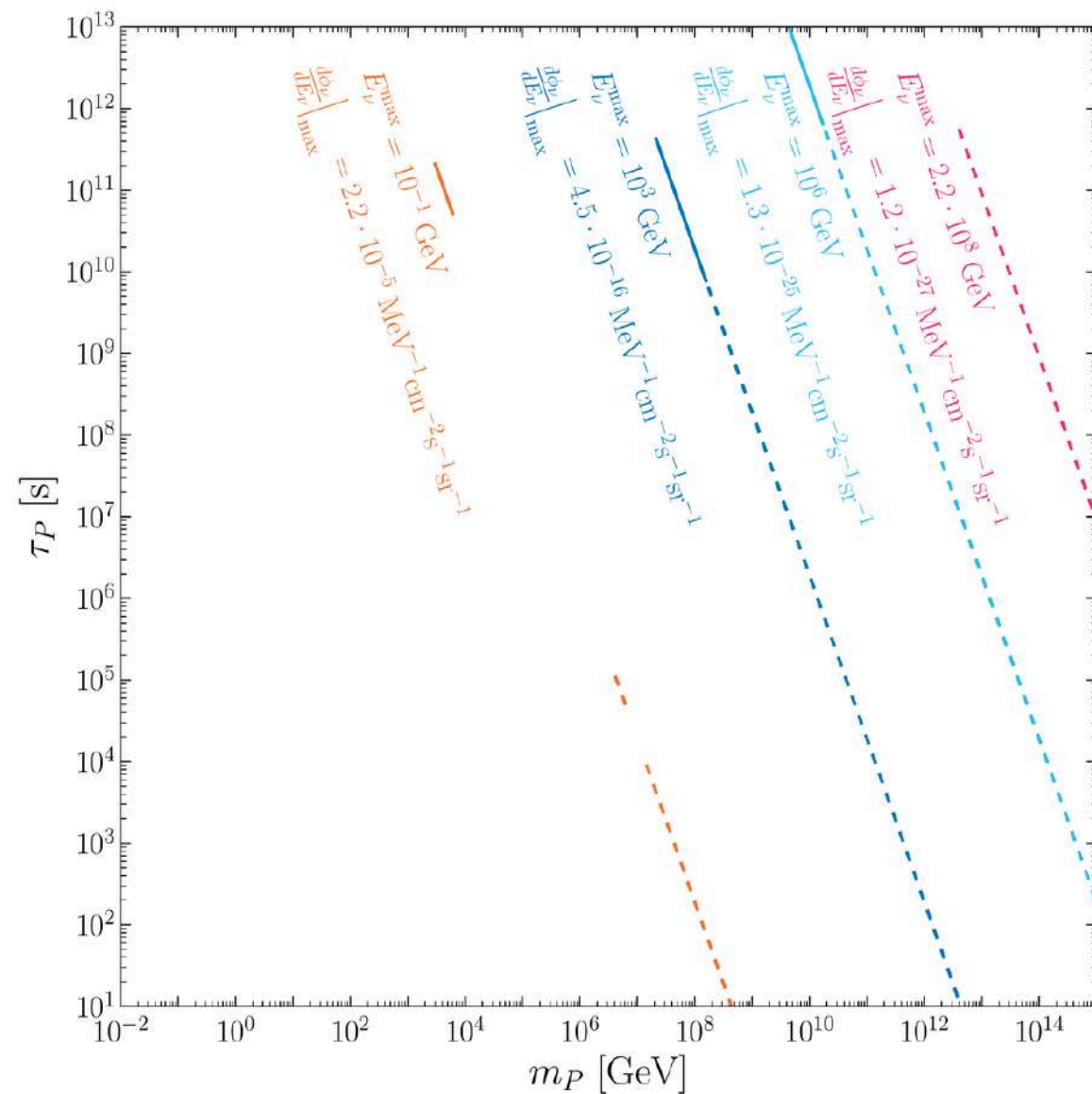


Constraints ●


Reconstruction of the heavy relic parameters:

Given the energy at the peak and the amplitude of a spectrum, 2 parameters can be reconstructed:

- Abundance and mass
- Lifetime and mass

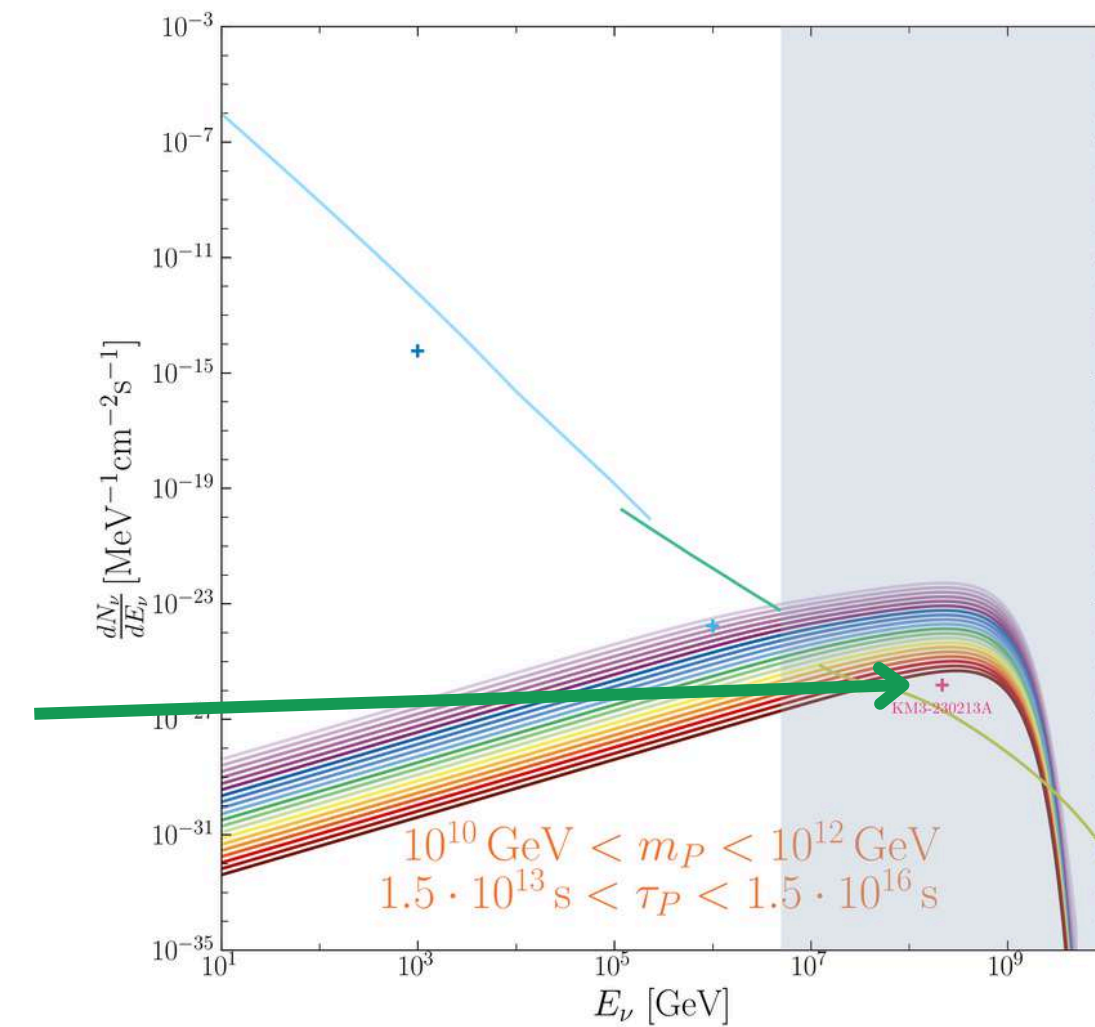


Take home message:

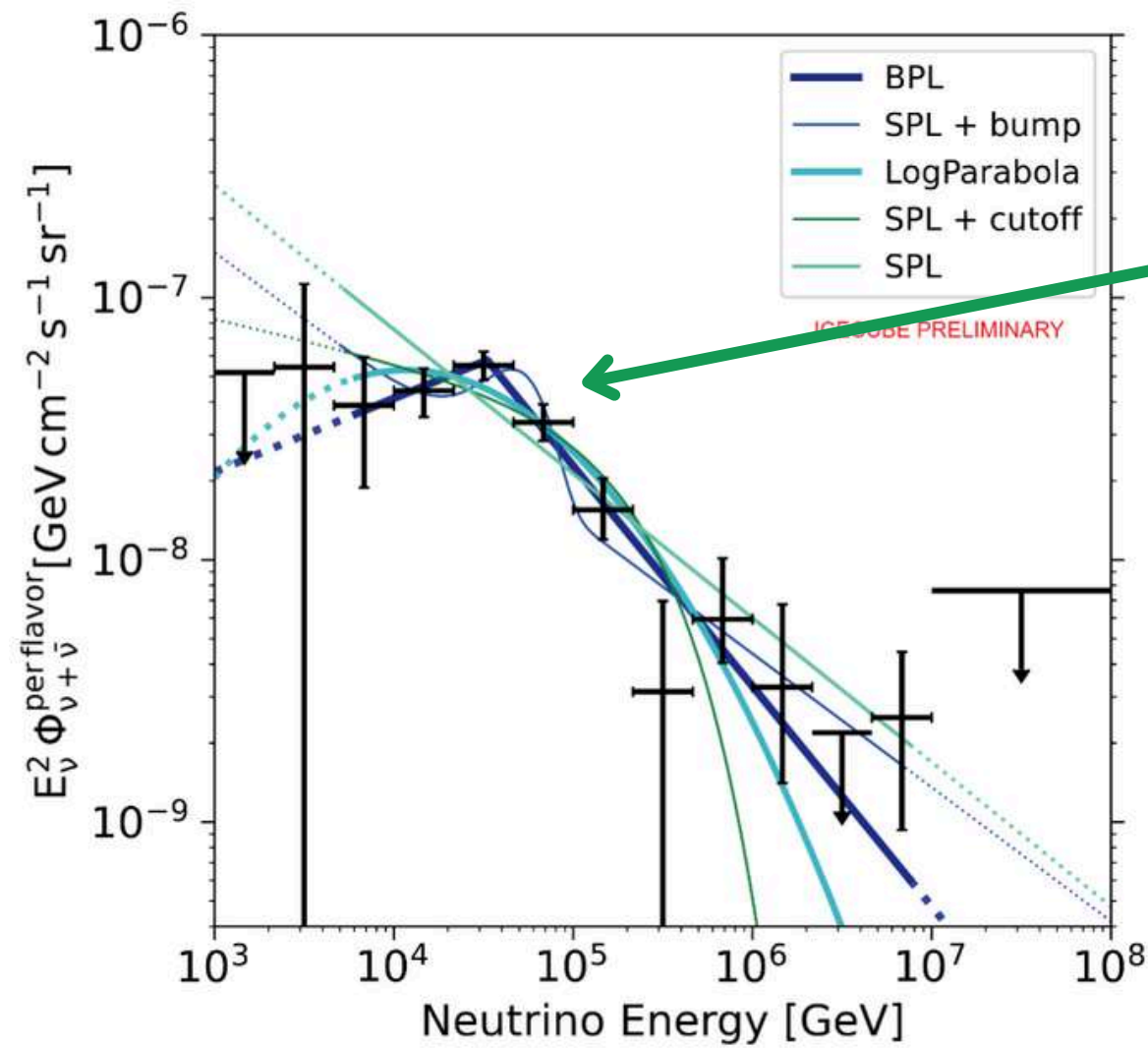
- PHENUs could be produced in the early universe with **sharp spectral features**
 - Scattering on the background or with other PHENUs is **negligible**
 - Sharp spectral features are **observable** for a range of lifetime, mass and abundance
- 

Bumps ?

PHENUs could potentially explain the KM3NeT event



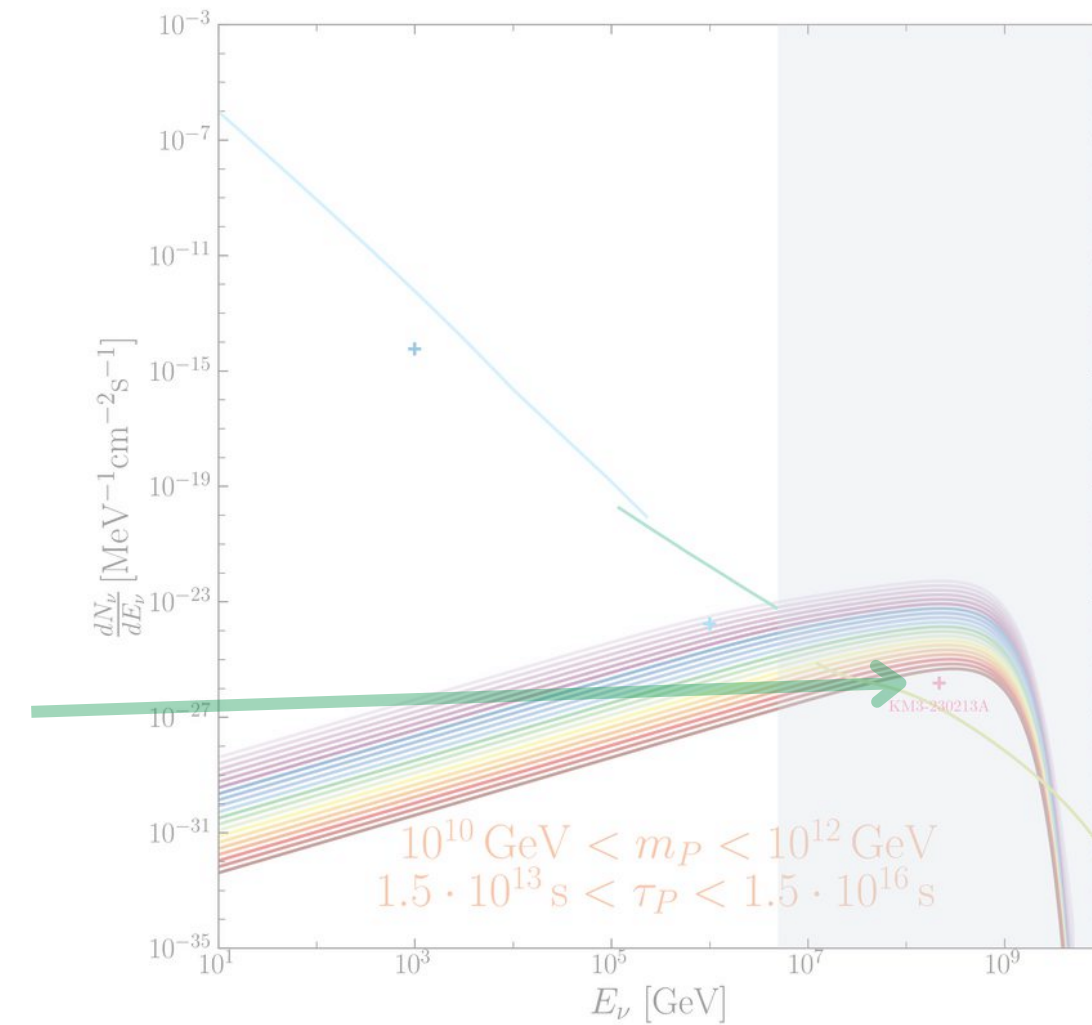
Bumps ?



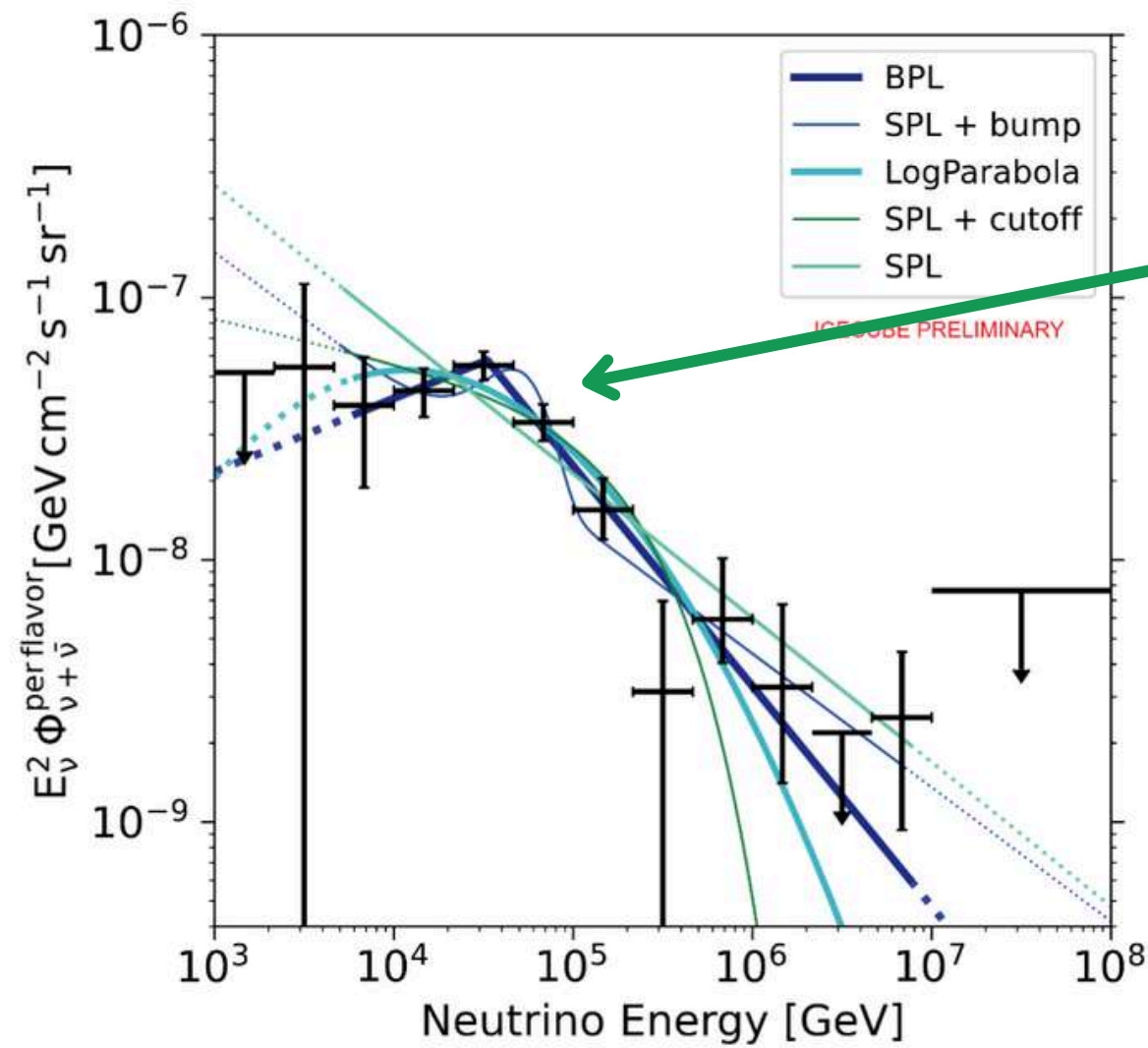
Substructure emerging in the diffuse astrophysical flux ~30 TeV and ~100 TeV

PHENUs could potentially explain the KM3NeT event

arXiv:2507.06002v1



Bumps ?



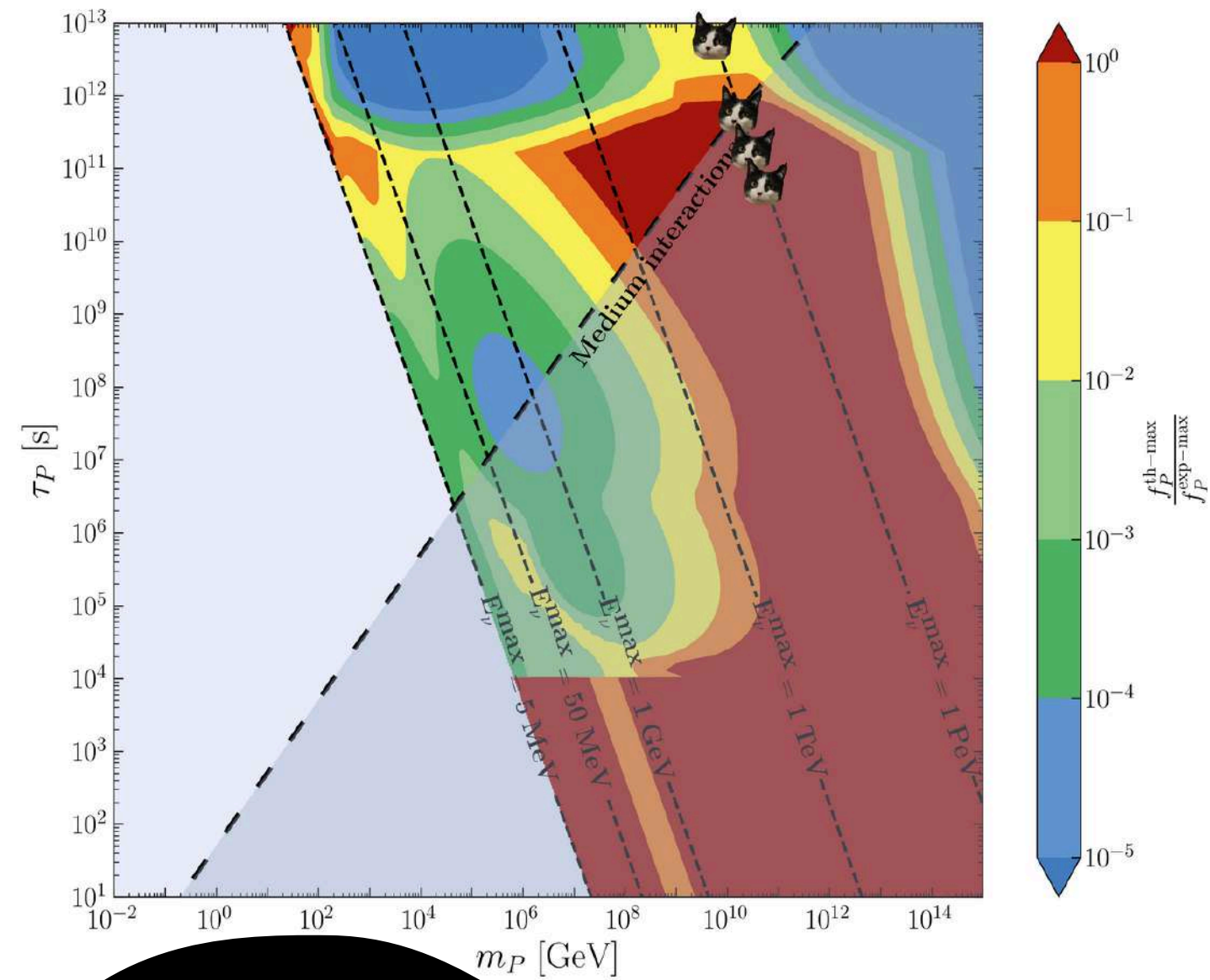
Substructure emerging in the diffuse astrophysical flux ~30 TeV and ~100 TeV

PHENUs could potentially explain the KM3NeT event

arXiv:2507.06002v1



Medium interactions II.



Medium interactions II.

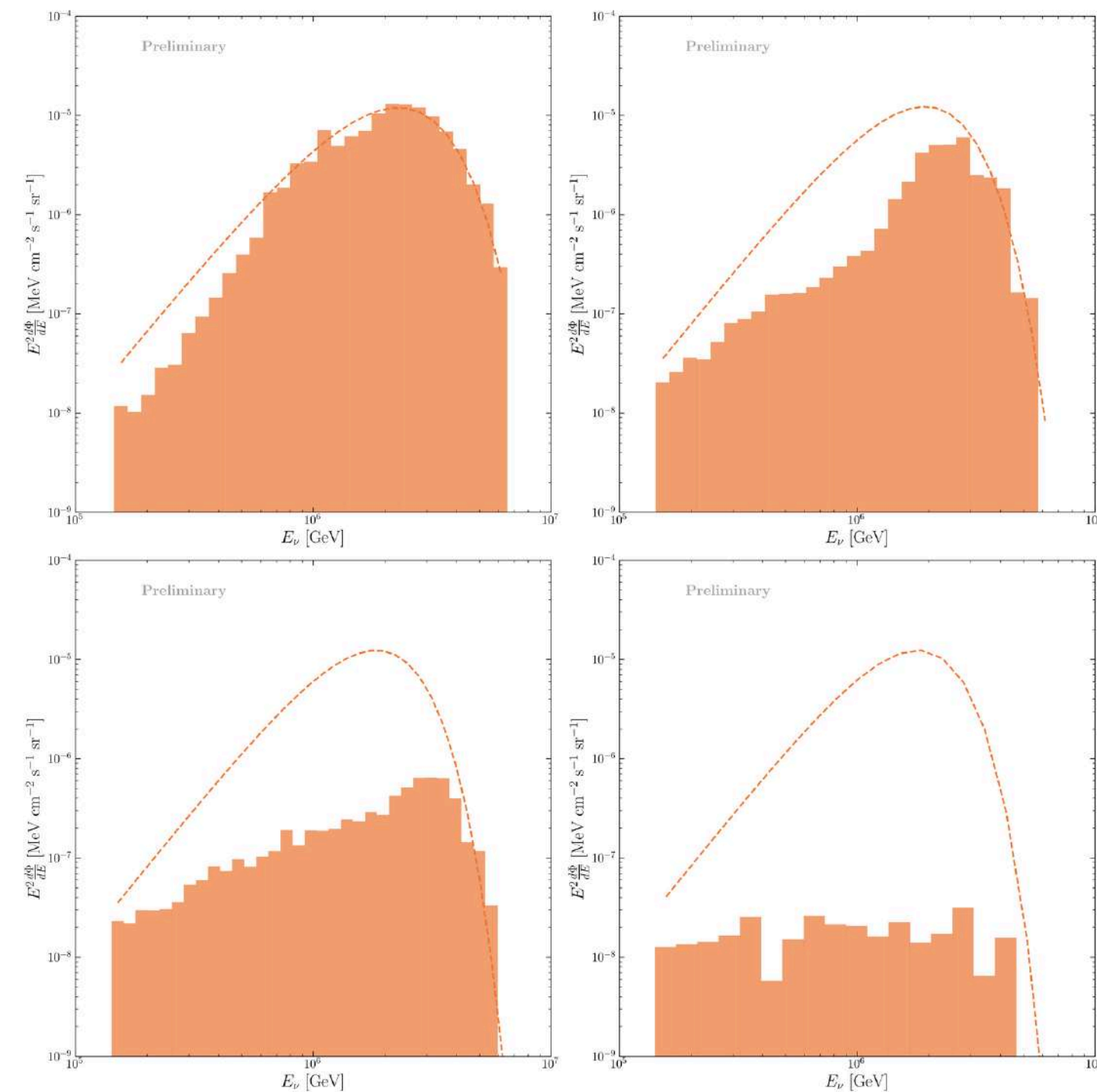
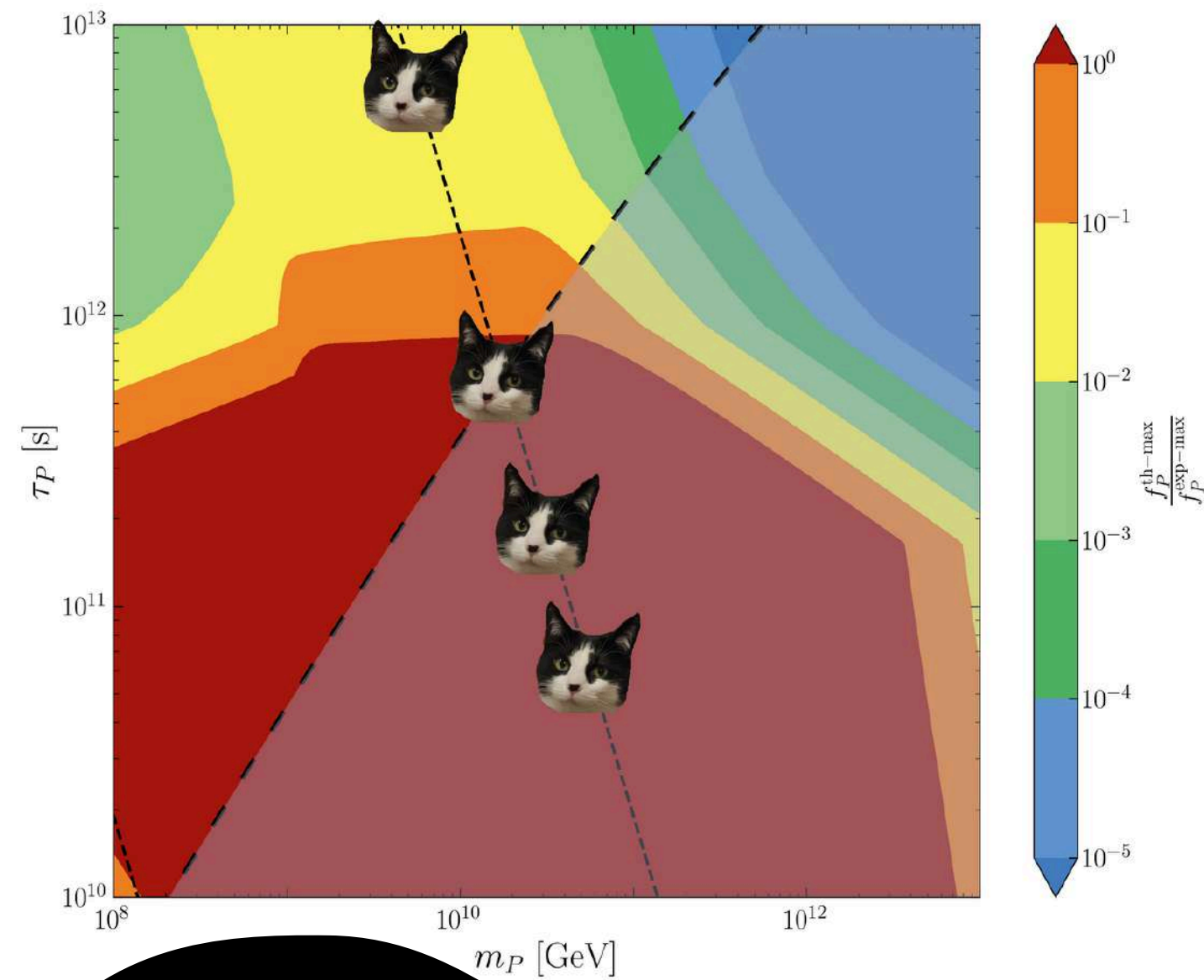
Elastic interactions

- Replace one PHENU by two high-energy neutrinos of smaller energies (upscatter CNB)
- Easy to implement
- More neutrinos to track → computationally expensive

Inelastic interactions

- For a proper treatment, need to implement EM and hadronic cascades → Hard to implement
- Most secondary neutrinos at lower energy → can be neglected
- → PHENU disappears into other SM particles
- Less neutrinos to track → simplifies computation

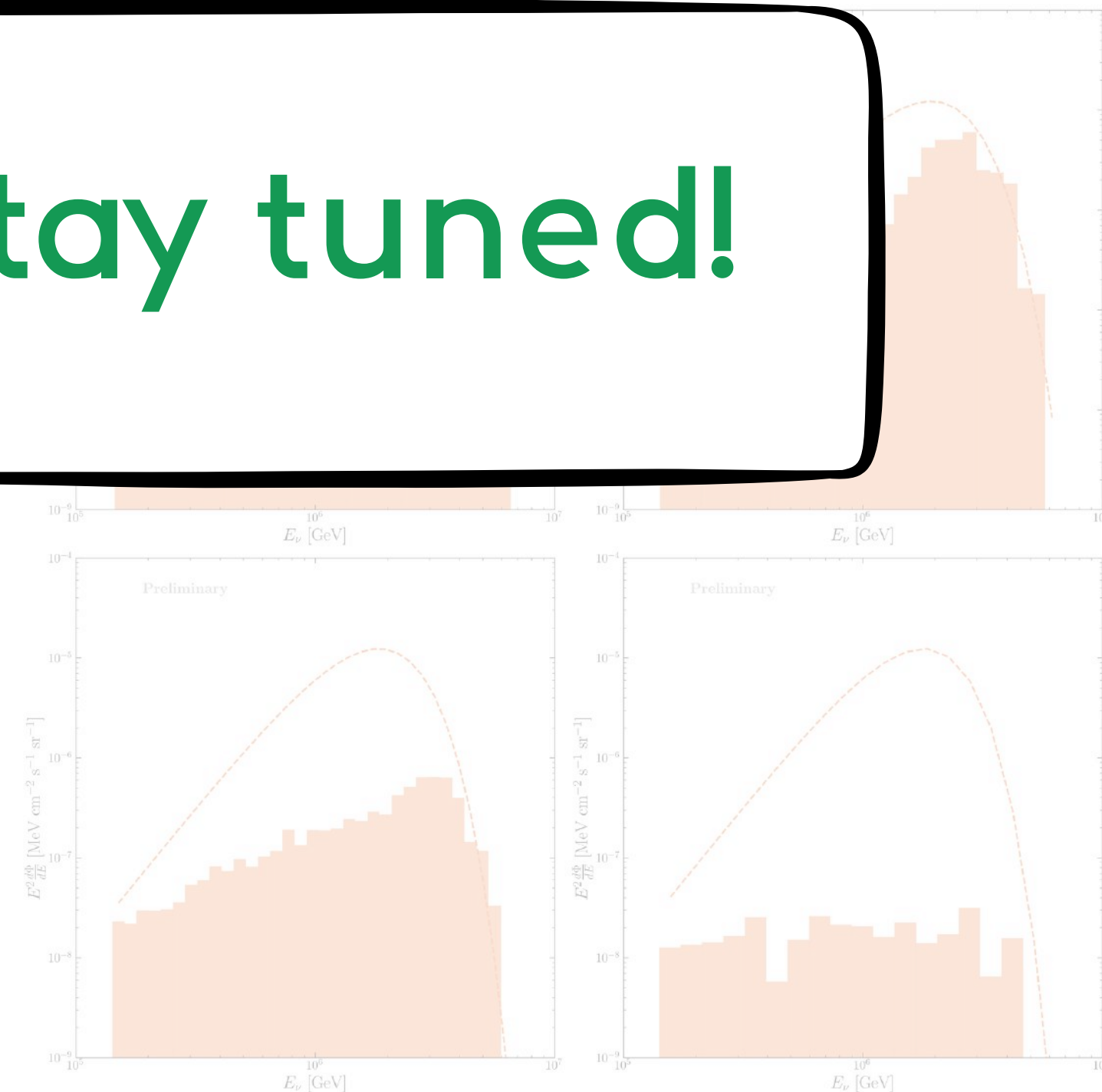
Medium interactions II.



Medium interactions II.



Stay tuned!



Thank you for your **attention**



arXiv:2507.02063
2512.XX???

Backup slides

Decay Spectra.

$$\frac{d\phi_\nu}{dE_\nu} = \frac{2\Omega_P^0 \rho_{crit}^0}{m_P H \tau_P E_\nu} e^{-t/\tau_P} \Theta\left(\frac{m_P}{2} - E_\nu\right)$$

$$\frac{d\phi_\nu}{dE_\nu} = \frac{6\Omega_P^0 \rho_{crit}^0}{\pi m_P^4 \tau_P E_\nu} \int_{E_\nu}^{\frac{m_P}{2}} dx x^2 \frac{e^{-t(E_\nu/x)/\tau_P}}{H(E_\nu/x)}$$

$$\frac{d\phi_\nu}{dE_\nu} = \frac{4\Omega_0^P \rho_{crit}^0}{\pi m_P^2 \tau_P E_\nu \sqrt{1 - (1 - \Delta)^2}} \int_{\max(E_\nu, E_-)}^{E_+} dx \frac{e^{-t(E_\nu/x)/\tau_P}}{H(E_\nu/x)}$$

$$\Delta = 1 - \frac{2m_{P'}}{m_P} \quad E^\pm = \frac{m_P}{4} (1 \pm \sqrt{1 - (1 - \Delta)^2})$$

2-body decay $\frac{dN}{dE} = \delta(E - m_P/2)$

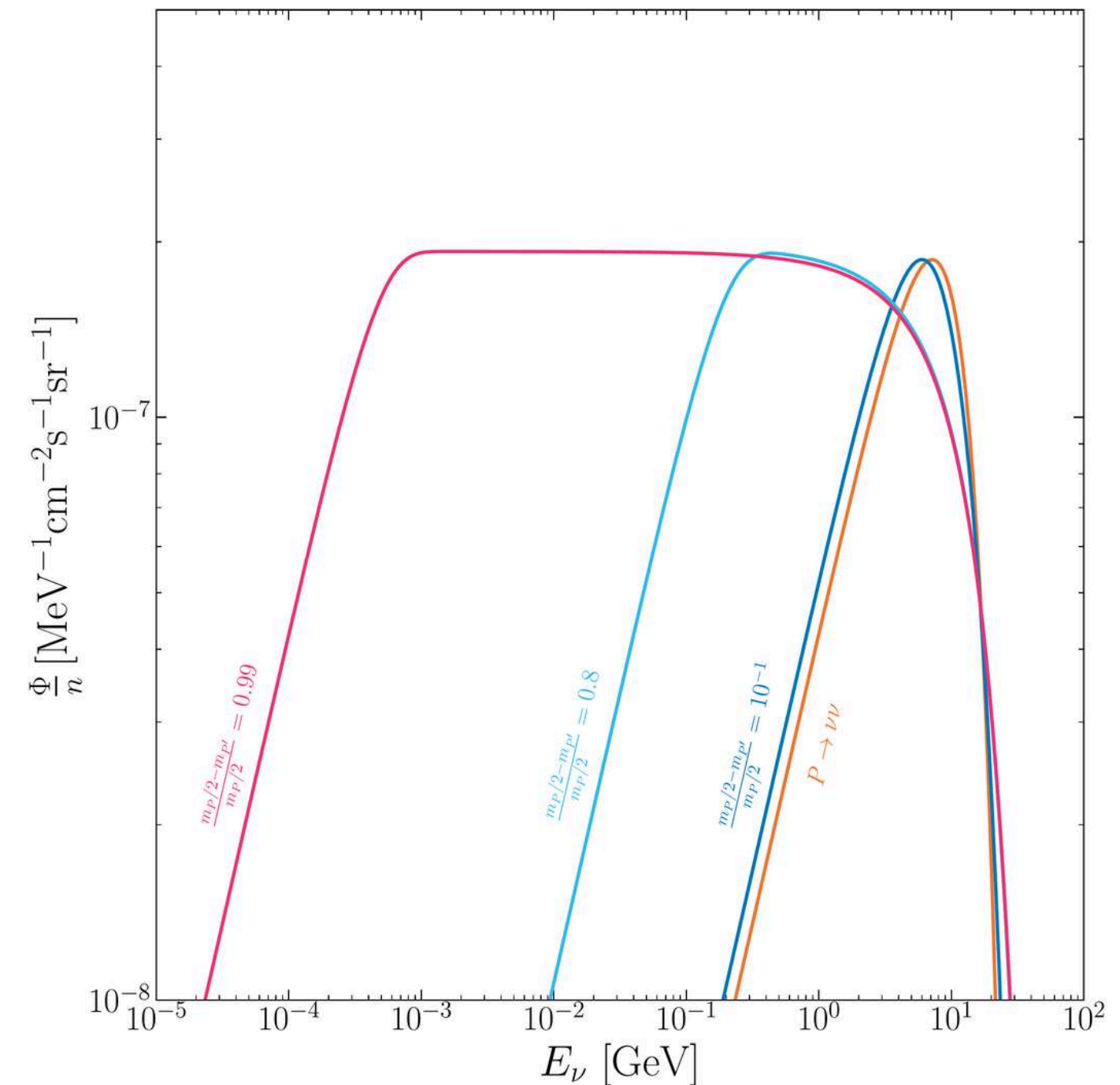
3-body decay $\frac{dN}{dE} = \Theta(m_P/2 - E) \cdot 24 \frac{E^2}{m_P^3}$

Box shaped $\frac{dN}{dE} = \frac{8}{m_P \sqrt{1 - \frac{4m_{P'}^2}{m_P^2}}} \Theta(E - E_-) \Theta(E_+ - E)$

Decay Spectra.

Δ controls the width of the box.

In the limit where $\Delta = 0$ we recover the 2-body decay spectrum



Annihilation.

$$\frac{d\phi_\nu}{dE_\nu} = \frac{\Delta n_\nu}{8\pi} \frac{(\Omega_P^0 \rho_{crit}^0)^2 m_P \langle \sigma v \rangle}{E_\nu^4 H} \frac{1}{\left(1 - \frac{\langle \sigma v \rangle s}{H} \left(1 - \frac{E_\nu(1+z_*)}{m_P}\right) \frac{n}{s} \Big|_{t_*}\right)^2}$$

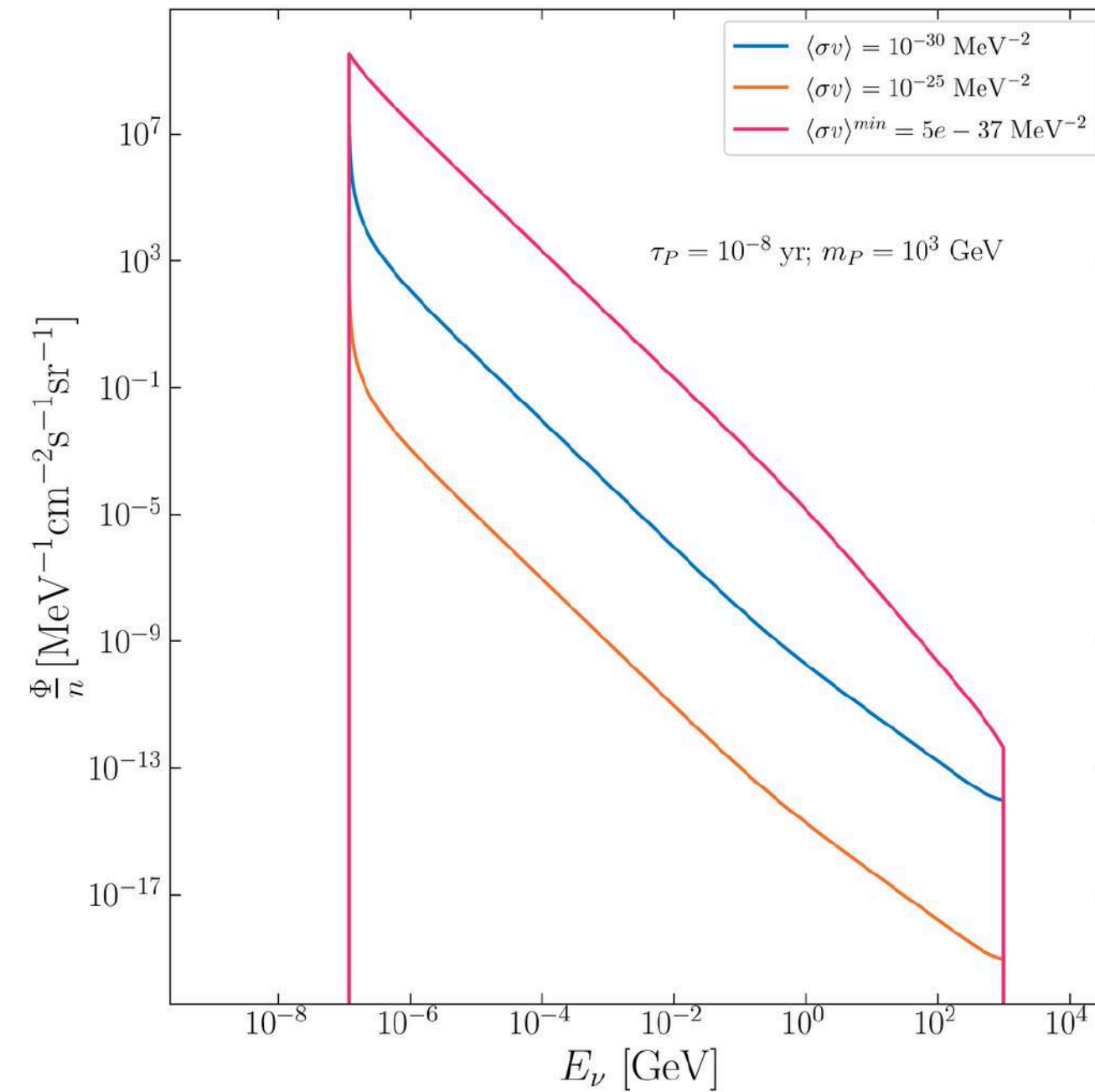
$$\langle \sigma v \rangle n_P^{eq} < H(t^{inj}) \quad \rightarrow \quad \langle \sigma v \rangle < \left(\frac{2\pi}{m_P T^{inj}}\right)^{3/2} \frac{e^{m_P/T^{inj}}}{2g_i t^{inj}}$$

$$\langle \sigma v \rangle n_P^{inj} > H(t^{inj}) \quad \rightarrow \quad \langle \sigma v \rangle > \frac{m_P}{2\Omega_P^0 \rho_{crit}^0} \sqrt{\frac{t^{inj}}{t_r^3}}$$

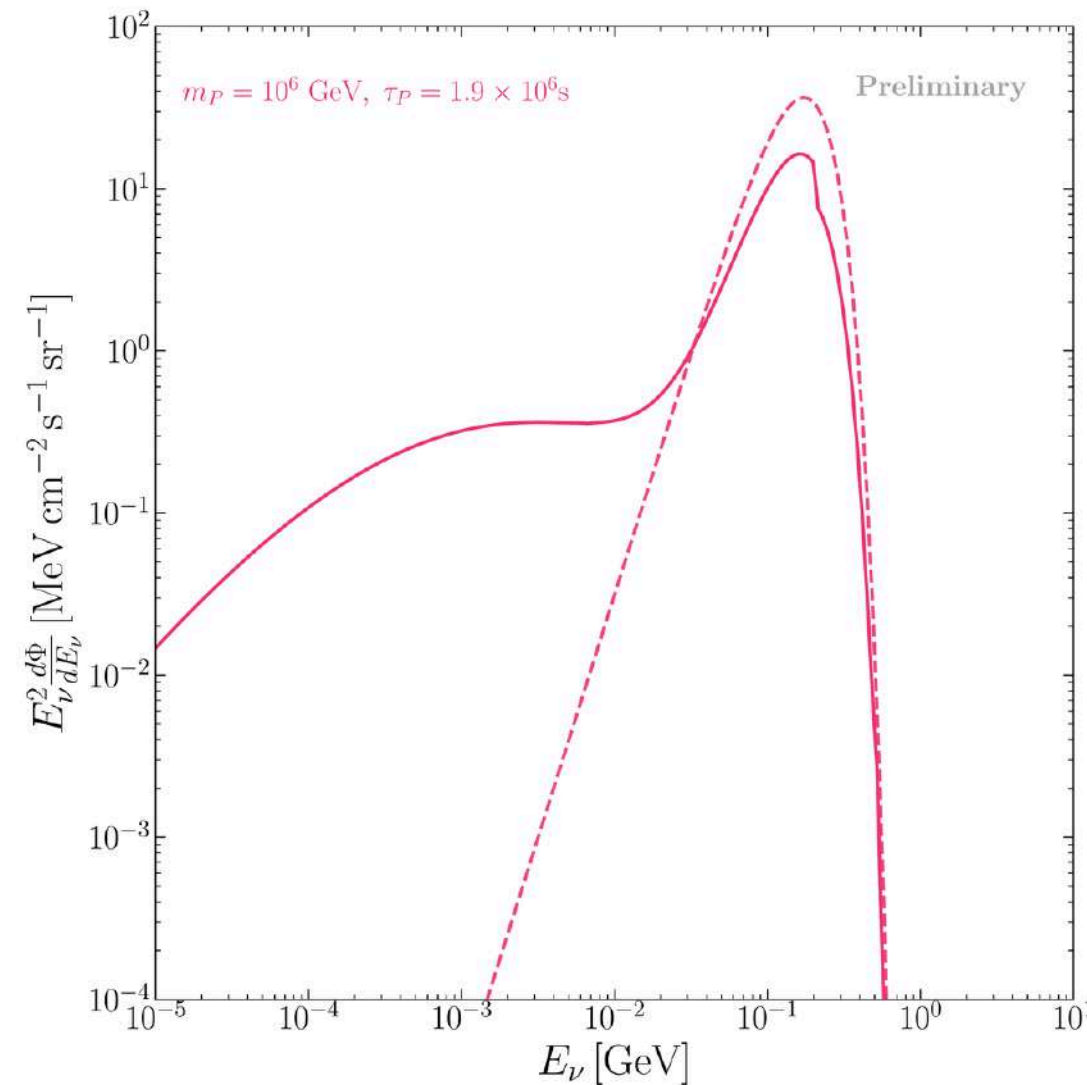
Not too constraining for large mass as it is satisfied as long as T_{inj} is sufficiently lower than m_P

Annihilation.

$$\langle \sigma v \rangle > \frac{m_P}{2\Omega_P^0 \rho_{crit}^0} \sqrt{\frac{t^{inj}}{t_r^3}}$$



Sharp Spectral Features.

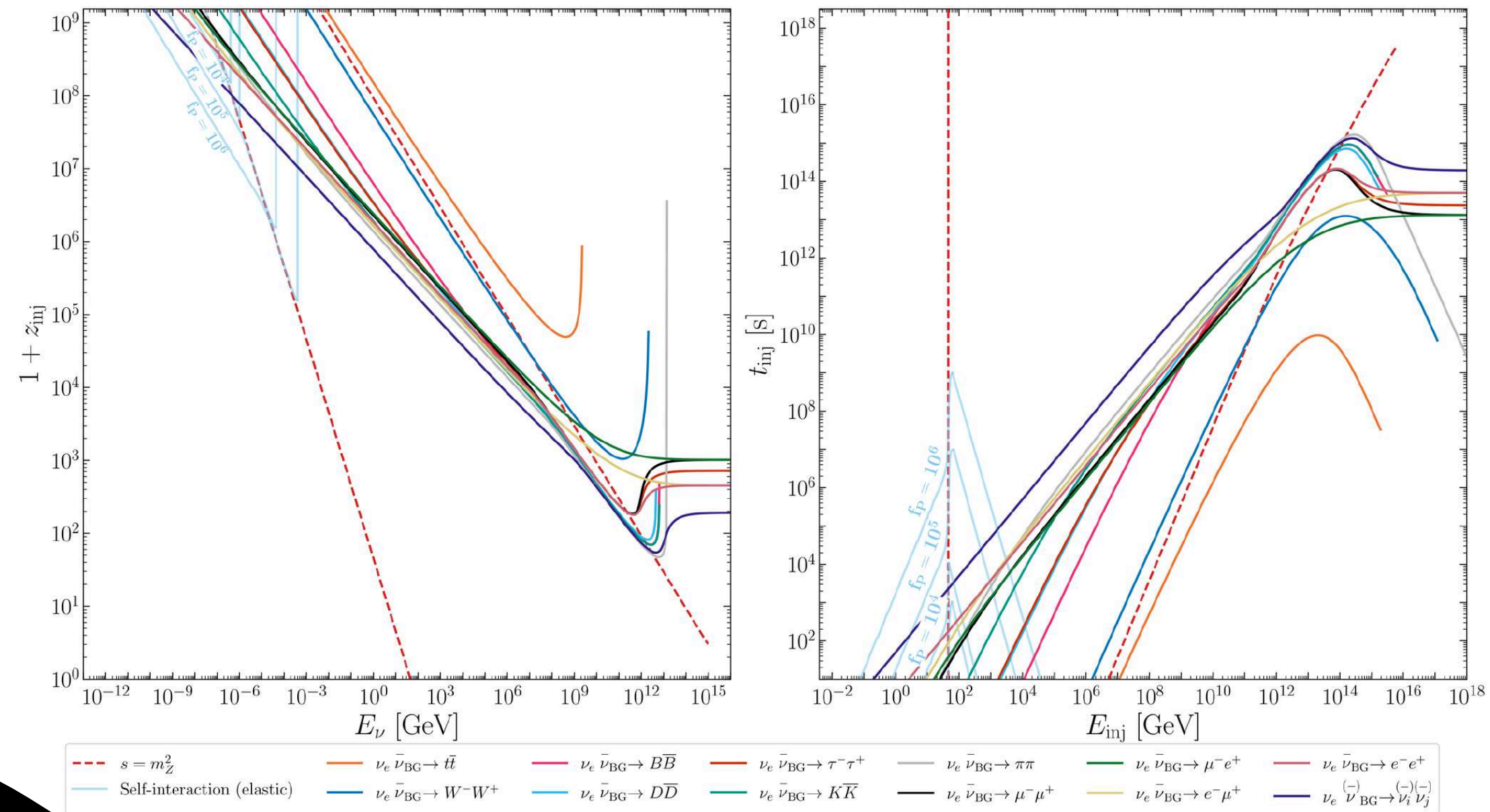


Final state radiation broadening

- If $E_\nu > M_{Z/W}$, gauge bosons can be radiated and generate a shower
- Production of (many) secondary neutrinos of lower energies
- Energy dependent process

Sharp feature mostly unaffected

Medium interactions.



Cross-sections.

Elastic

$$\frac{d\sigma}{dt} = \frac{g^4}{64\pi \cos(\theta_W)^4} \frac{C(s, t, m_Z)}{(t - m_Z^2)^2}$$

Process	$C(s, t, m_Z)$
$\nu_l \bar{\nu}_l \rightarrow \nu_l \bar{\nu}_l$	$\frac{(s+t)^2 (s+t-2m_Z^2)^2}{s^2 (s-m_Z^2)^2}$
$\nu_l \bar{\nu}_l \rightarrow \nu_{l'} \bar{\nu}_{l'}$	$\frac{(s+t)^2 (t-m_Z^2)^2}{s^2 (s-m_Z^2)^2}$
$\nu_l \nu_l \rightarrow \nu_l \nu_l$	$\frac{(s+2m_Z^2)^2}{(s+t+m_Z^2)^2}$
$\nu_l \bar{\nu}_{l'} \rightarrow \nu_l \bar{\nu}_{l'}$	$\frac{(s+t)^2}{s^2}$
$\nu_l \nu_{l'} \rightarrow \nu_l \nu_{l'}$	1

Cross-sections.

Inelastic $\nu_l \bar{\nu}_l \rightarrow l^- l^+$

$$\frac{d\sigma}{dt} = \frac{g^4}{64\pi s^2 (s - m_Z^2)(t - m_W^2)} \left\{ K_1 + \frac{s - m_Z^2}{t - m_W^2} K_2 + \frac{(t - m_W^2) \tan(\theta_W)^4}{s - m_Z^2} K_3 \right\}$$

$$K_1 = (2 \sin(\theta_W)^2 - 1) \left(s \frac{m_l^4}{2m_W^2} + (s + t - m_l^2)^2 \right) + 2 \sin(\theta_W)^2 m_l^2 \left(s + \frac{(m_l^2 - t)^2}{2m_W^2} \right)$$

$$K_2 = (s + t)(s + t + 2m_l^2) + m_l^4 \left(1 + \frac{s}{m_W^2} + \frac{(m_l^2 - t)^2}{4m_W^4} \right),$$

$$K_3 = s^2 + 2(m_l^4 - 2m_l^2 t + t(s + t)) - \frac{m_l^2 s + (s + t - m_l^2)^2}{\sin(\theta_W)^2} + \left(\frac{s + t - m_l^2}{2 \sin(\theta_W)^2} \right)^2.$$

Cross-sections.

Inelastic $\nu_l \bar{\nu}_l \rightarrow l'^+ l'^-$

$$\frac{d\sigma}{dt} = \frac{g^4 \tan(\theta_W)^4}{64\pi s^2 (s - m_Z^2)^2} K_3$$

$$K_1 = (2 \sin(\theta_W)^2 - 1) \left(s \frac{m_l^4}{2m_W^2} + (s + t - m_l^2)^2 \right) + 2 \sin(\theta_W)^2 m_l^2 \left(s + \frac{(m_l^2 - t)^2}{2m_W^2} \right)$$

$$K_2 = (s + t)(s + t + 2m_l^2) + m_l^4 \left(1 + \frac{s}{m_W^2} + \frac{(m_l^2 - t)^2}{4m_W^4} \right),$$

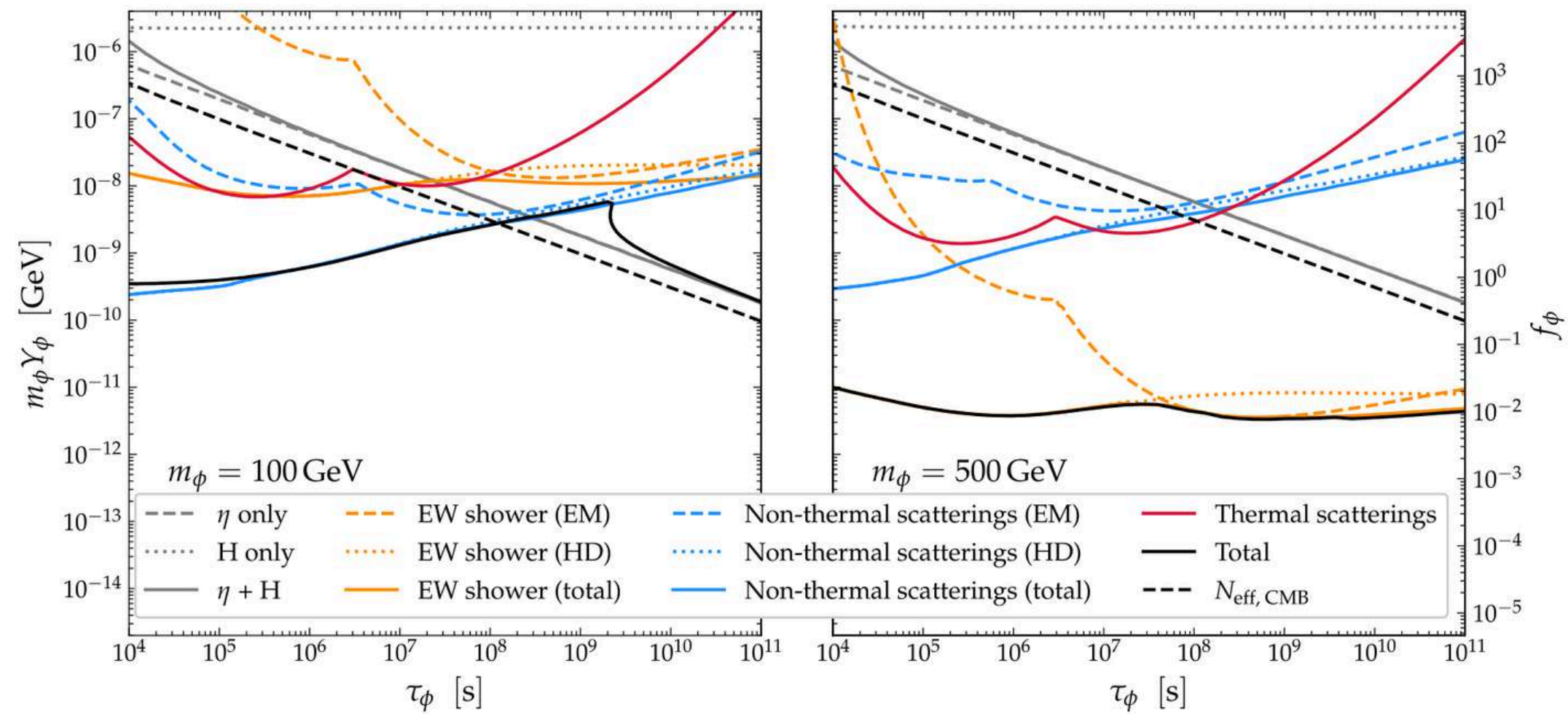
$$K_3 = s^2 + 2(m_l^4 - 2m_l^2 t + t(s + t)) - \frac{m_l^2 s + (s + t - m_l^2)^2}{\sin(\theta_W)^2} + \left(\frac{s + t - m_l^2}{2 \sin(\theta_W)^2} \right)^2.$$

Self-scattering.

$$S_\nu(z, E_\nu^0) = \int_0^z \frac{dz'}{(1+z')H(z')} \Gamma(E_\nu^0(1+z'), z')$$

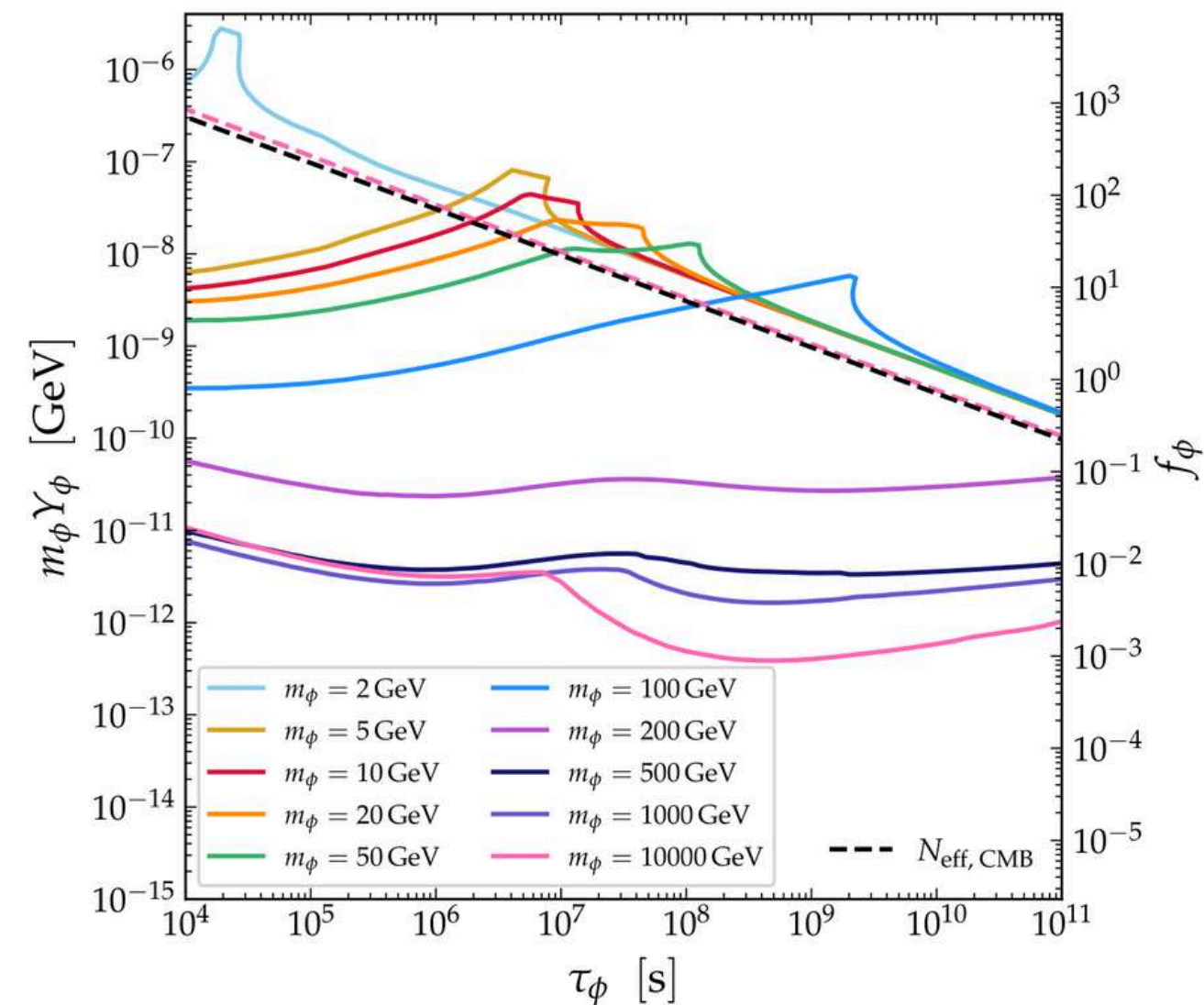
$$\langle \Gamma(E_0, z) \rangle = \frac{\Omega_P^0 \rho_{crit}^0 (1+z)^3}{4E_0^2 (1+z)^2 m_P \tau_P} \int_0^{2E_0(1+z)m_P} ds \sigma(s) s \int_{\frac{s}{4E_0(1+z)}}^{m_P/2} \frac{dE}{E^3} \frac{e^{-t(a_E)/\tau_P}}{H(a_E)}$$

BBN constraints.



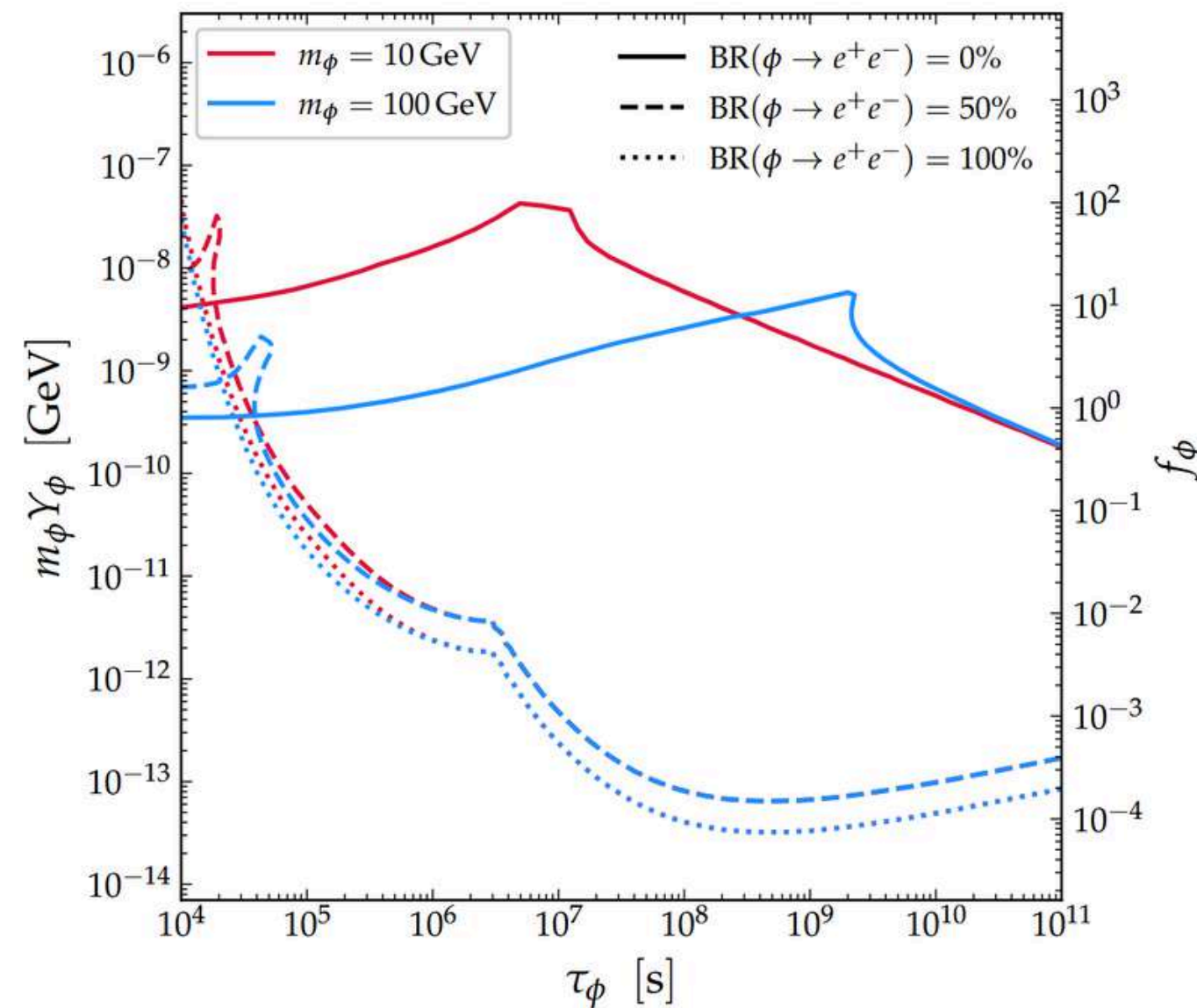
Bianco, Depta, Frerick, Hambye, Hufnagel, Schmidt-Hoberg 25'

BBN constraints.

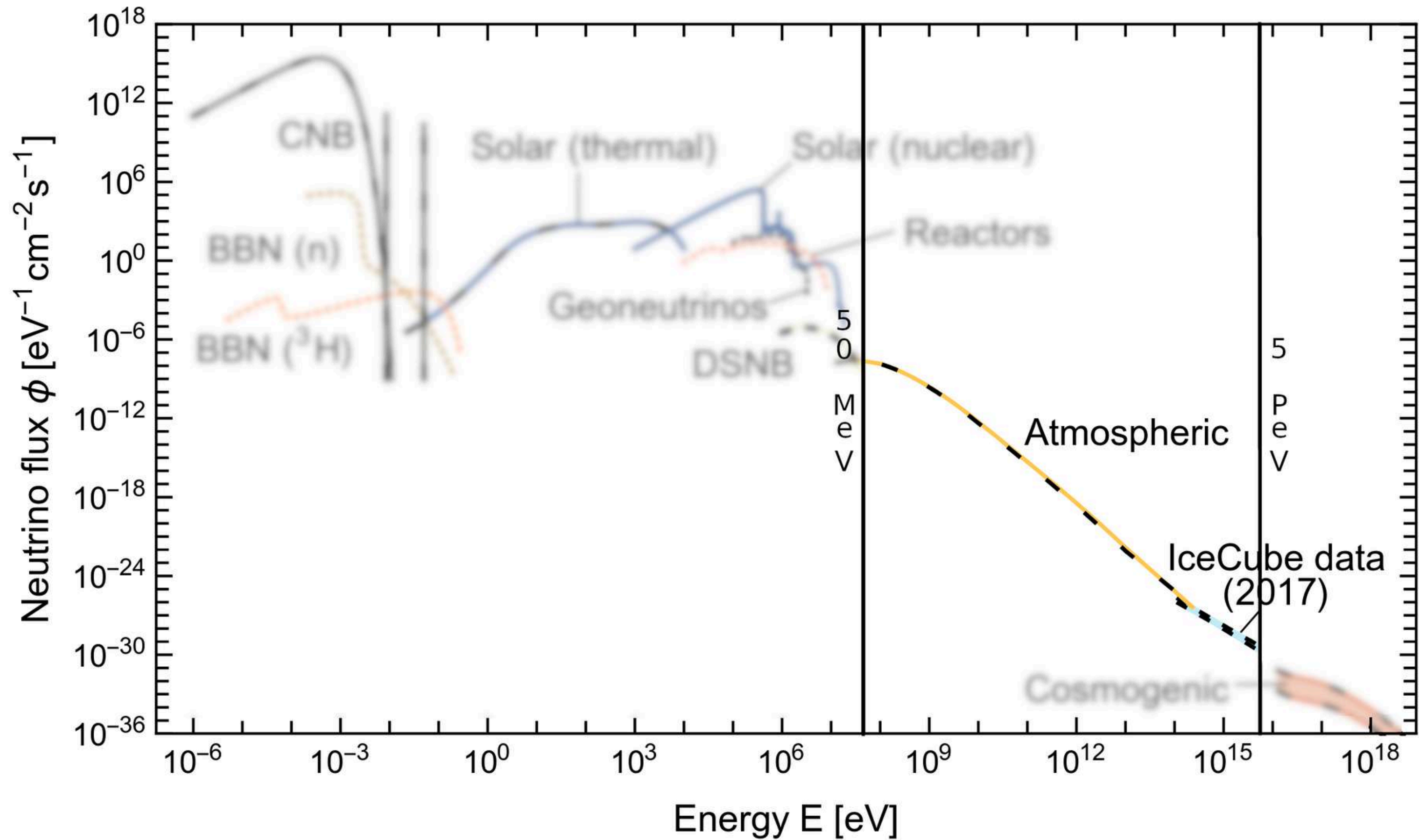


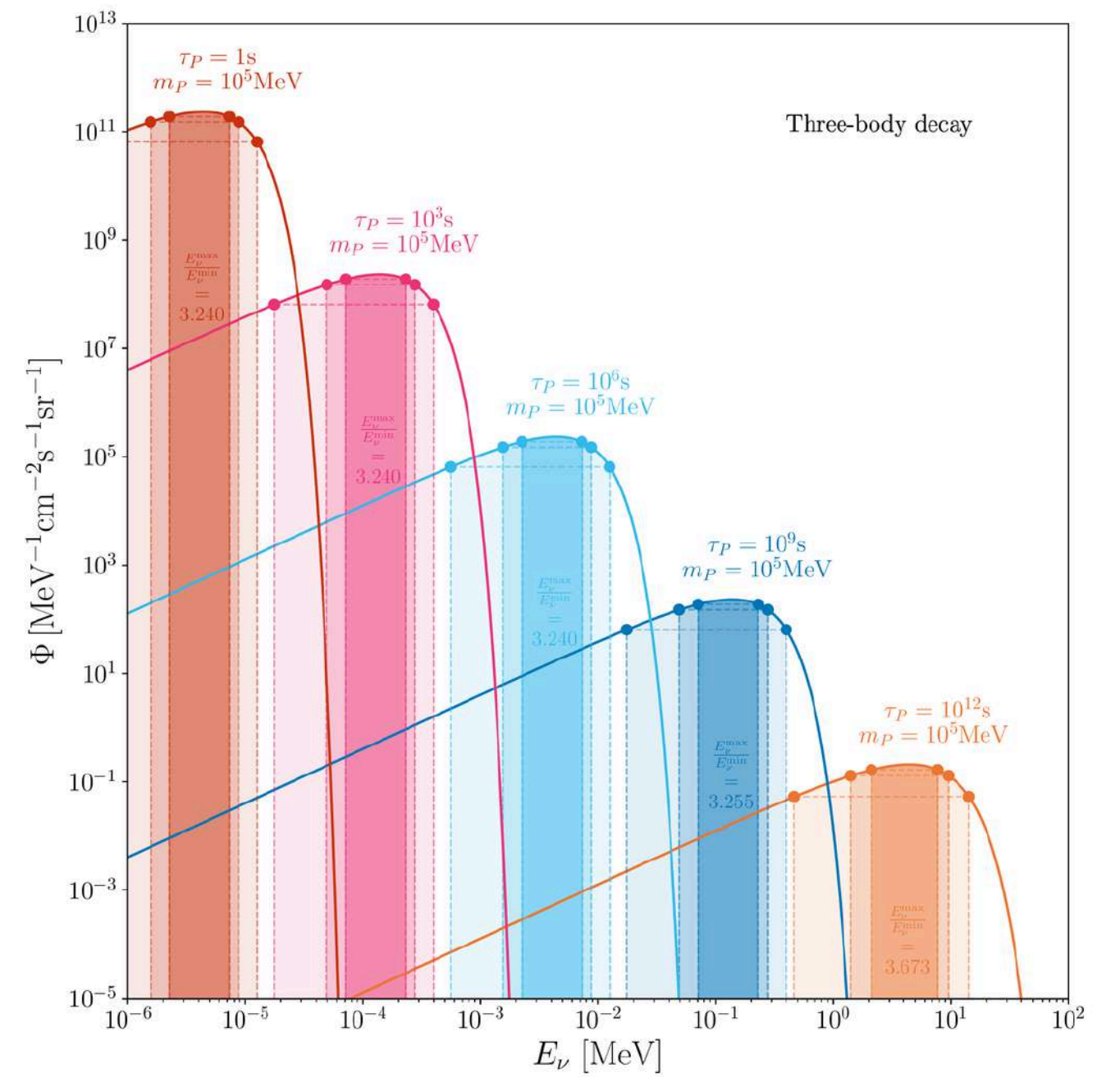
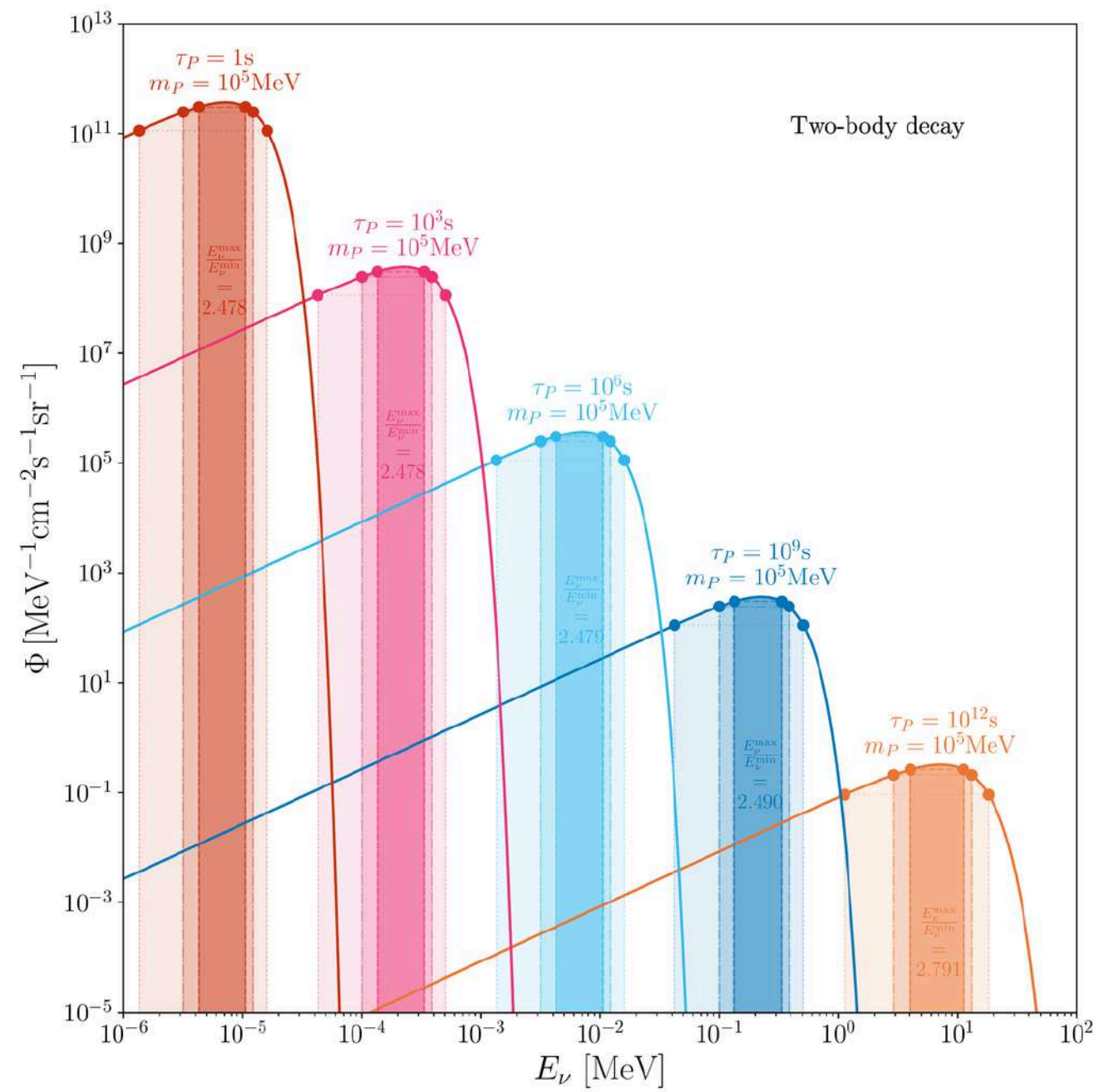
Bianco, Depta, Frerick, Hambye, Hufnagel, Schmidt-Hoberg 25'

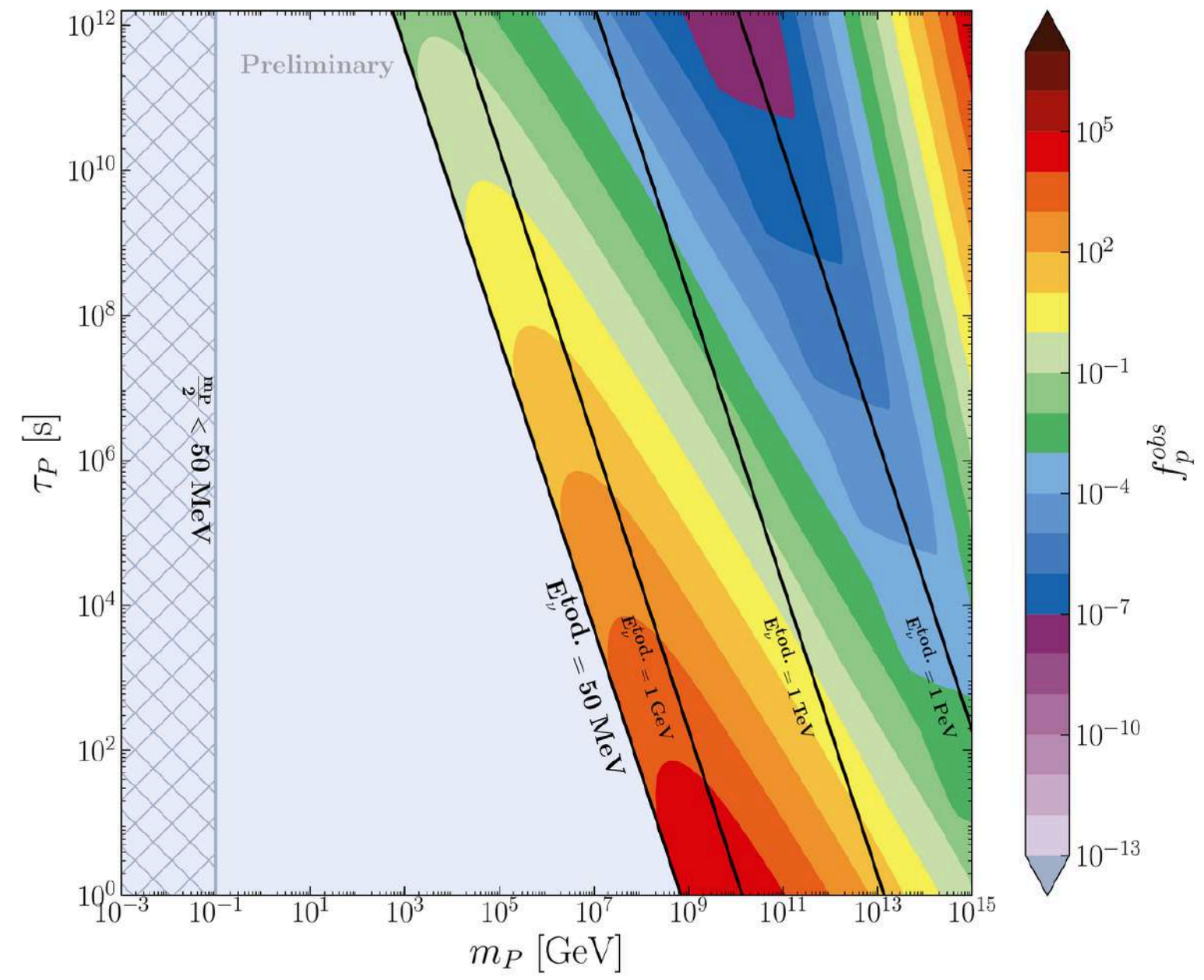
BBN constraints.

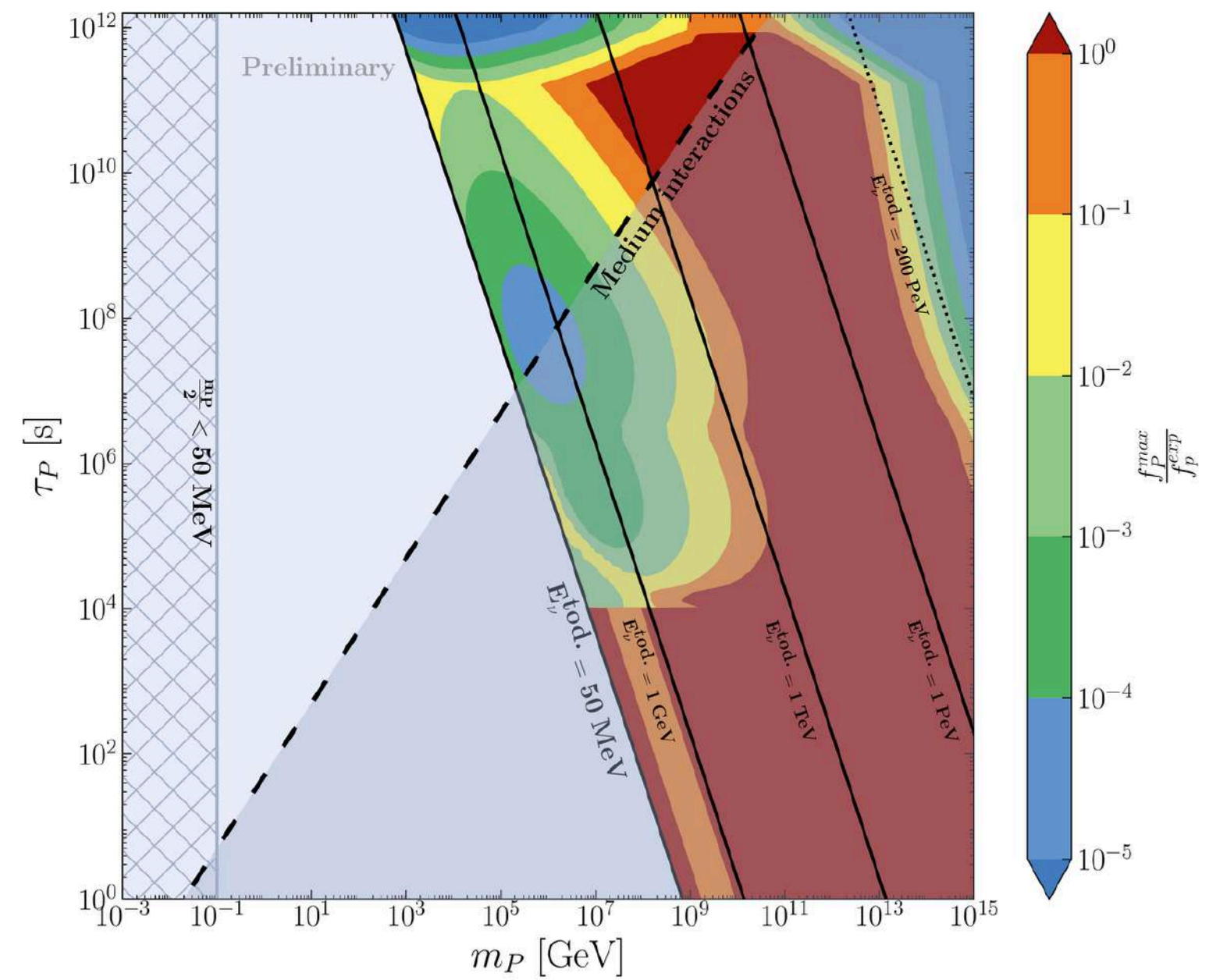
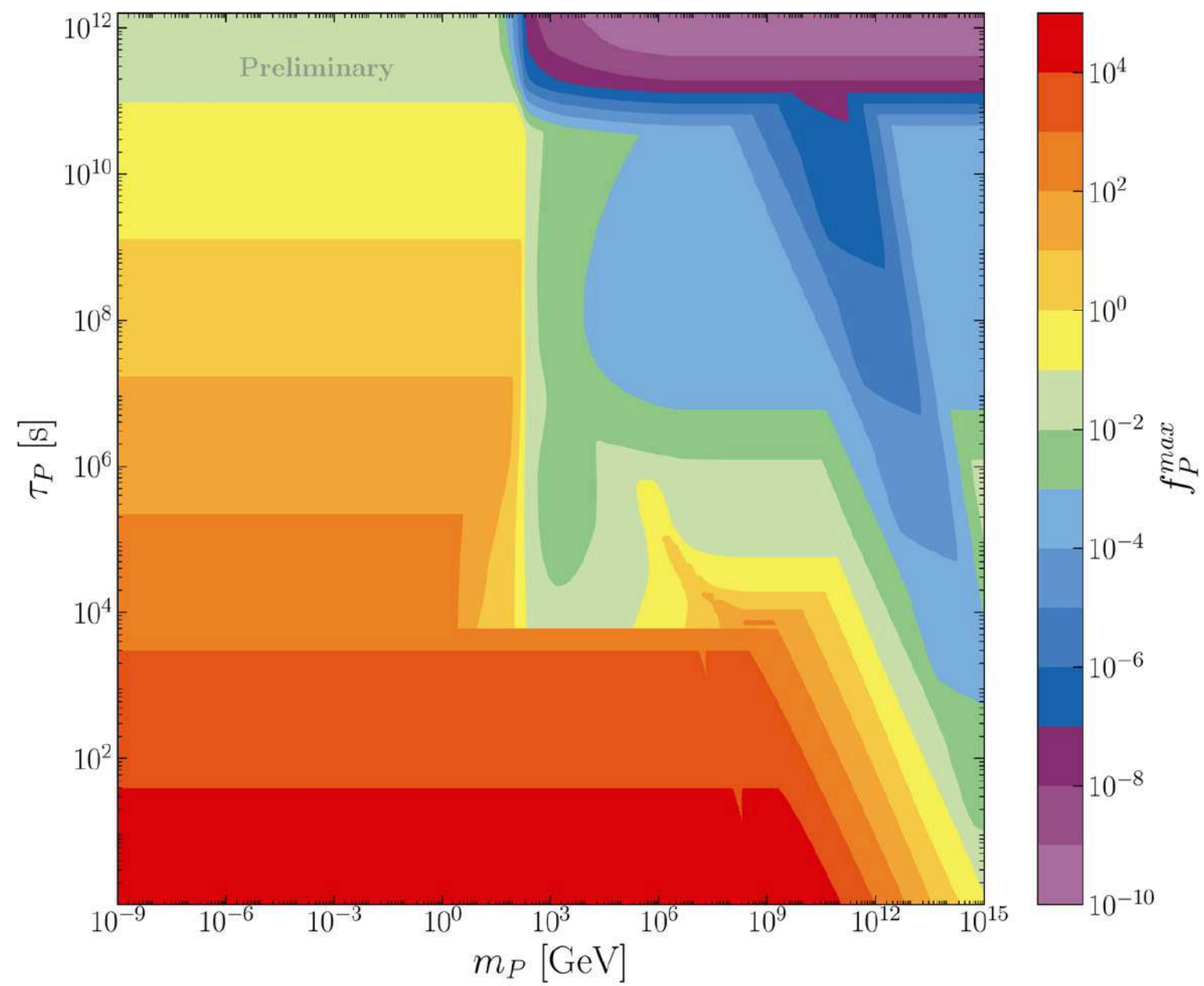


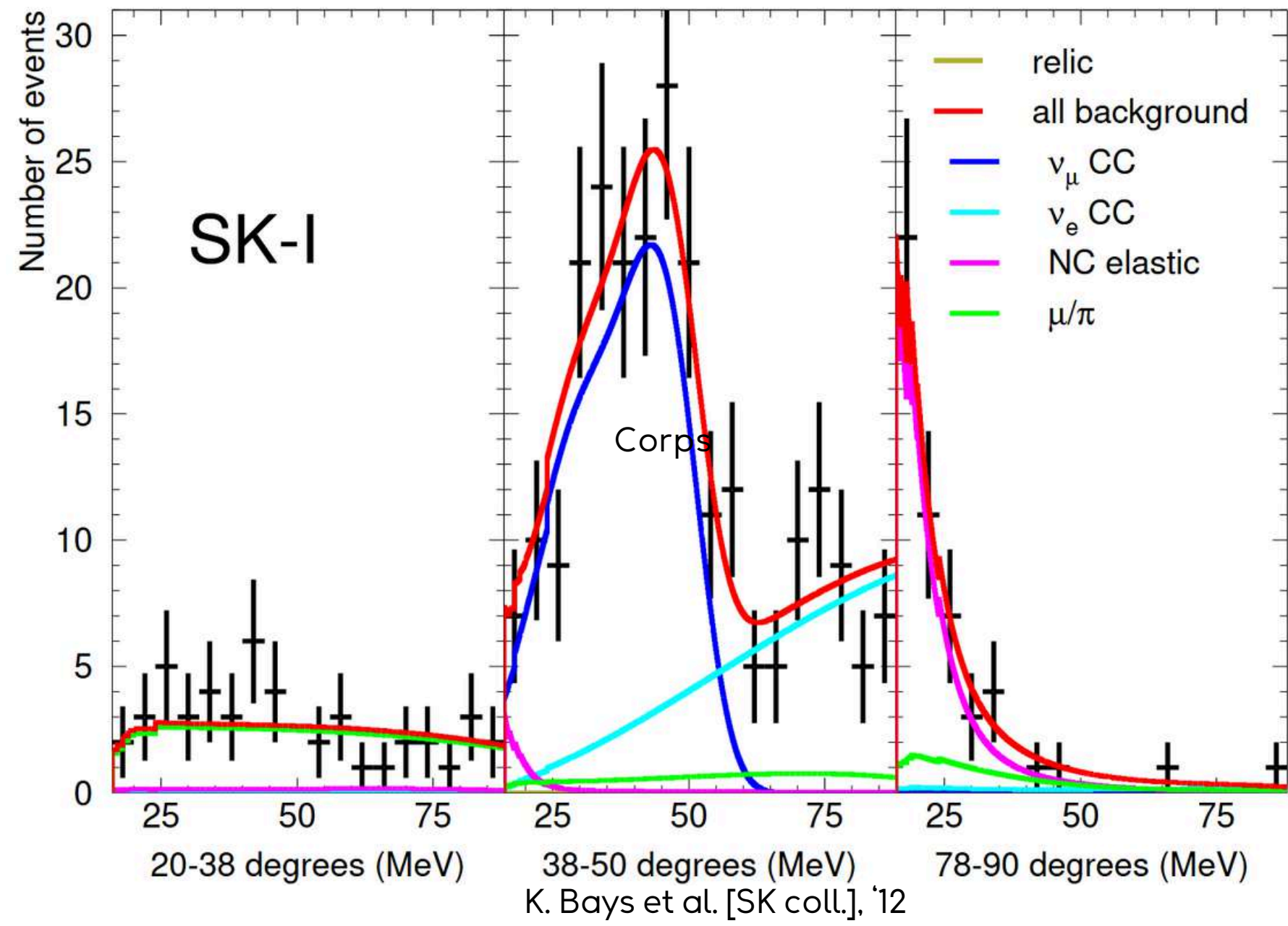
Bianco, Depta, Frerick, Hambye, Hufnagel, Schmidt-Hoberg 25'

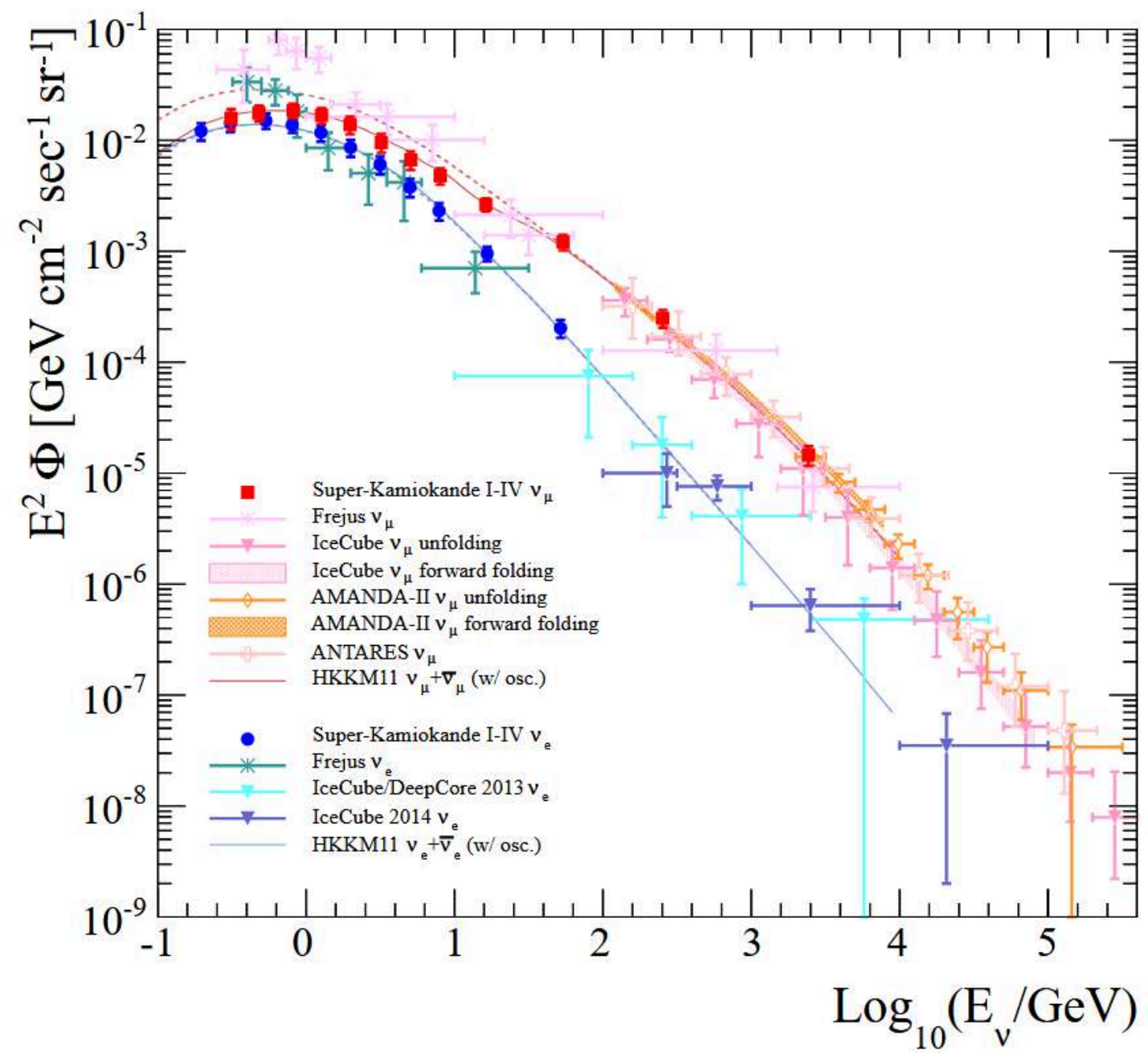












Richard et al. [SK Coll.] 15'

Models

- Scalar triplet
- Majoron
- Vector decay (Coy, Hambye '20)

